

# Stark broadening of Kr He- $\beta$ lines for electron-density measurement on NIF

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# Summary

- Kr He $\beta$ , 15.43 keV,  $\Delta E=400$  eV or 1.4 keV, Ge (220),  $\theta_B=11.6^\circ$ ,  $\Delta\theta_{RC} \sim 41$   $\mu$ rad,  $\Delta E_{RC}=3$  eV
- Cylindrical
  - Rays from 2-cm high crystal ( $\Omega \sim 1.3 \times 10^{-6}$  sr) fit within a 400- $\mu$ m slit
  - Energy spread over 100- $\mu$ m detector “pixel”: 5.5 eV (-> 6.25 eV total)
  - High quality concave cylindrical lenses are available as substrates
- Conical
  - Rays from 2-cm high crystal fit within a 200- $\mu$ m slit
  - Narrow spatial peak will provide better time resolution with DISC
  - Energy spread over 100- $\mu$ m detector “pixel”: 7.5-9 eV for 100- $\mu$ m or 500- $\mu$ m slit
  - Substrate requires special fabrication
- Cone length 23.5 mm, angle:  $23.545^\circ$ ,  $r_{min}: 95.447$  mm,  $r_{max}: 100.14$  mm
- We plan to obtain both a cylindrical and a conical crystal for evaluation
- Layout drawings to confirm clearances relative to other systems in progress

# R&D progress has been made on DIM-based high resolution x-ray spectrometer

- Physics parameters to measure
  - $T_e$  from dielectronic satellites
  - $n_e$  from Stark broadening of He- $\beta$  lines
  - K or L<sub>3</sub> absorption edge spectra with high resolution
  - Doppler  $T_i$
- Focused on two experiments
  - Time resolved measurement of Kr He $\beta$  in symcap
    - $n_e$  from Stark broadening
    - $T_e$  from dielectronic satellites
  - XAFS of Cu K or Ta L<sub>III</sub> edge
- Estimated performance metrics
  - X-ray intensities
  - Spectrometer throughputs
  - Signal levels at detector
  - Optimization of S/N
  - Resolution expected
- R&D performed
  - Analytically evaluated six spectrometer geometries
  - Experimentally evaluated four spectrometer geometries

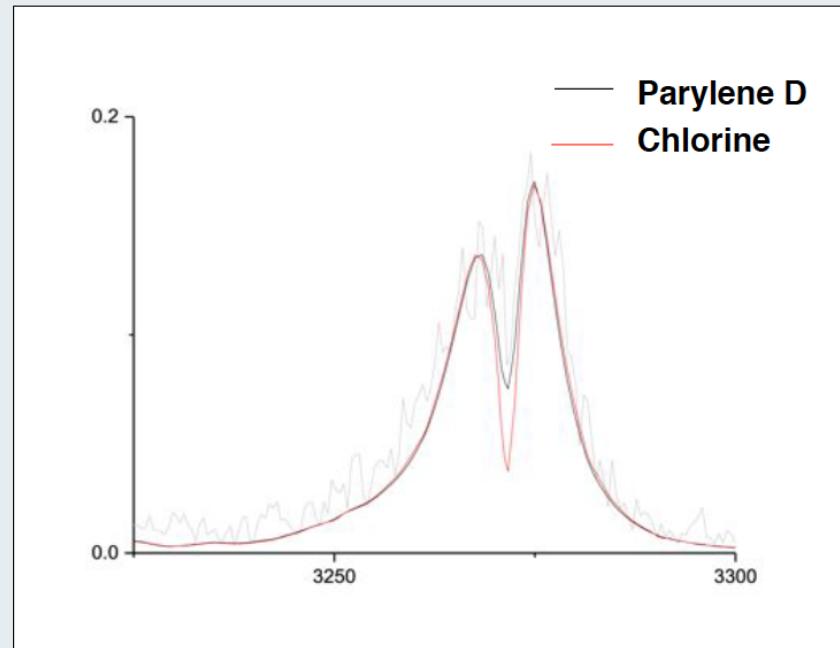
# We have developed analytical optical tools and experimentally studied several spectrometer geometries

- **Spatially focusing – best for streak camera**
  - Optimal S/N
  - Sagittally focusing Johann ( $\theta > 45^\circ$ ) (TITAN, ORION) – excellent spectral res. & sagittal focusing
  - Spherical crystal von-Hamos-like geometry ( $\theta < 45^\circ$ ) – *ditto* but low throughput in DIM geometry (small Bragg angle)
  - **von Hamos (cylindrical)** –  $\Omega \sim 2 \times 10^{-6}$  sr
  - **Conical crystal von Hamos**
- **Spatially diverging – for area detectors**
  - Suitable for framing camera or image plate
  - Modified Johann (source inside Rowland circle)
  - Flat crystal
  - Convex spherical crystal
  - 2D logarithmic spiral
- **Advanced concepts**
  - 2D and 3D Logarithmic spiral
  - Spherical crystal with detector near Rowland circle

# Electron-density measurement by Stark broadening of Cl He- $\beta$ lines was demonstrated on ORION

## Fit of the chlorine He- $\beta$ line with ALICE

- Ion dynamics changes the line shape by filling in the central dip
- ALICE treats the three species in PyD ( $C_8H_6Cl_2$ ) self-consistently
- The calculations assume a temperature of  $T_e = 550$  eV and a density of  $3.0 \text{ e}^{23} \text{ cm}^{-3}$



Beiersdorfer *et al.*

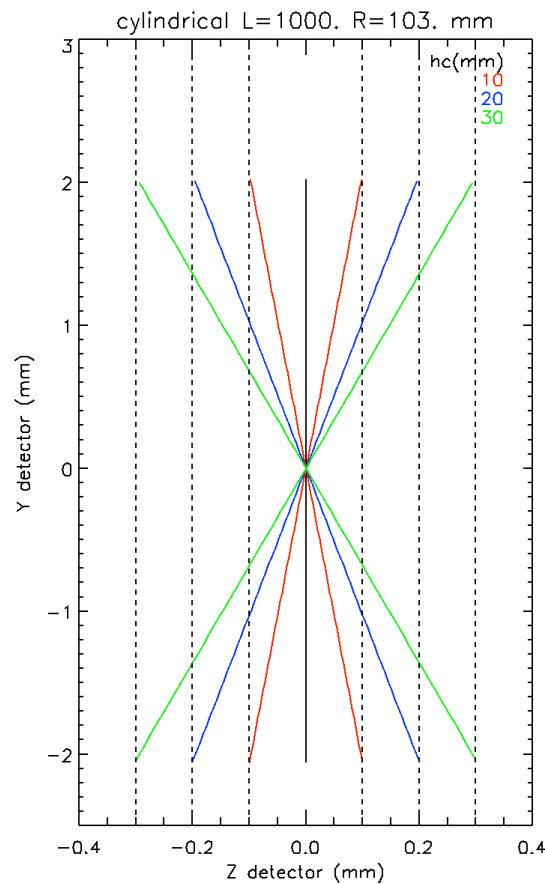
# Photonics were estimated for two experiments

- Time resolved measurement of Kr He $\beta$  in a symcap
  - $T_e = 3 \text{ keV}$
  - $n_e = 2 \times 10^{24} \text{ cm}^{-3}$
  - 0.01% Kr
  - 50  $\mu\text{m}$  symcap
  - Spectrometer solid angle =  $10^{-6} \text{ sr}$
  - $\rightarrow 7 \times 10^4$  photons in 30 ps

Simulation of ray paths for cylindrical  
and conical von Hamos spectrometers

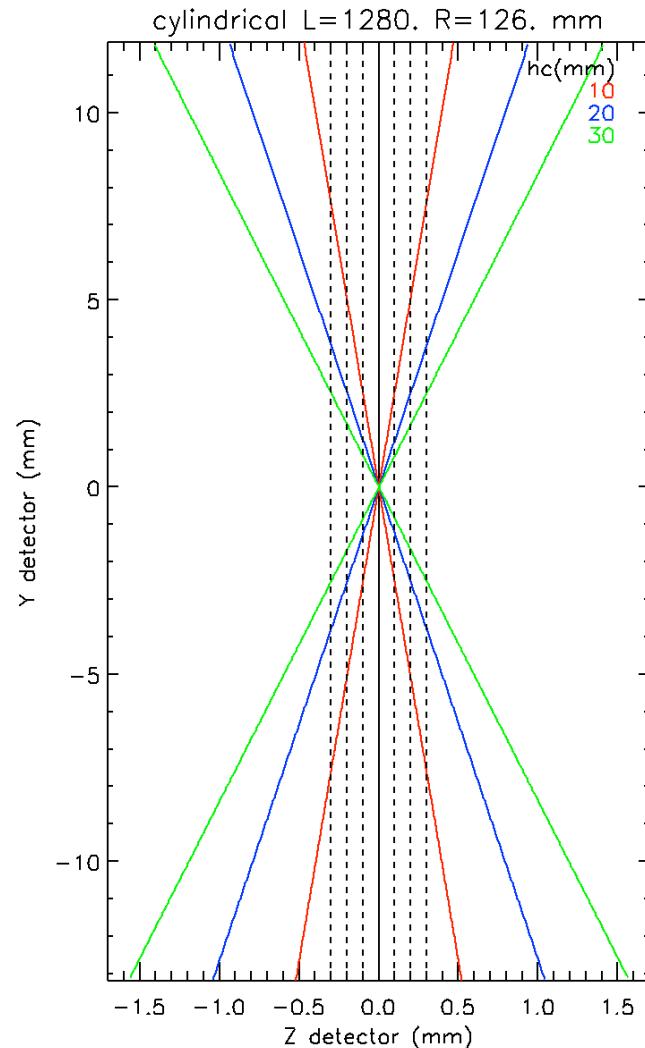
# For cylindrical von Hamos the image from a 2-cm high crystal fits within a 400 $\mu\text{m}$ slit (blue curves)

