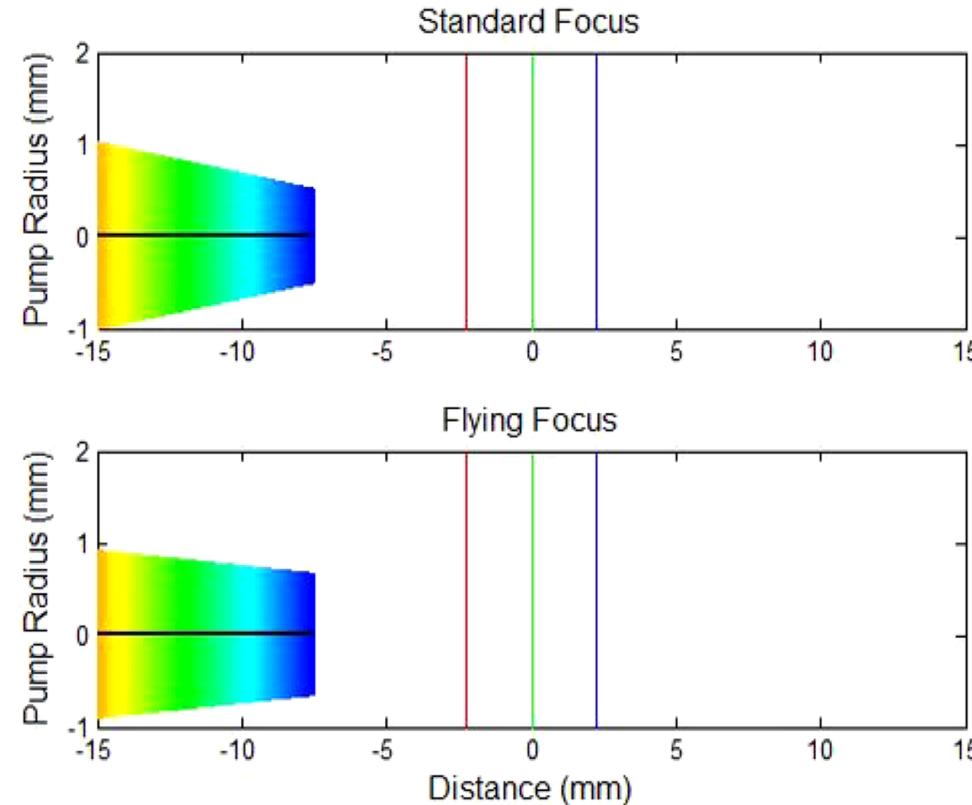


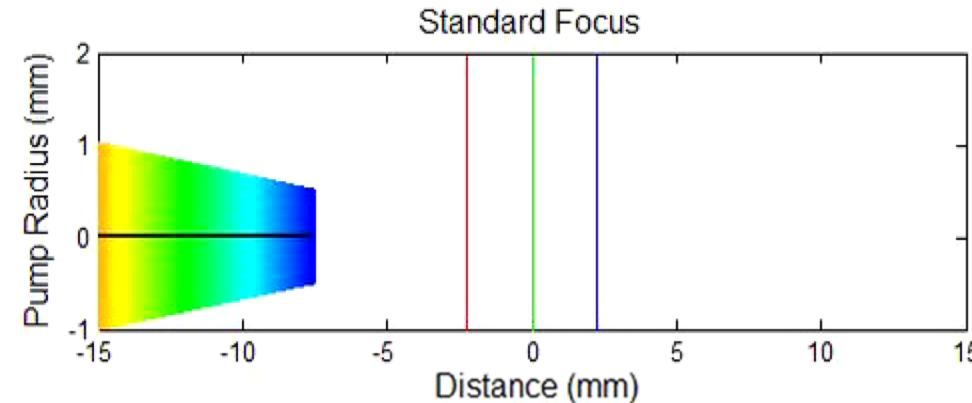
# Frequency Conversion of Laser Pulses Reflected from Ionization Waves of Arbitrary Velocity



