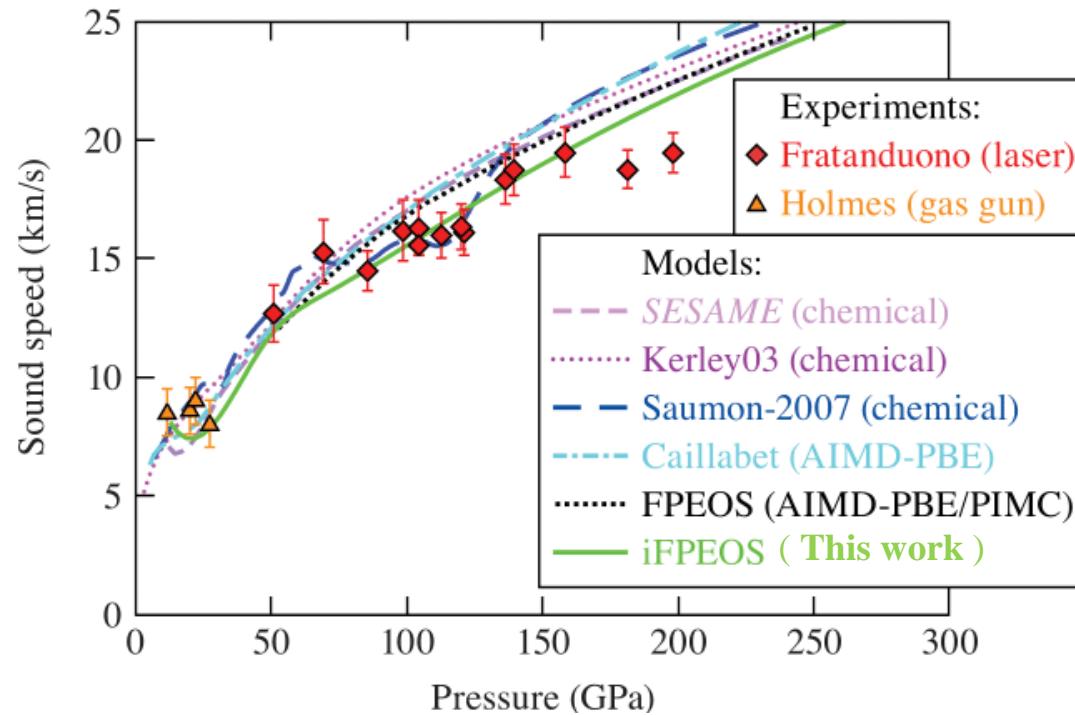


# Improved first-principles equation-of-state table of deuterium for high-energy density science applications



Deyan I. Mihaylov  
University of Rochester  
Laboratory for Laser Energetics

APS Division of Plasma Physics  
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# Collaborators

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**V. V. Karasiev, S. X. Hu, J. R. Rygg, V. N. Goncharov, and G. W. Collins**

**University of Rochester  
Laboratory for Laser Energetics**

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# An improved first-principles equation-of-state (iFPEOS\*) table of deuterium has been constructed using DFT calculations with thermal meta-GGA XC functional (T-SCAN-L) and NQEs<sup>UR</sup> LLE

- We have applied MD driven by DFT using newly developed, *finite-temperature*, meta-GGA exchange-correlation functional T-SCAN-L\*\* for consistent and accurate treatment of temperature effects across all conditions.
- Comparing iFPEOS to other EOS models, we conclude that iFPEOS does provide a better agreement with latest experimental measurements of properties such as the principal Hugoniot and sound speed for pressures up to  $\sim 200$  GPa and temperatures up to  $\sim 60\,000$  K.

Even though we obtain better agreement with experiment at  $P < 200$  GPa, the discrepancy between theory and experiment in the high- $P/T$  regime is confirmed by iFPEOS.

EOS: Equation of State

MD: Molecular Dynamics

DFT: Density Functional Theory

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NQEs: Nuclear Quantum Effects

\*D. I. Mihaylov, V. V. Karasiev, S. X. Hu, J. R. Rygg, V. N. Goncharov, and G. W. Collins, Phys. Rev. B 104, 144104 (2021).

\*\*V. V. Karasiev, D. I. Mihaylov, and S. X. Hu, “Meta-gga exchange-correlation free-energy density functional to achieve unprecedented accuracy for warm-dense-matter simulations” (2021), submitted to Phys. Rev. Lett.