Boundaries of spectral-spatial image on detector



- The x-ray intensity is distributed spatially (Z detector) uniformly within the bowtie limit lines
- For a conical crystal the intensity is highly concentrated in the center of the slit
- Calculations for 400-eV bandwidth

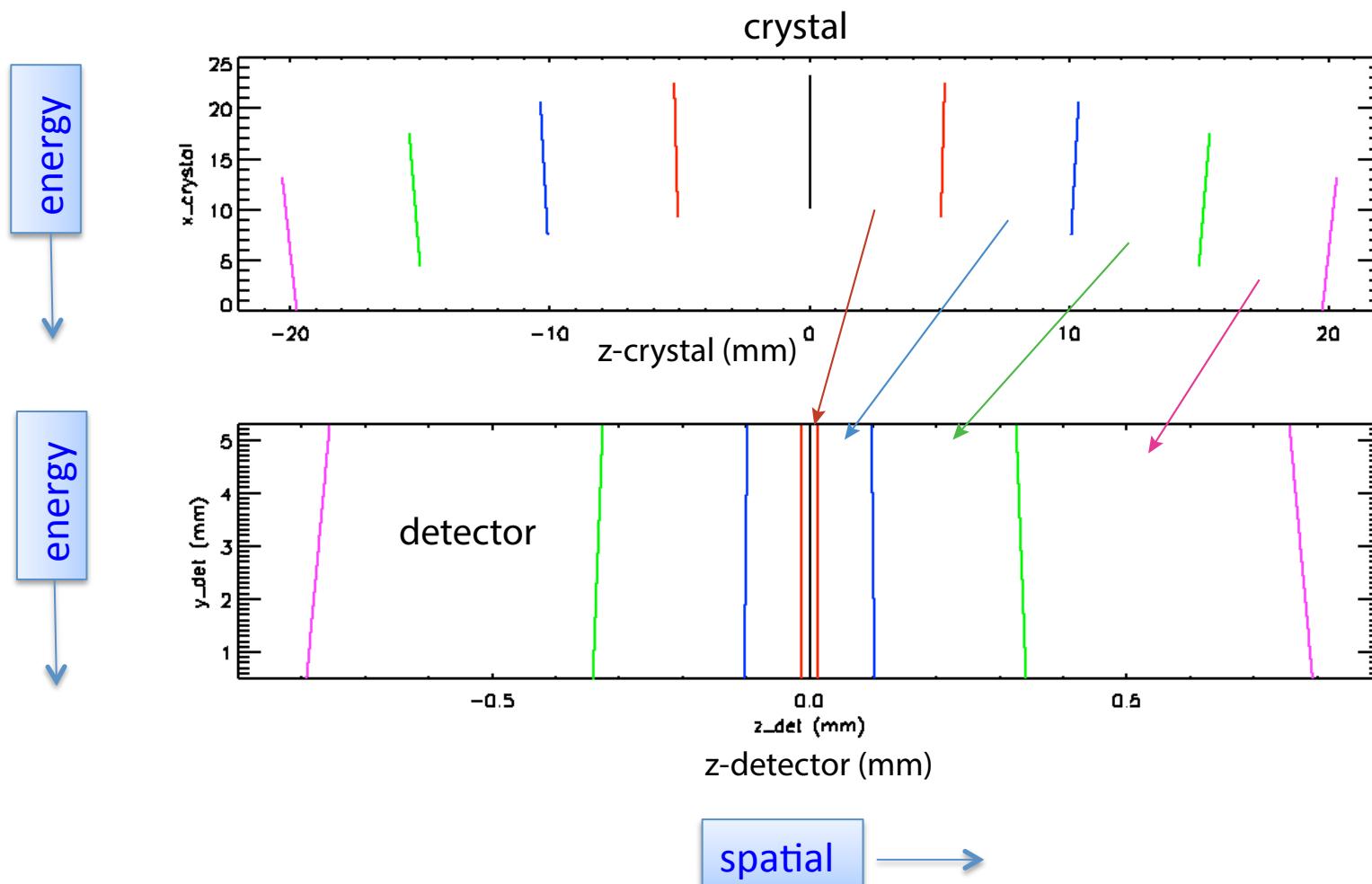
# The “bowtie” effect broadening, however, is large if the full 25-mm photocathode is illuminated



- Cylindrical von Hamos
- 15.2 – 16.67 keV
- 10-cm high crystal fills a 1-mm wide slit (red lines)

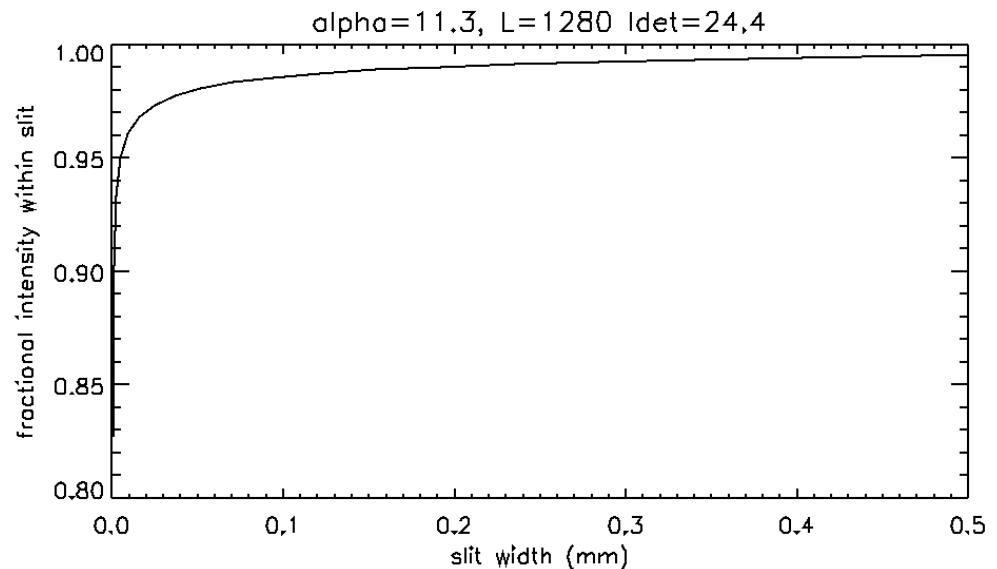
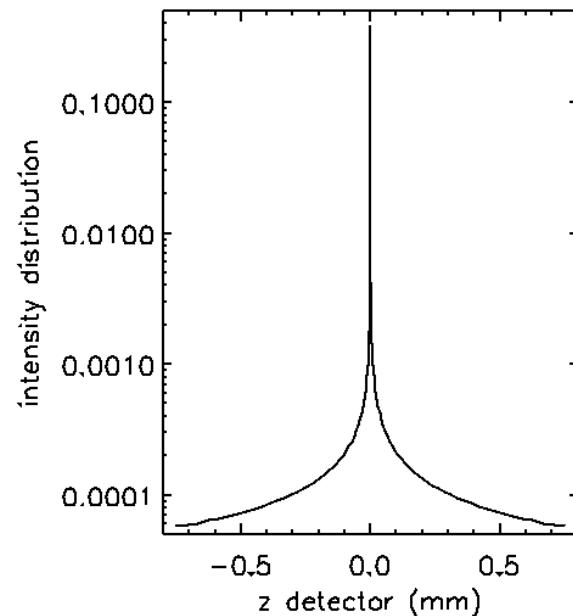
# X-ray intensities from equal areas of crystal are concentrated toward center of detector in the conical crystal geometry

All x rays from a 20-mm high crystal are concentrated inside a 200  $\mu\text{m}$  detector slit