**Philip Franke, John P. Palastro, David Turnbull, Dustin H. Froula**  
**University of Rochester**  
**Laboratory for Laser Energetics**

**61<sup>st</sup> APS DPP**  
**Ft. Lauderdale, FL**  
**21-25 October 2019**

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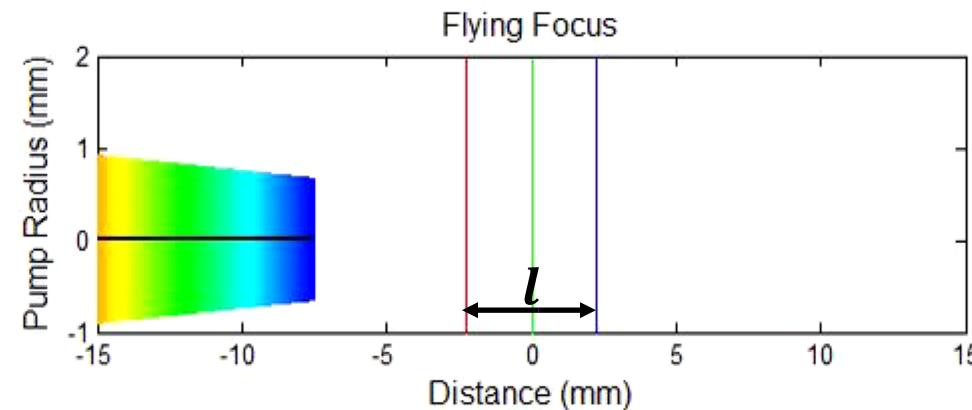
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T07:12 (T. T. Simpson)  
T07:13 (D. W. Ramsey)



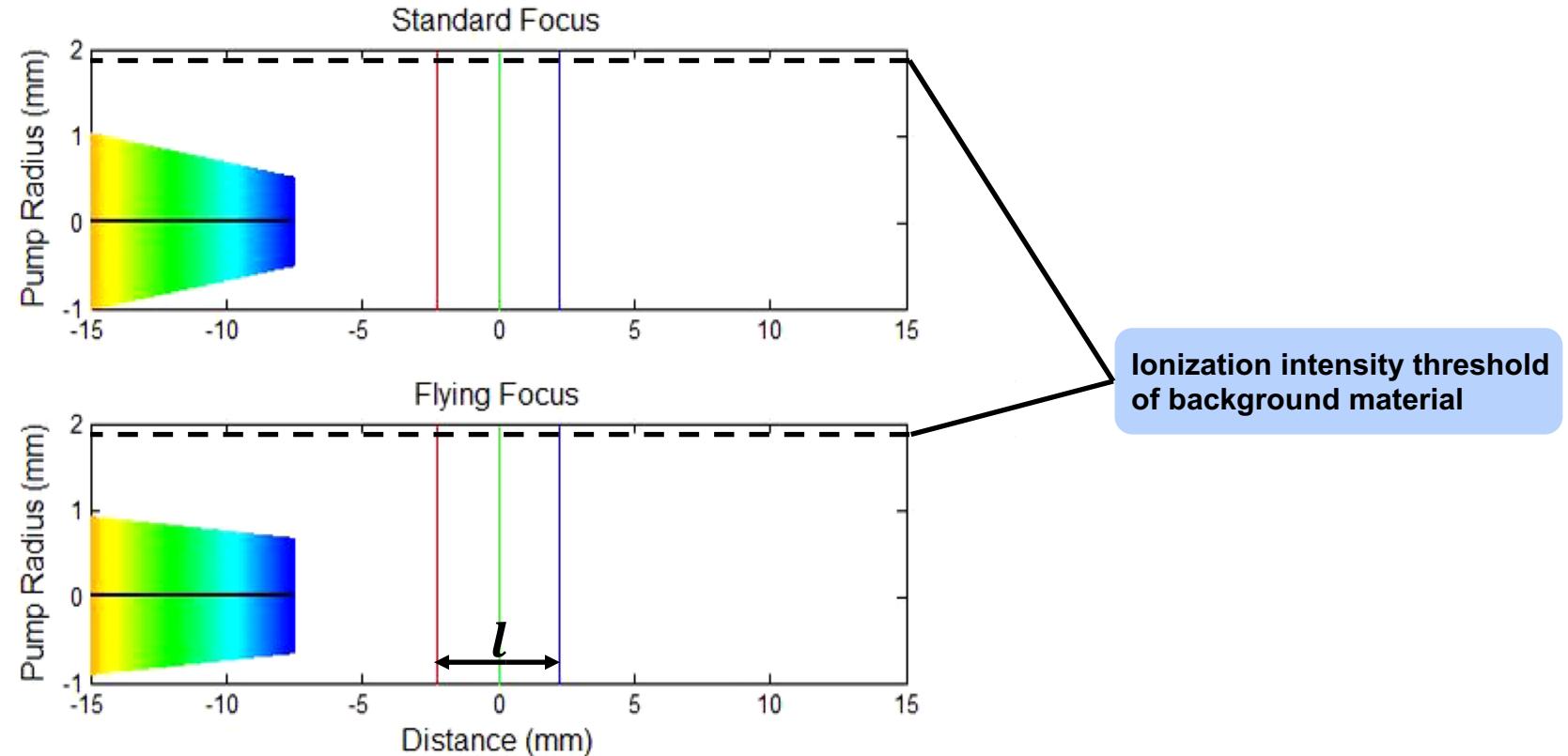
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# Laser pulses reflected from flying focus-driven ionization fronts can undergo extreme frequency upshifts