# iFPEOS was motivated by the need for an accurate EOS table for D<sub>2</sub>/DT and recent success of new developments in finite-T DFT

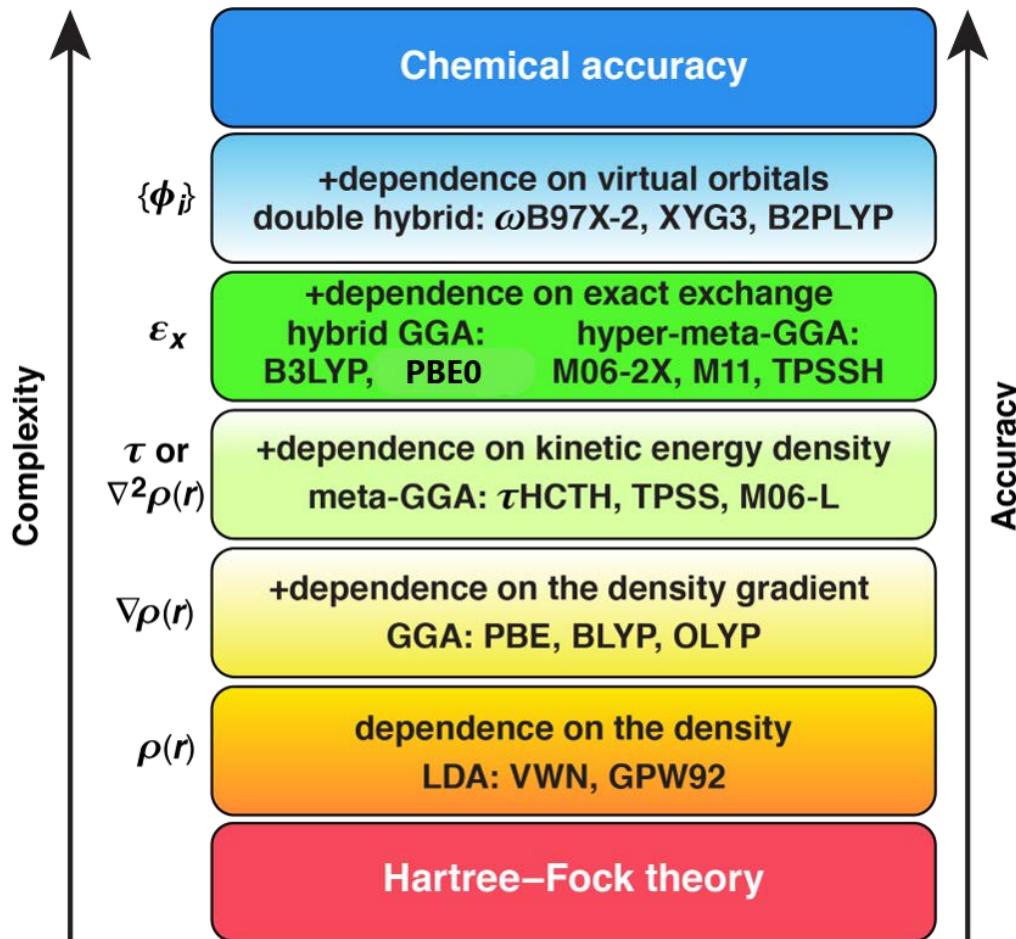


- Understanding EOS of D<sub>2</sub>/DT/H<sub>2</sub> under extreme conditions is still challenging to both theory and experiment, which is evidenced by a systematic disagreement between latest experimental measurements of principal and reshock Hugoniot and sound speed and various EOS models in the high-P/T regime.
- Recently, it was shown that DFT+MD using the SCAN-L + rVV10 XC functional is remarkably successful, and much more accurate than PBE, in predicting the conditions for the dissociation of molecular to atomic fluid in dense deuterium/hydrogen\*.
- Additionally, iFPEOS was motivated by the development of new finite-T version of the SCAN-L functional (T-SCAN-L) and the need to take into account nuclear quantum effects (NQEs).

\* J. Hinz, V. V. Karasiev, S. X. Hu, M. Zaghou, D. Mejía-Rodríguez, S. B. Trickey, and L. Calderín, Phys. Rev. Res. 2, 032065(R) (2020).

iFPEOS is based on a recently developed advanced, thermal exchange-correlation functional T-SCAN-L, which is at the meta-GGA level of DFT.