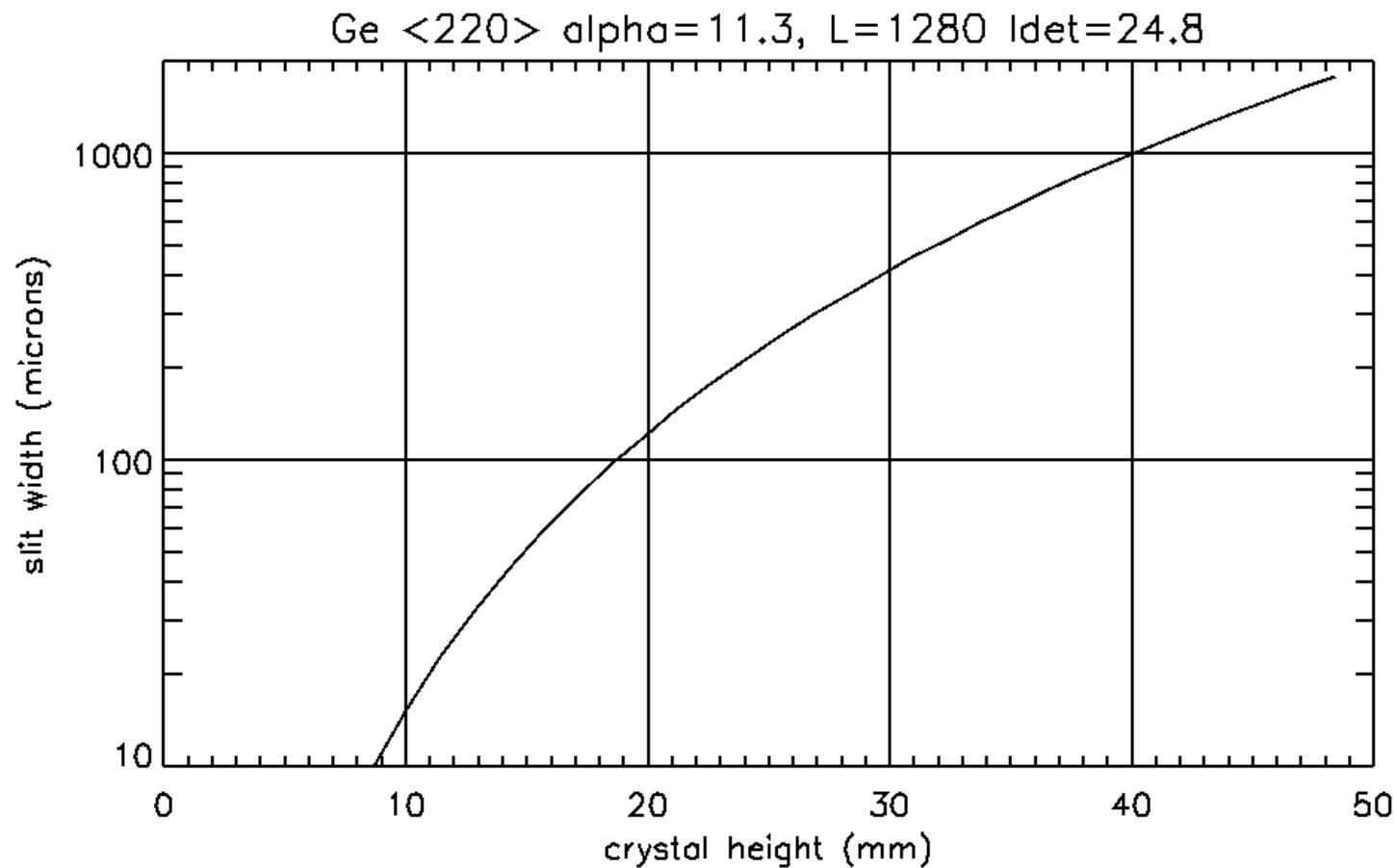


# Most of the intensity is concentrated in a narrow line (conical crystal)

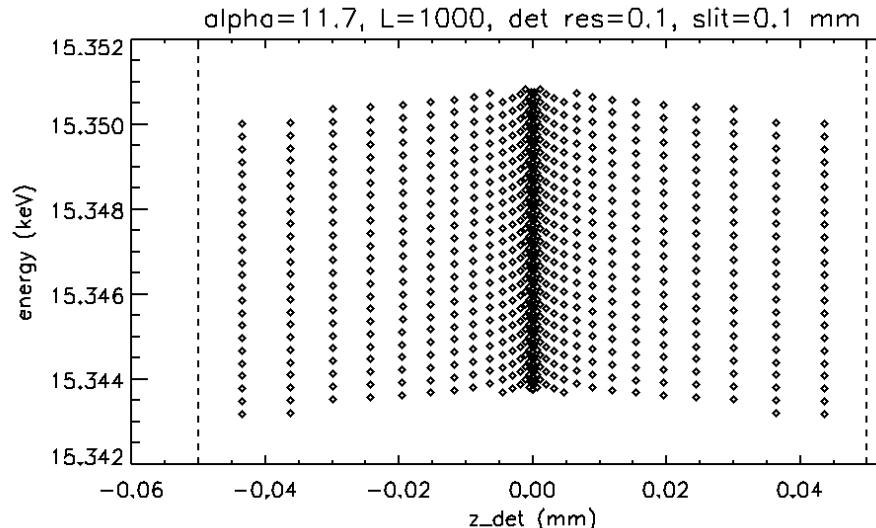
98% of intensity falls within 100  $\mu\text{m}$  slit



# The spatial width of the spectrum increases with crystal height



# The energy spread falling on a 100- $\mu\text{m}$ detector “pixel” within 100 and 500- $\mu\text{m}$ wide slits is 7.5-9 eV