Jacob's ladder of zero-temperature XC functionals:



Finite-temperature XC density functionals at corresponding level of theory:

- ← KDT0<sup>†</sup> : finite- $T$  extension to PBE0
- ← T-SCAN-L †† : finite- $T$  extension to SCAN-L, the de-orbitalized version of SCAN
- ← Finite-temperature GGA (KDT16)\*
- ← Finite-temperature LDA (KS<sup>\*\*</sup>, (corrKS<sup>\*\*</sup>)\*)

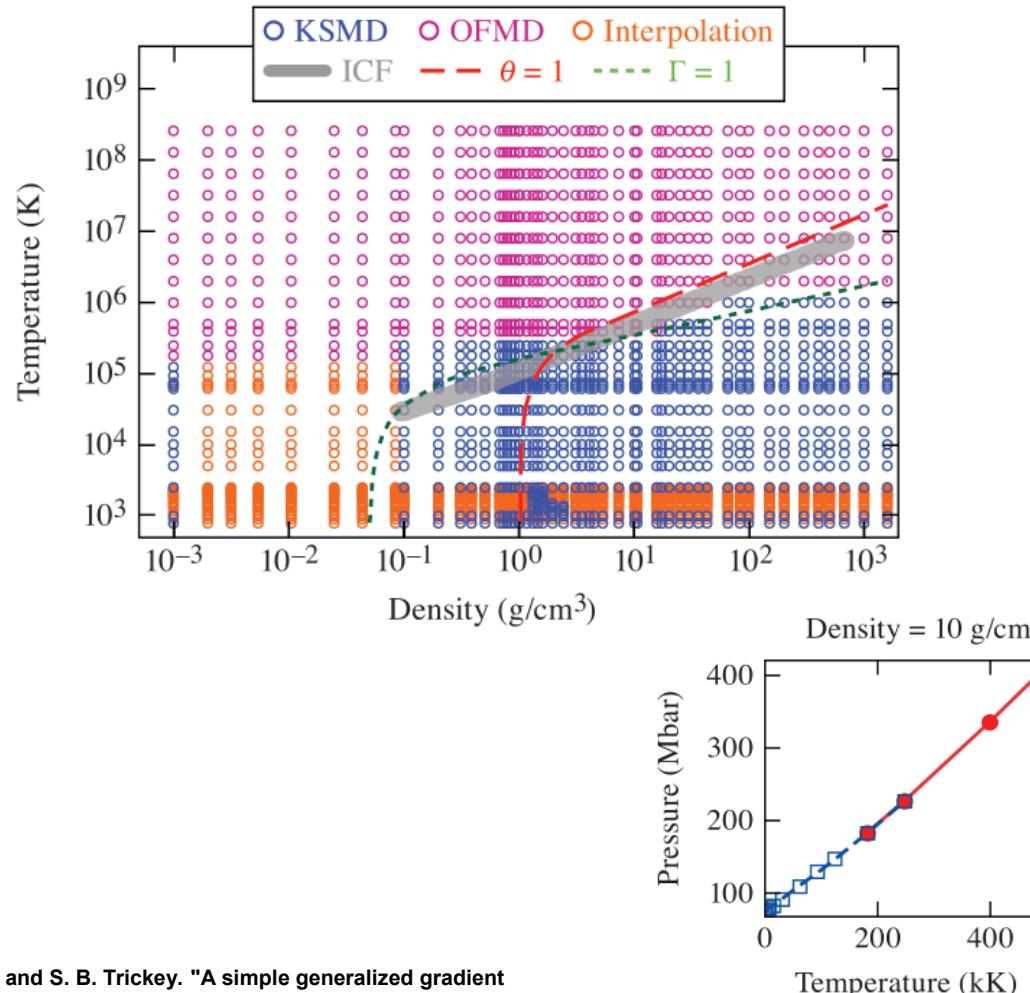
\* V. V. Karasiev, J. W. Duffy, and S. B. Trickey, Phys. Rev. Lett. **120**, 076401 (2018).

\*\* V. V. Karasiev et al., Phys. Rev. Lett. **112**, 076403 (2014).

† D. I. Mihaylov, V. V. Karasiev, and S. X. Hu, Physical Review B **101** (24), 245141.

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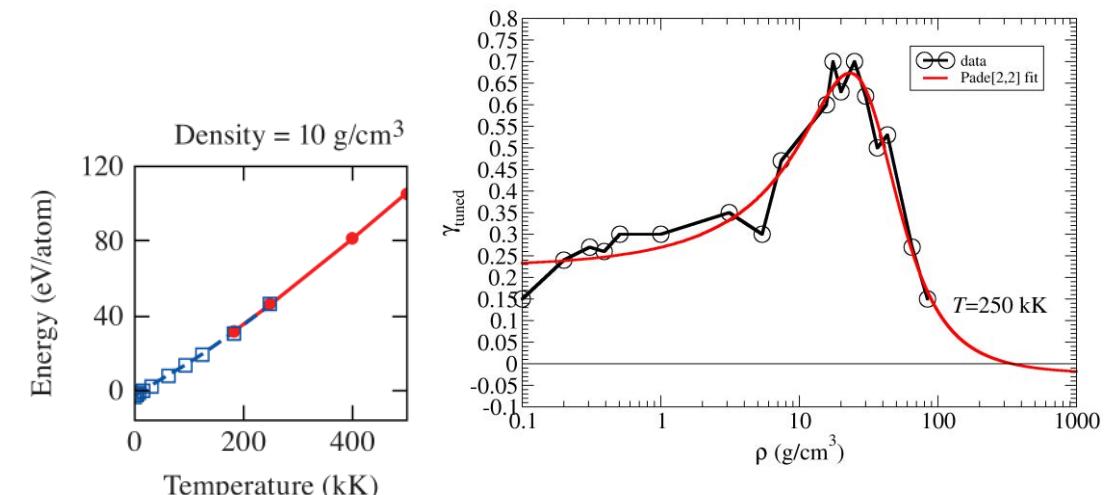
# We use orbital free DFT with T-SCAN-L for XC to cover temperatures up to 256 MK



Orbital-free (OF) calculations are carried out with newly-developed, orbital-free, free-energy, non-interacting, tunable density functional LKT $\gamma$ TF (unpublished).

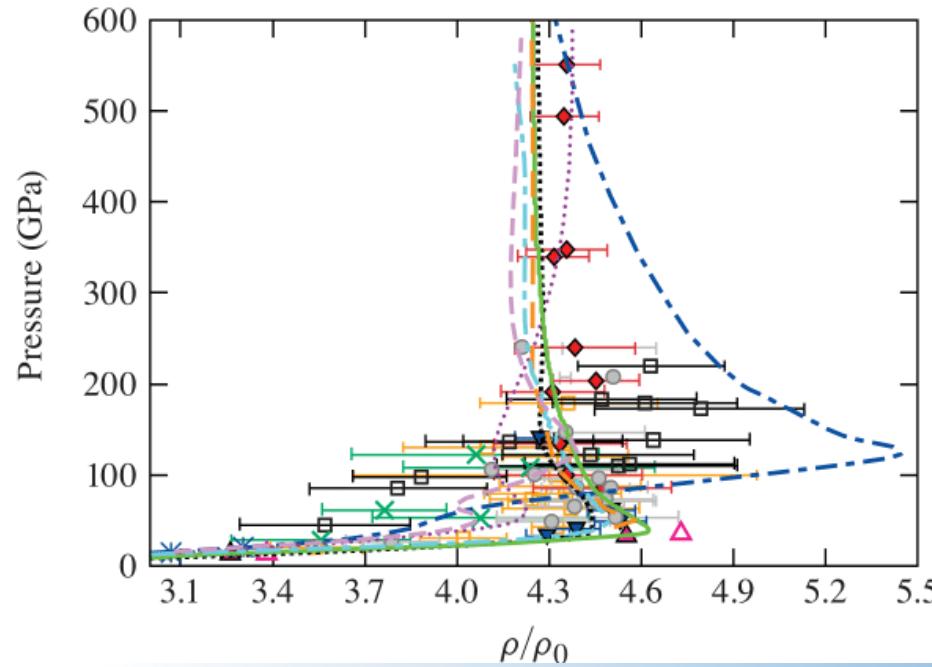
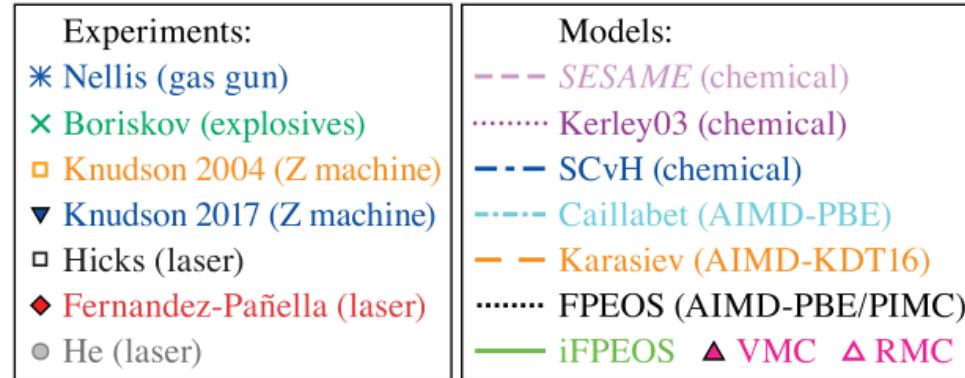
$$F_s^{LKT\Gamma TF}[\mathbf{n}, T] = \gamma F_s^{LKT TF}[\mathbf{n}, T] + (1 - \gamma) F_s^{TF}[\mathbf{n}, T]$$