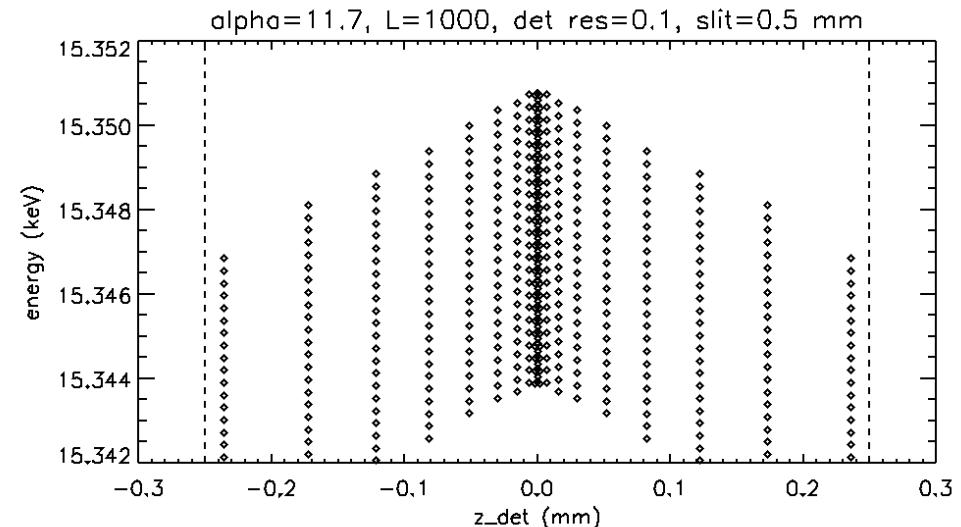


100- $\mu\text{m}$  slit

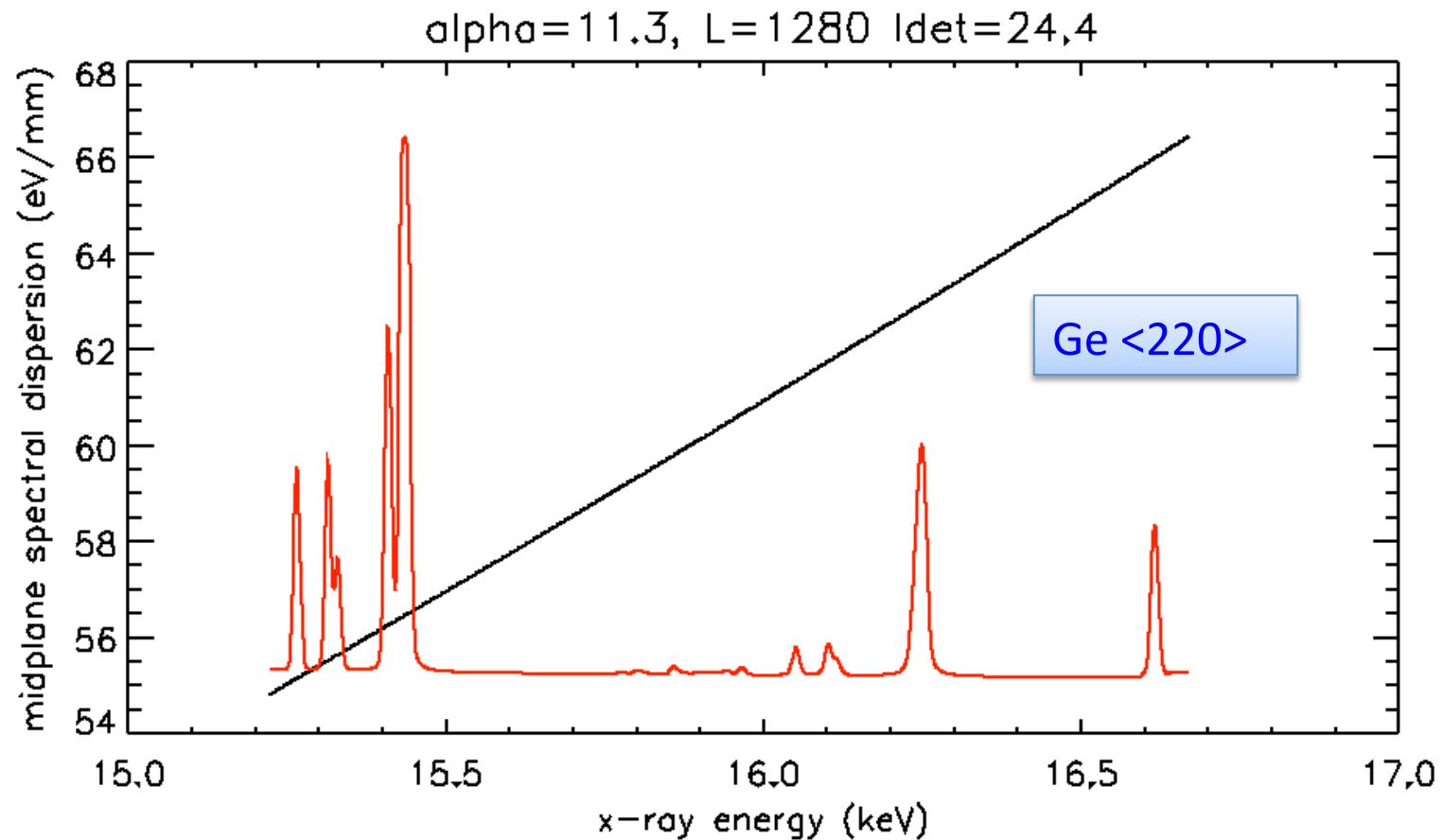
500- $\mu\text{m}$  slit

conical

versus 5.5 eV for a flat or cylindrical crystal



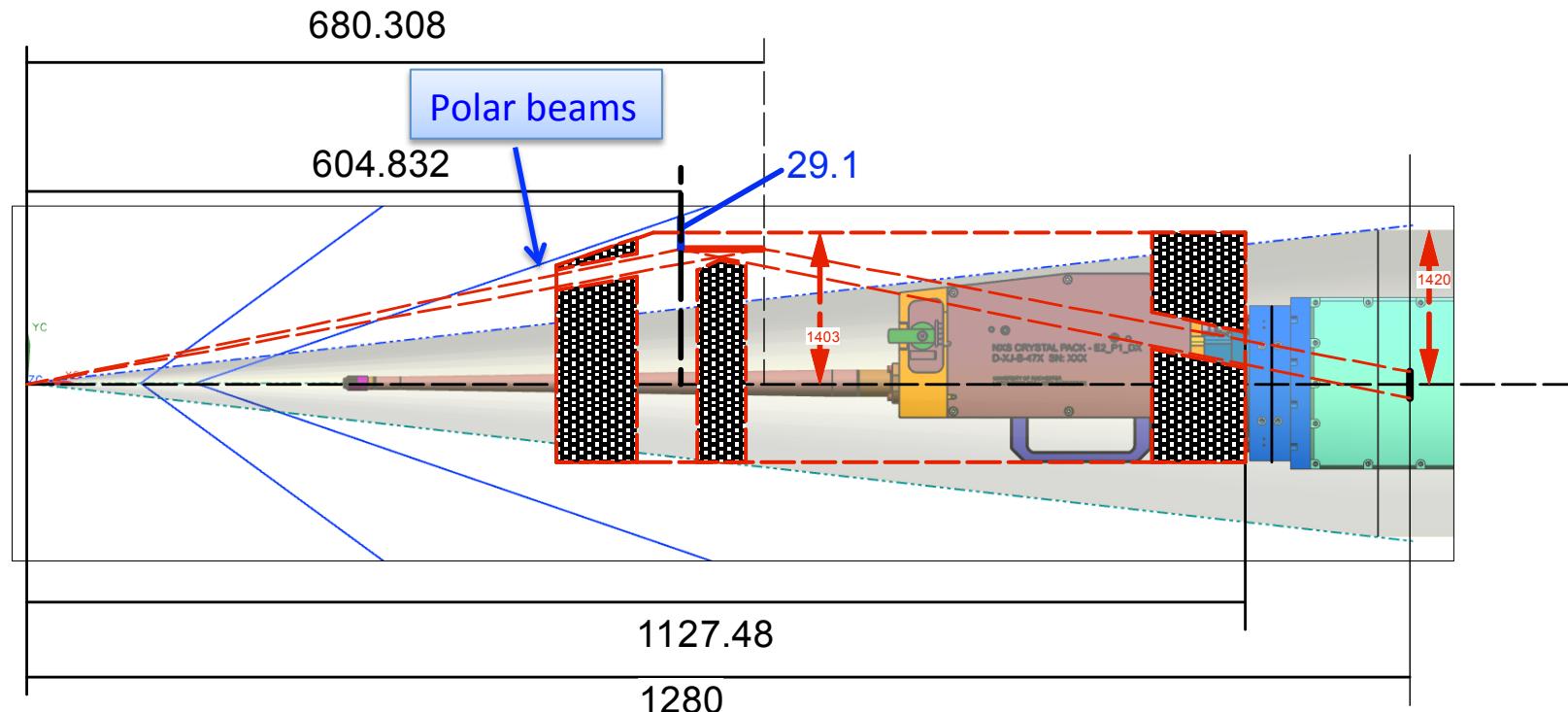
For L=1280 mm a 25-mm photocathode just barely includes the Kr He- $\delta$  line



The inverse dispersion ranges from 55 to 66 eV/mm

# Mechanical layouts

An NXS drawing was used to estimate clearance of a conical crystal HiRes relative to the polar beams and TIM envelope

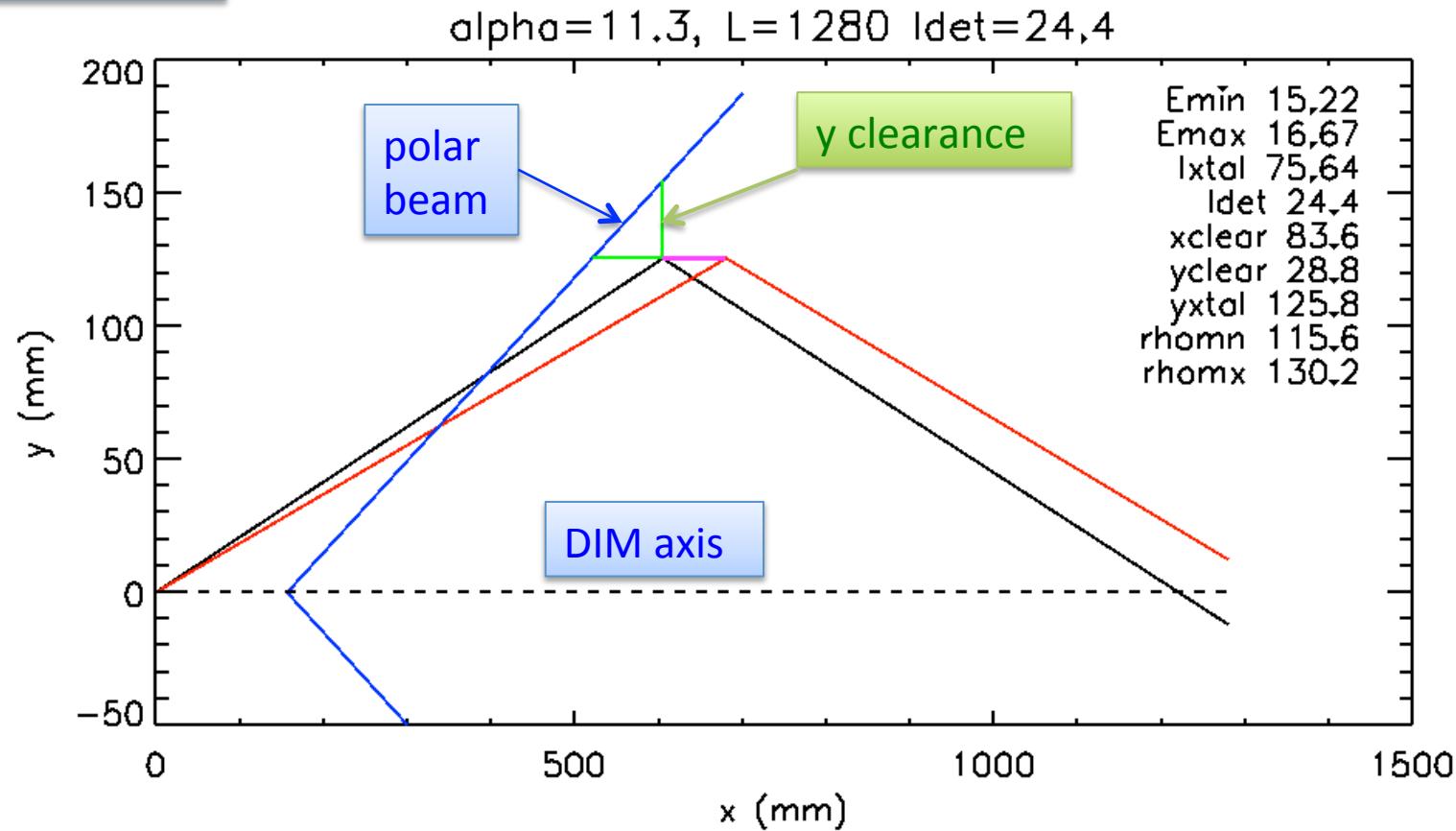


- For L=1280 mm from TCC to DISC photocathode, the front end of the crystal clears the polar beam by 29 mm
- More accurate CAD layouts are being done

# Graphing the x-ray paths in our IDL program allows study of the crystal clearance for different values of L

Ge <220>

Note: Drawing is not isotropic!



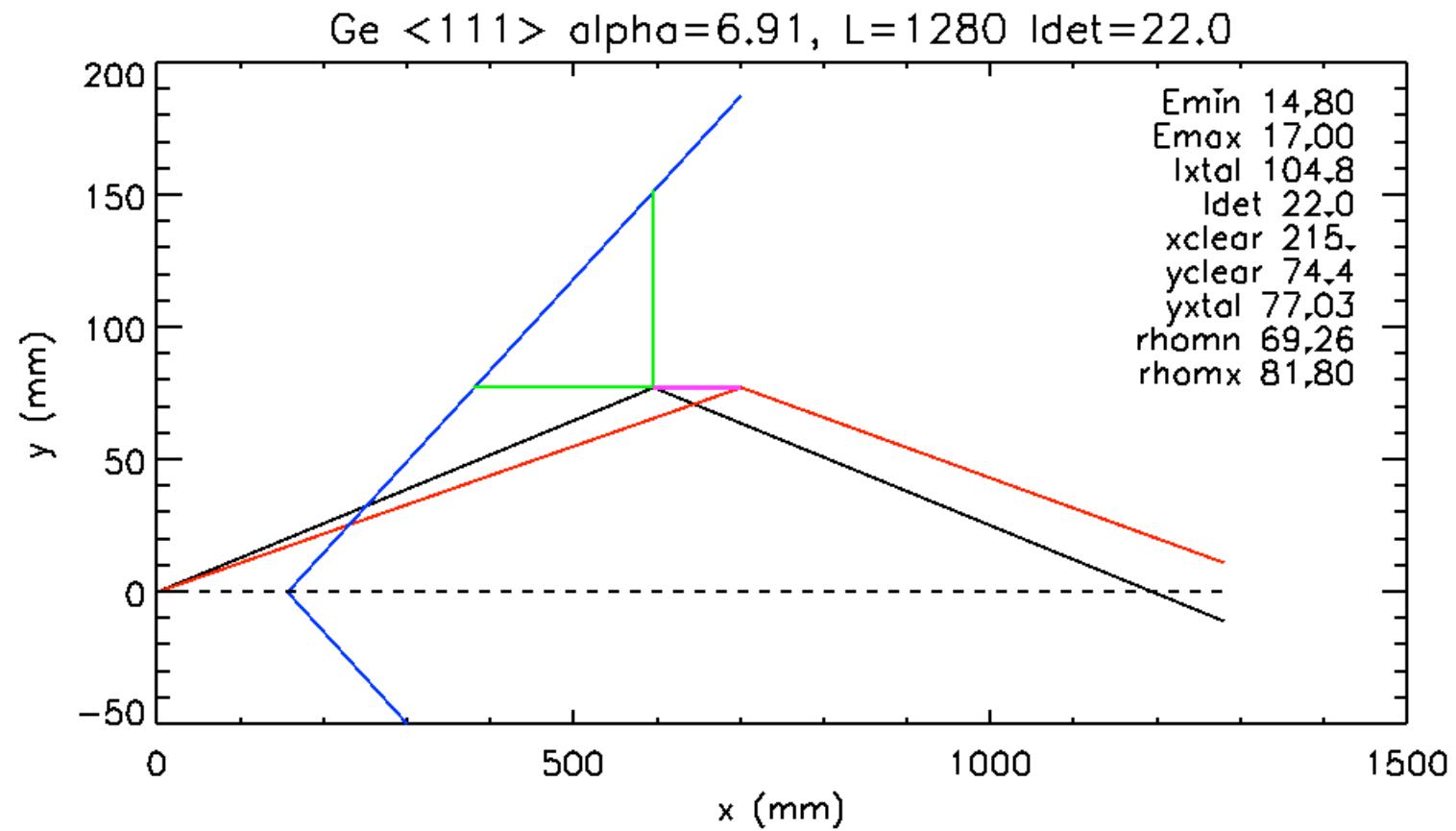
# Larger L (TCC-to-detector) clears polar beams better but may violate TIM stay-in radius requirement

All distances in mm (Ge <220>)

L	x clearance	y clearance	detector length	y-crystal
1000	31.1	10.7	19.1	108.1
1100	49.8	17.2	21.0	117.9
1280	83.6	28.8	24.4	125.8
1350	96.7	33.3	25.8	132.7

- y-crystal is distance from axis to front surface of crystal; add thicknesses
- x,y clearances are x,y distances of left front edge of crystal from polar beam
- Need to add thicknesses of crystal/substrate, crystal holder, cassette wall
- Detector lengths for E from 15.22 to 16.67 keV

A Ge <111> crystal fits inside a smaller cassette,  
but the spectral resolution is poorer



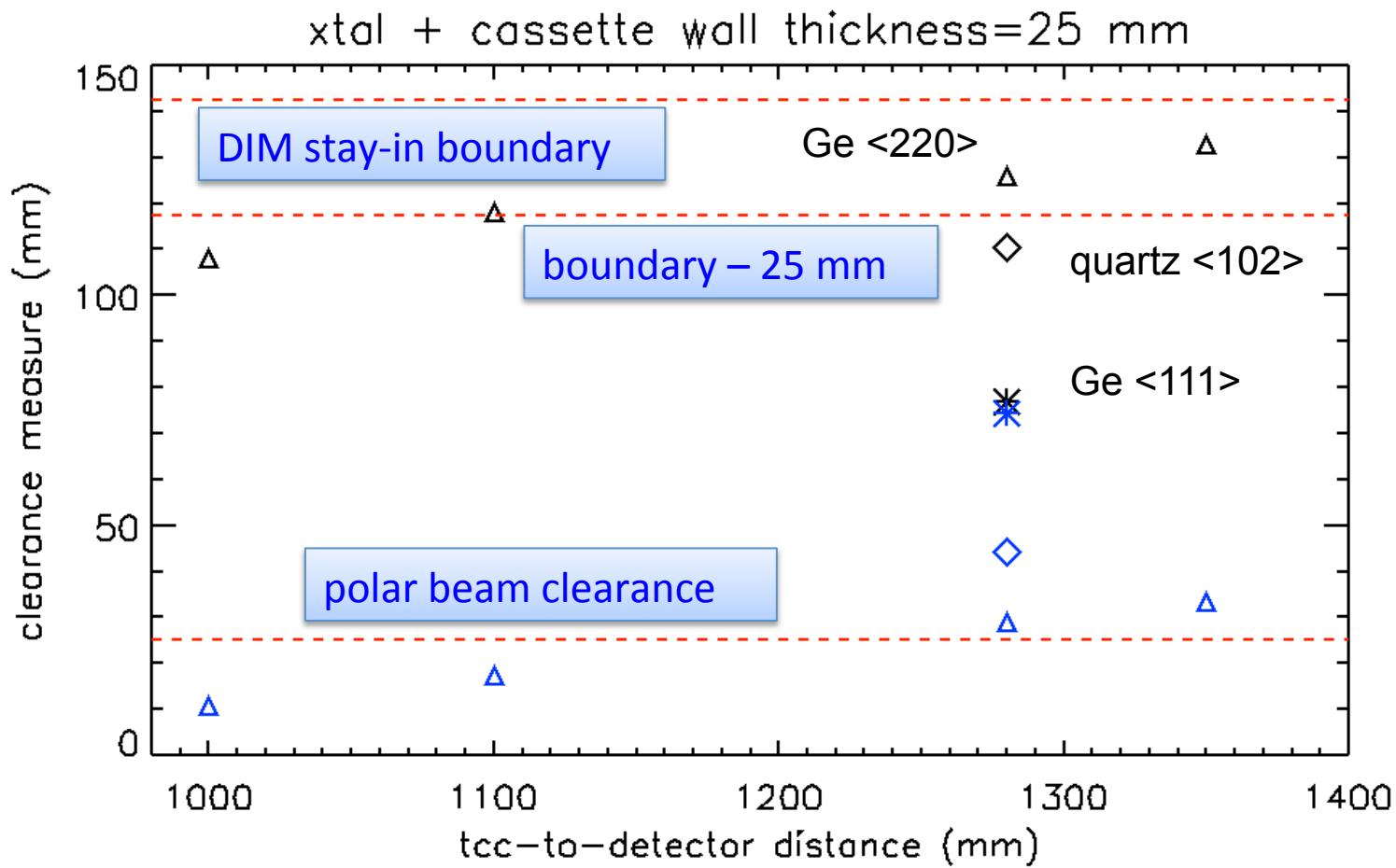
# The quartz <102> and Ge <111> crystals allow better clearance

All distances in mm

L	x clearance	y clearance	detector length	y-crystal	Crystal	Bragg angle
1280	83.6	28.8	24.4	125.8	Ge <220>	11.59°
1280	128	44.2	22.6	110.4	quartz <102>	10.16°
1280	215	74.4	22.0	77.0	Ge <111>	7.06°

- But reflectivity of quartz <102> is one fifth that of Ge <220>
- Resolution of Ge <111> is poorer than that of Ge <220>