LKT $\gamma$ TF is a one-parameter convex combination of LKT $\gamma$ \* (Luo, Karasiev, Trickey Free-energy) and TF (Thomas-Fermi).  $\gamma$  is a free parameter and is tuned based on a reference Kohn-Sham calculation.

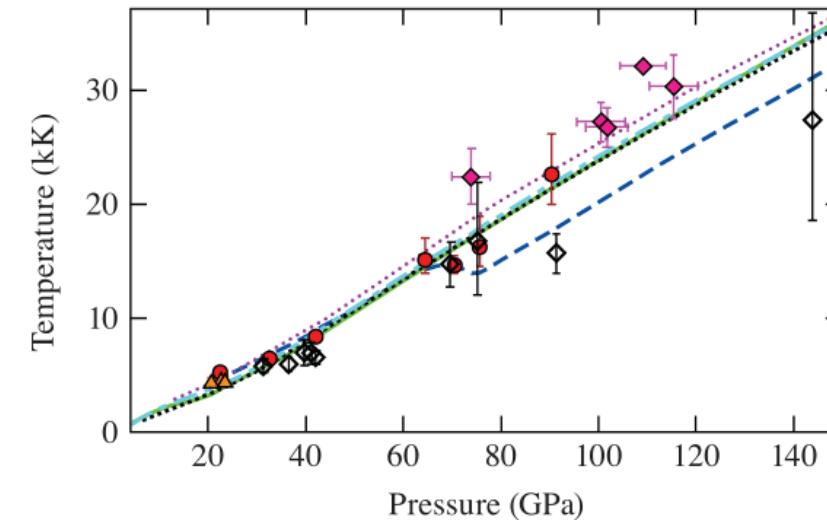
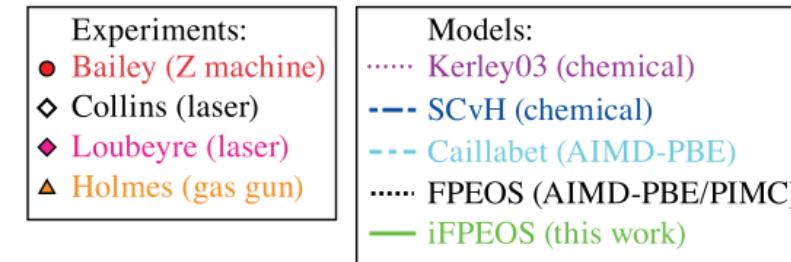


\* K. Luo, V. V. Karasiev, and S. B. Trickey. "A simple generalized gradient approximation for the noninteracting kinetic energy density functional." Phys. Rev. B 98 (2018):