# Clearance from polar beams and cassette boundary requirement have been studied

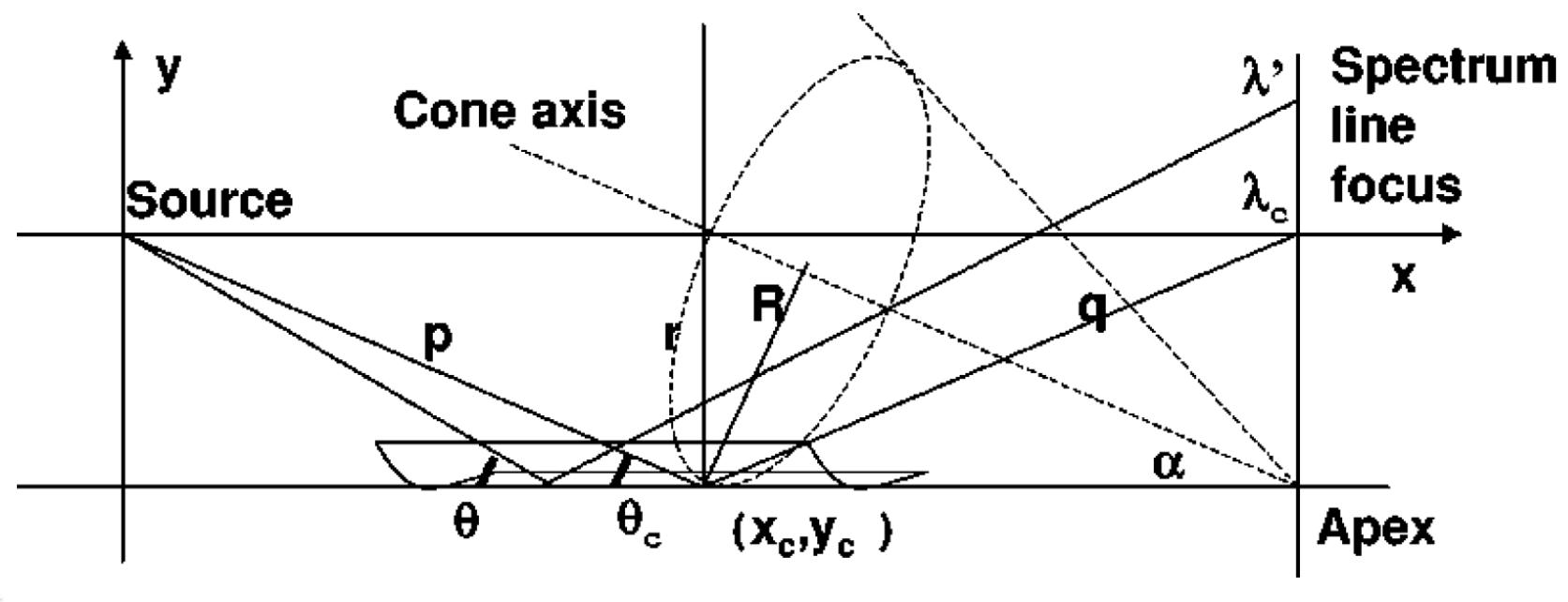


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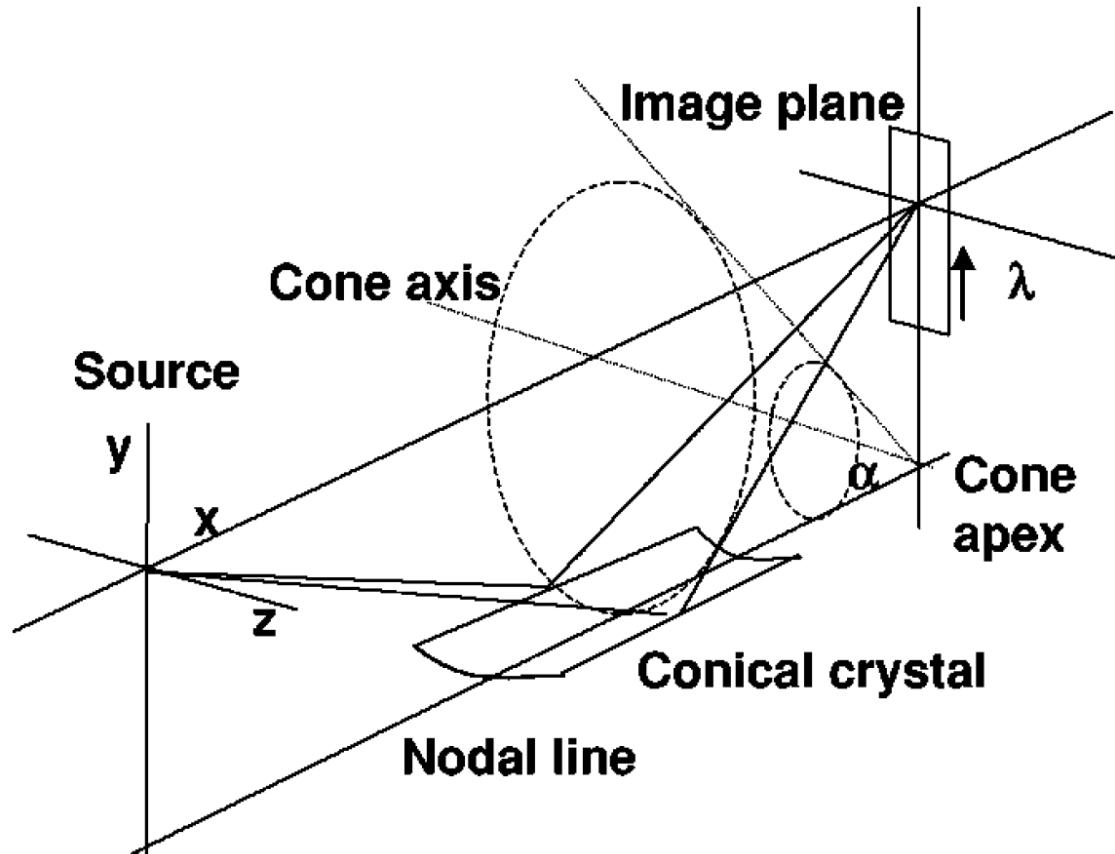
# EXTRAS

# Energy increases with x position on crystal and y position on detector



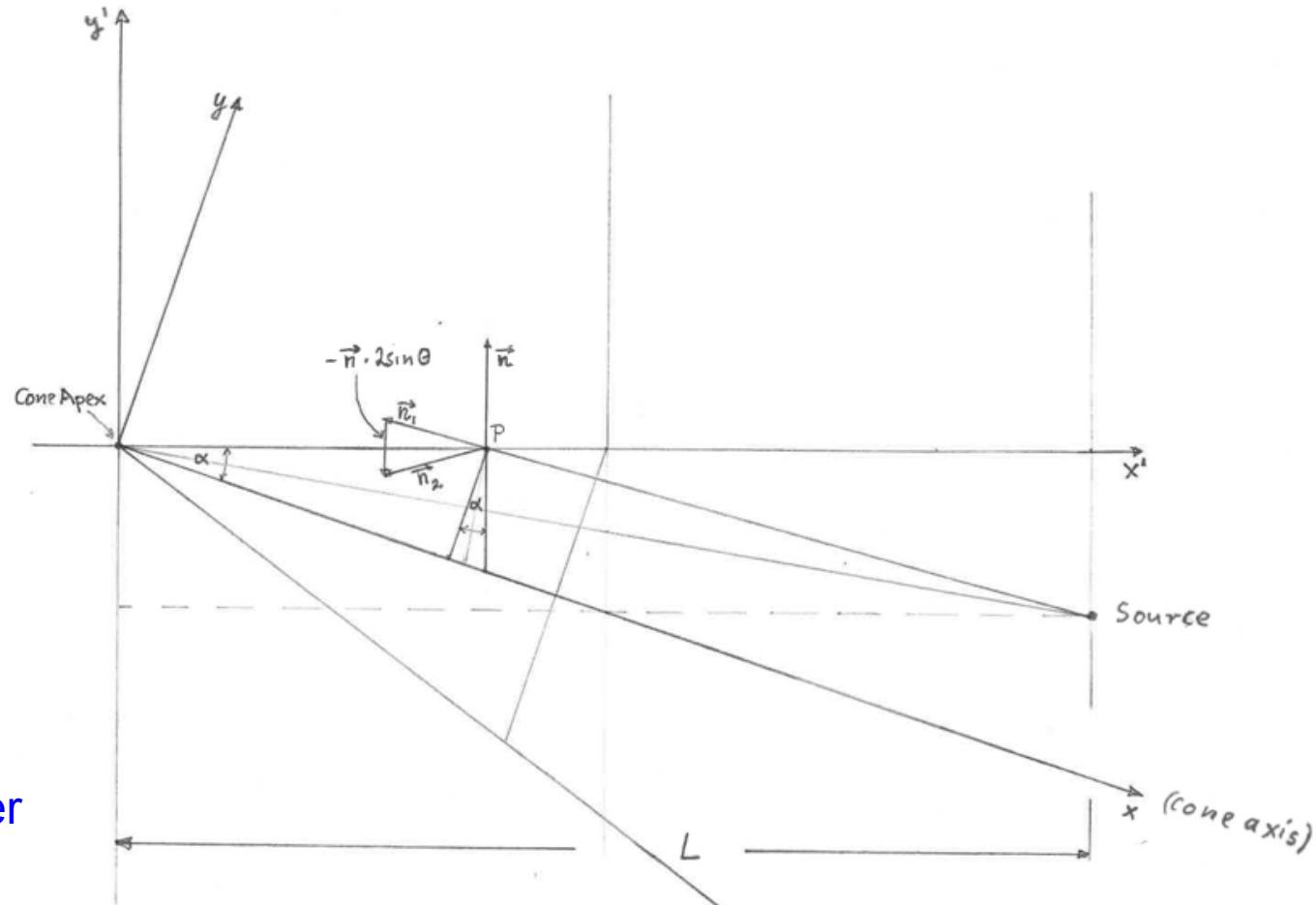
Martinelli, RSI (2004)

Z is the spatial coordinate in the image plane  
(detector)



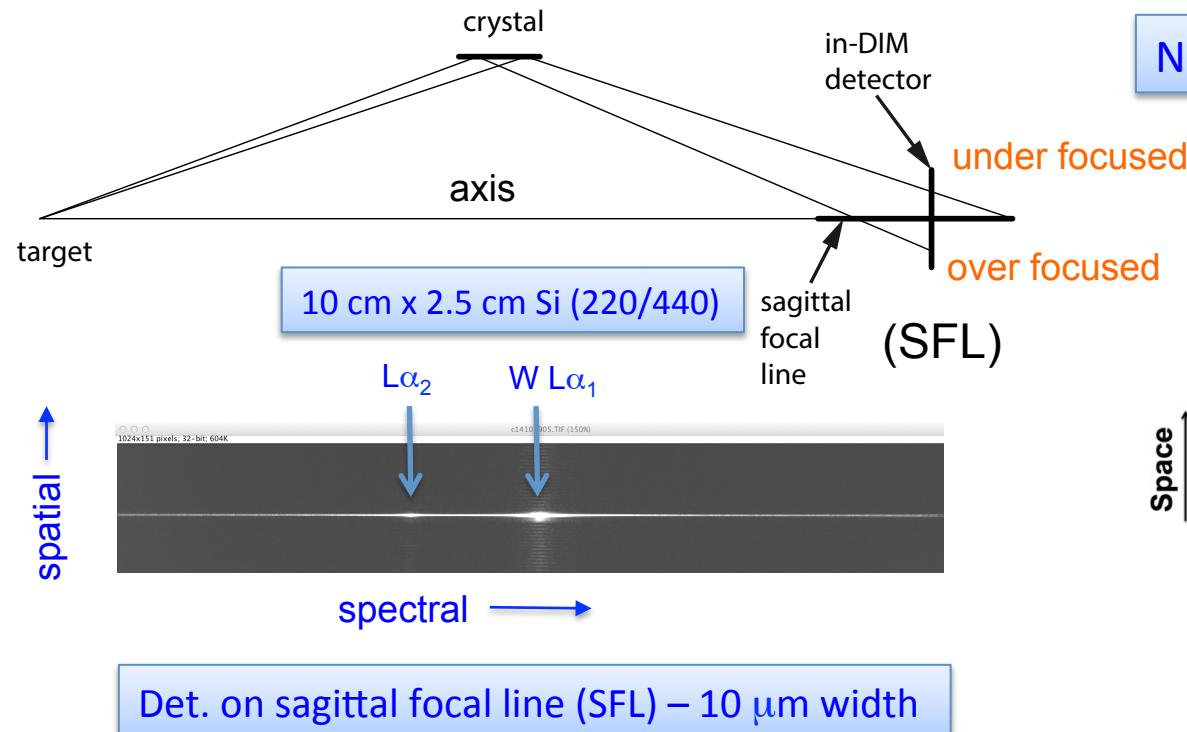
Martinolli, RSI (2004)

# Geometry used for the PPPL conical von Hamos calculations

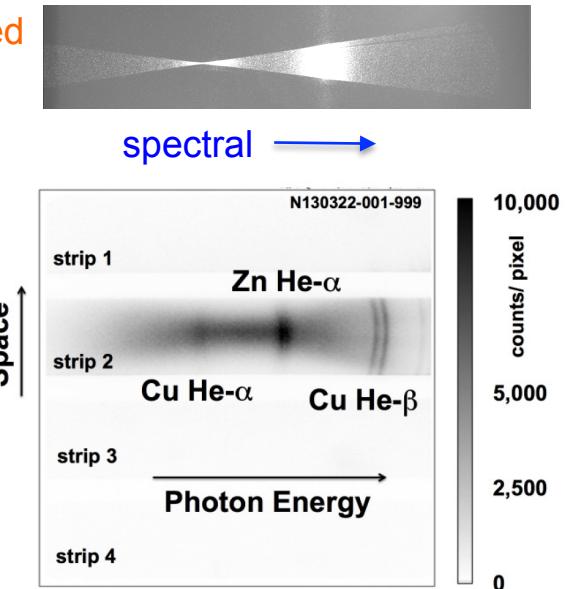


M. Bitter

For detectors perpendicular to the spectrometer axis the “bowtie” effect occurs for cylindrical or spherical crystals



Not on SFL => “bowtie” effect



Doeppner et al. RSI 2014

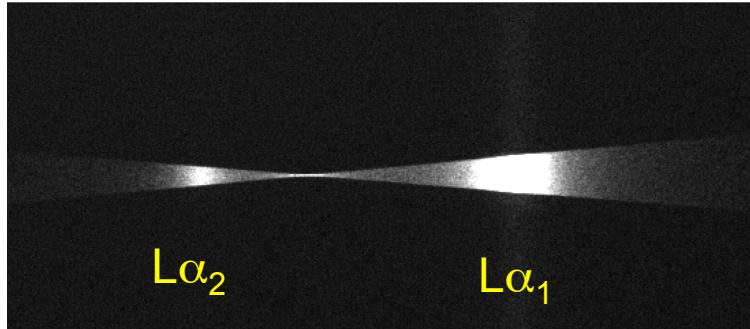
- Sagittal focusing greatly improves S/N ; may saturate detector
- Image plate for EXAFS can be on SFL
- “Bowtie” effect can affect performance for streak camera
- Consider putting GXD electronics to side of MCP, instead of behind

# We have been focusing on cylindrical and conical von Hamos configurations

- Kr He $\beta$ , 15.43 keV, Ge (220), 11.6° Bragg angle,  $\Delta\theta \sim 41 \mu\text{rad}$
- Solid angle  $\Omega \sim 2 \times 10^{-6} \text{ sr}$  for crystal height  $h_c=3 \text{ cm}$  and source-to-detector distance  $L=128 \text{ cm}$
- Dispersion along slit  $\sim 55 \text{ eV/mm}$  and on axis  $\sim 11 \text{ eV/mm}$
- For comparison, NXS with a flat Ge (220) crystal and 500  $\mu\text{m}$  slit has  $\Omega \sim 1.7 \times 10^{-8} \text{ sr}$  ( $\phi=0.04/97 \sim 4.2 \times 10^{-4}$ )

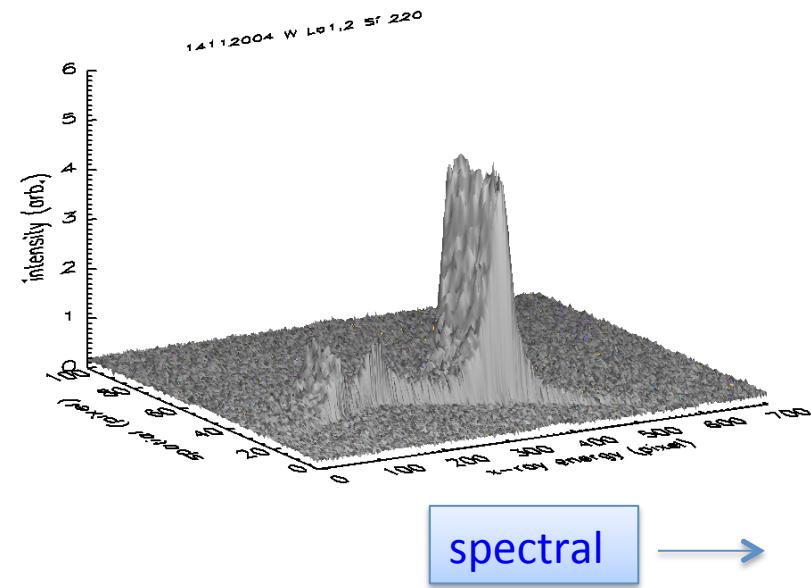
# The bowtie is 370 $\mu\text{m}$ high at the tungsten $\text{La}_1$ line

But the OMEGA EP streak-camera slit can be placed on the sagittal focal line



spectral →

- Line separation is  $\sim 62$  eV and 2.98 mm on CCD
- Si 220,  $\theta=23^\circ$ , R=35 cm, 8 cm x 2.5 cm, crystal-detector distance=20 cm