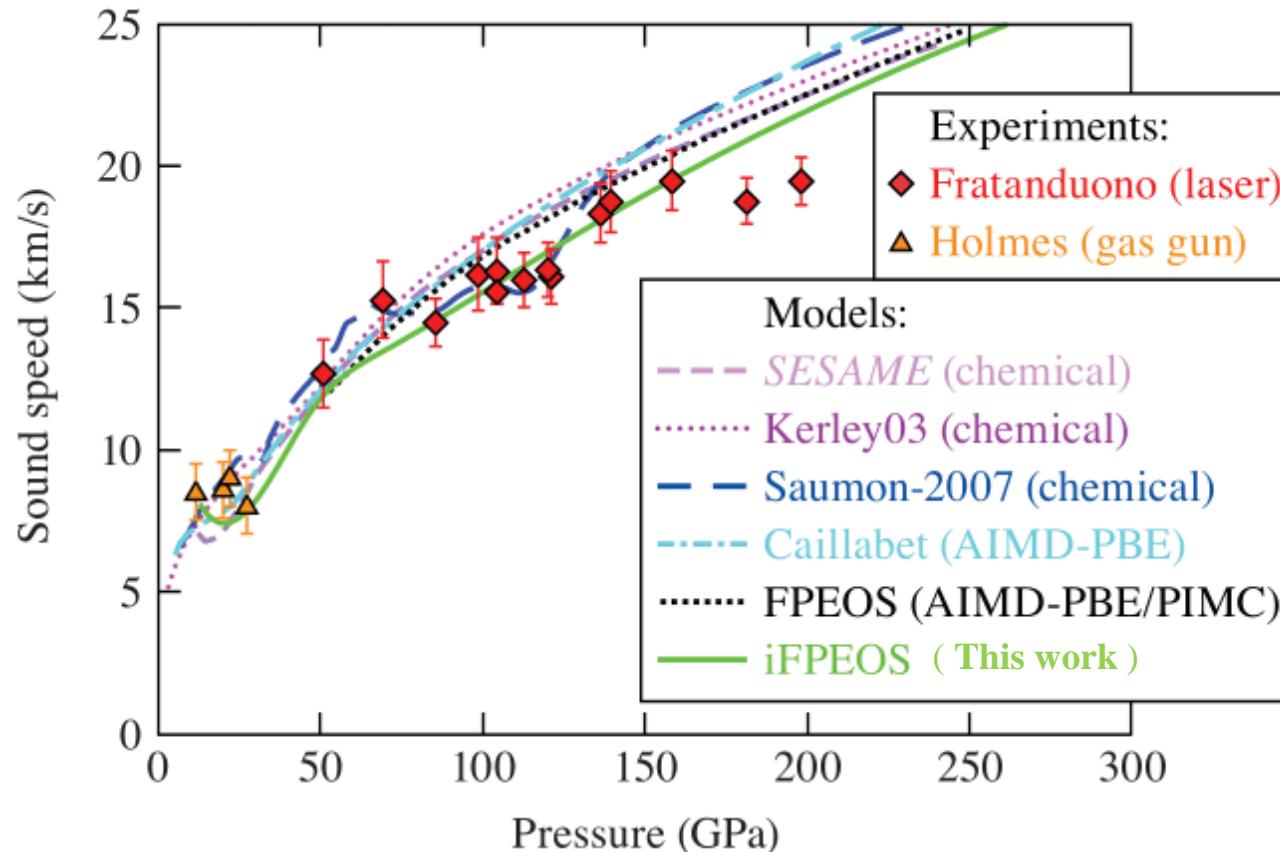
# iFPEOS predicts a higher compressibility, but in the high-pressure regime, it is in agreement with PBE-based models which predict smaller compressibility compared to experiment.



$$E - E_0 = \frac{1}{2} (P + P_0) \left( \frac{1}{\rho_0} - \frac{1}{\rho} \right)$$