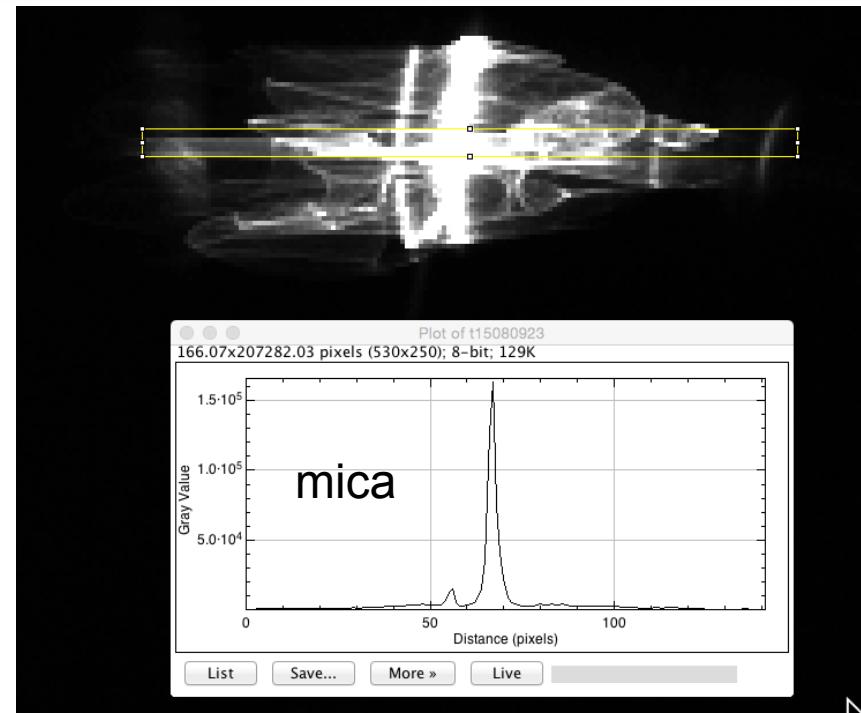
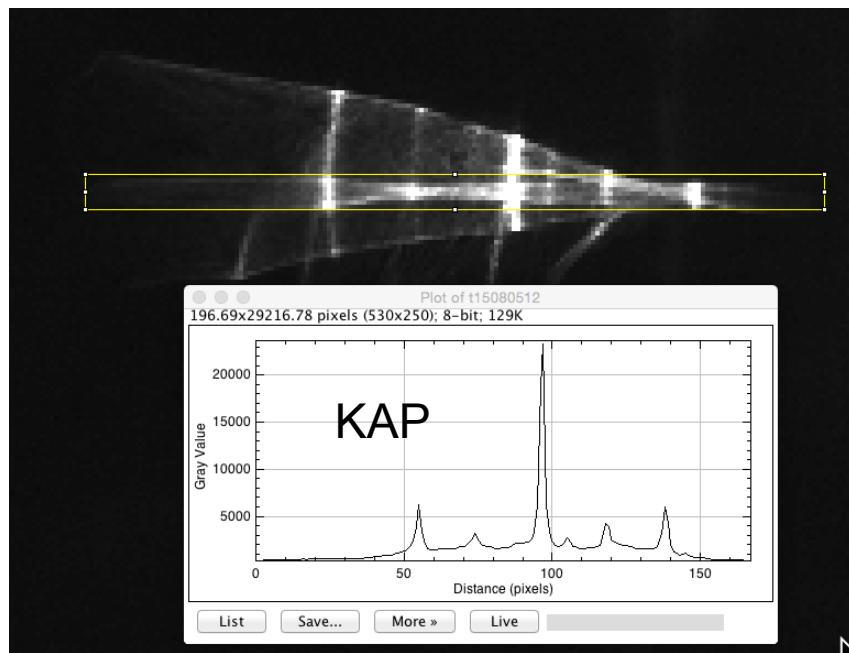


# Photonics were estimated for two experiments

- Time integrated XAFS of Cu K or Ta L<sub>3</sub> edge
  - Backlighter:  $4 \times 10^{18}$  eV/eV at 10 keV
  - Spectrometer solid angle  $10^{-6}$  sr
  - 10% detector efficiency
  - 30% transmission through target
  - $\rightarrow 10^6$  counts/eV
  - Note: spectrometer dispersion is about 50 eV/mm for detector perpendicular to DIM axis or 11 eV/mm for detector surface along axis (von Hamos)

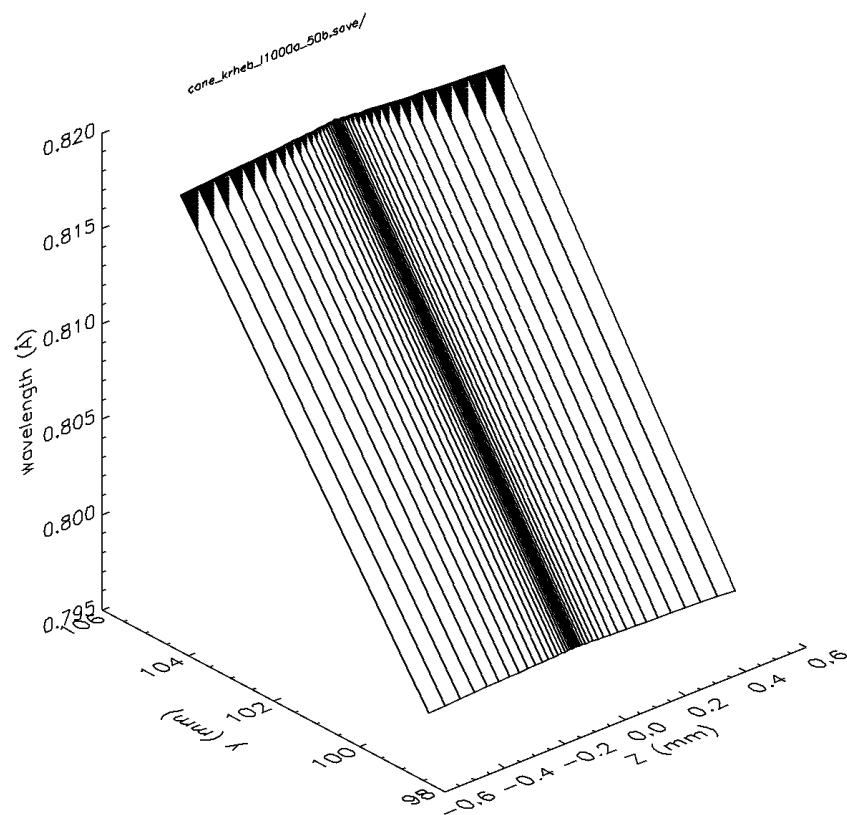
# We need a silicon or germanium cylindrical crystal to continue lab evaluations

Jim Emig provided us with KAP and mica crystals, but the spatial-spectral images are poor, and it is hard to find a single sagittal focus. We work in 4<sup>th</sup> and 3<sup>rd</sup> orders with these crystals, whereas we would have first order reflection with Si or Ge (111), and probably much better quality images.

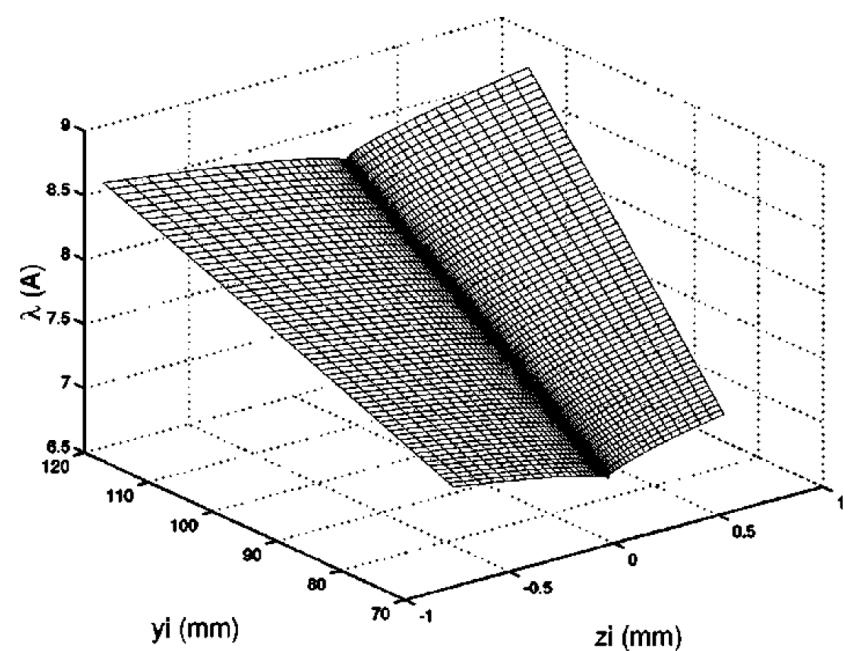


# Our conical crystal analysis code predictions are similar to those of Martinolli et al. RSI (2004)

PPPL 0.8 Å, Kr He $\beta$



Martinolli, 8 Å



We have looked at concepts for a dual von Hamos spectrometer for time integrated and time resolved spectra