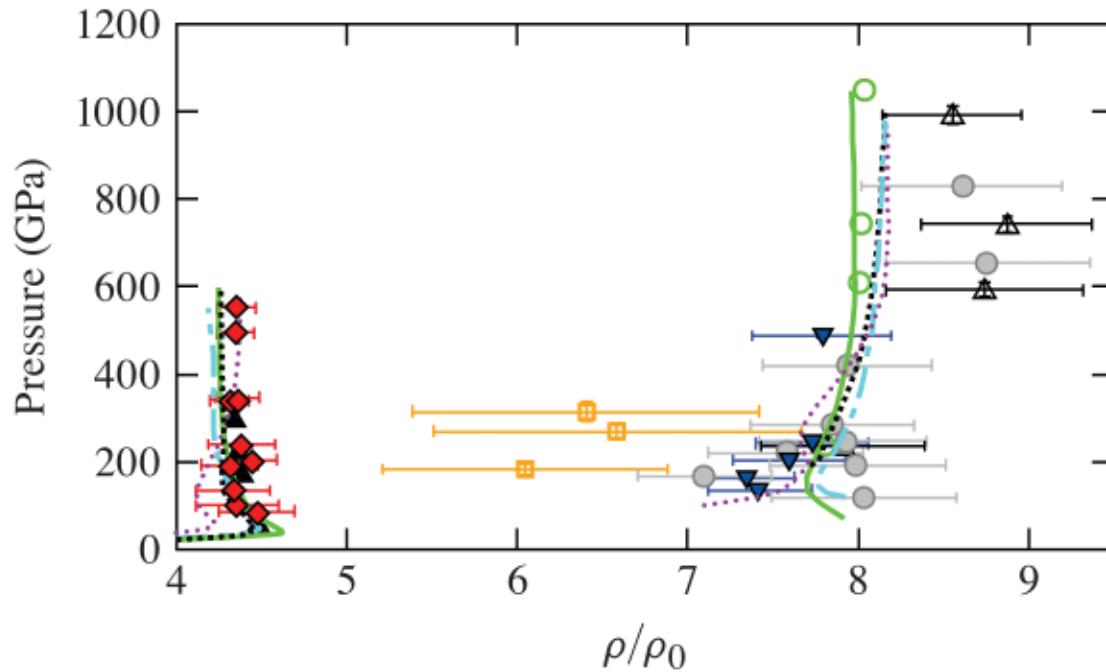
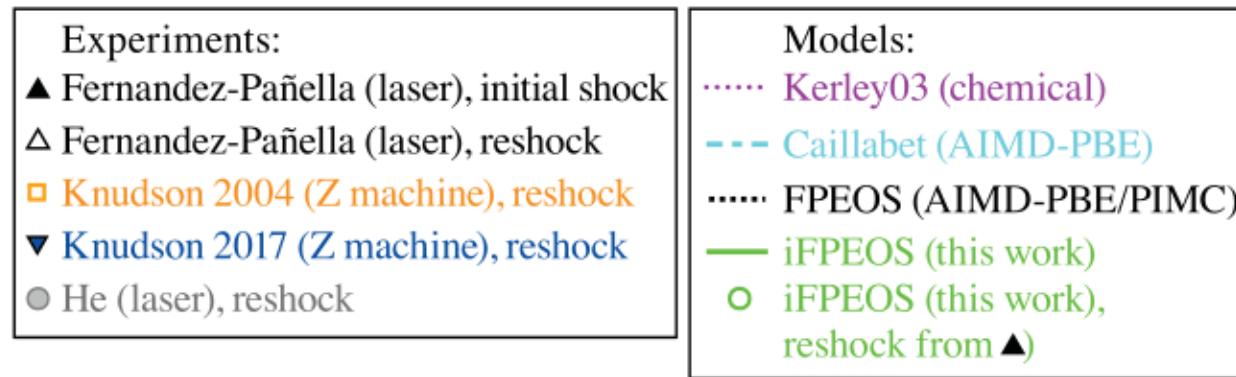
iFPEOS-predicted sound speed shows improved agreement with experiment in the 80-150 GPa pressure regime – corresponding to 15 – 40 kK, where XC thermal effects are most important.



Eulerian sound speed:

$$c = \sqrt{\left(\frac{\partial p}{\partial \rho}\right)_s}.$$

# In the low-pressure regime iFPEOS agrees with other models and latest experimental measurements of double-shocked deuterium, but in the high-pressure regime iFPEOS predicts a significantly softer reshock Hugoniot.



$$E - E_0 = \frac{1}{2} (P + P_0) \left( \frac{1}{\rho_0} - \frac{1}{\rho} \right)$$

$$\rho = \frac{\rho_0(u_s - u_{p0})}{(u_s - u_p)}$$

$$P = P_0 + \rho_0(u_s - u_{p0})(u_p - u_p)$$

- Reshock states (green circles) were determined by Impedance Matching (IM) with  $\alpha$ -quartz\*.
- iFPEOS reshock Hugoniot (green curve) is launched off of iFPEOS principal Hugoniot.

\* Supplemental Material - A. Fernandez-Pañella, M. Millot, D. Fratanduono, M. Desjarlais, S. Hamel, M. Marshall, D. Erskine, P. Sterne, S. Haan, T. Boehly, et al., Physical review letters 122, 255702 (2019).

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