- High density ionization fronts can be driven over long distances at any velocity with the flying focus
- Reflected pulses can be shifted to high frequencies, while retaining desirable characteristics such as spatial coherence, low divergence, and ultrashort duration
- Output frequency is easily tuned over a broad range by changing the front velocity

# Experiments have demonstrated that the flying focus can create predictable and tunable ionization waves of arbitrary velocity (IWAV's)



$$v_{focus}/v_g = \left(1 \pm \frac{\tau v_g}{l}\right)^{-1} = v_{IWAV}/v_g$$

$v_{focus}$ : velocity of flying focus intensity peak

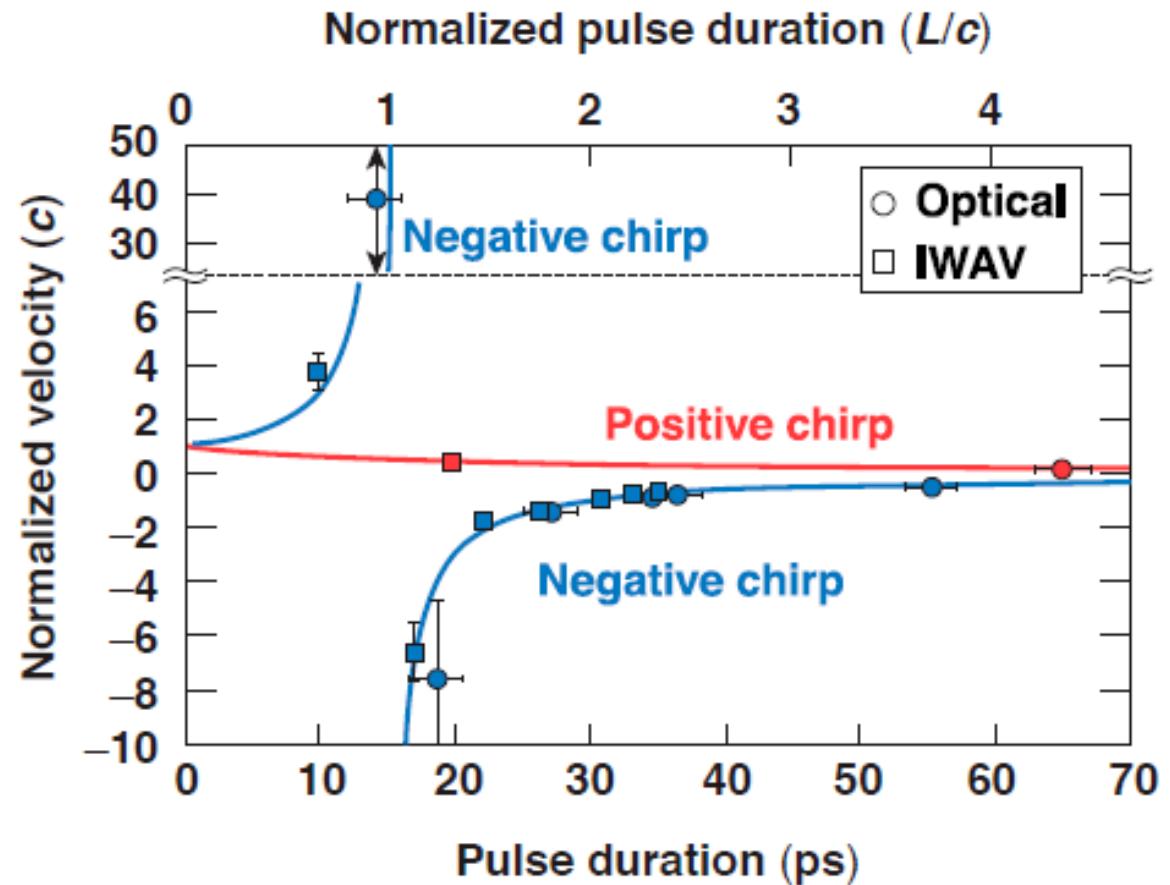
$v_g$ : laser group velocity

$\tau$ : pulse duration

$l$ : longitudinal focal shift across bandwidth

$\pm$ : sign of chirp

$v_{IWAV}$ : IWAV velocity



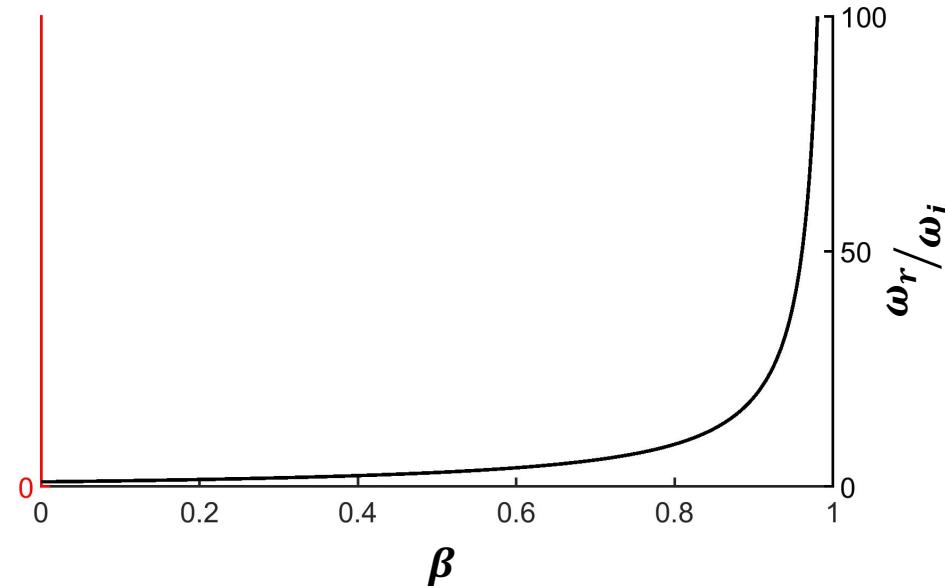
IWAV velocity is decoupled from the laser group velocity

- \* D. Turnbull et al., Phys. Rev. Lett. 120, 225001 (2018).
- \*\* D. Froula et al., Nature Photonics 12, 262+ (2018).
- † D. Froula et al., Phys. Plasmas 26, 032109 (2019).
- ‡ J. P. Palastro et al., Phys. Rev. A 97, 033835 (2018).
- ¶ P. Franke et al., Opt. Express 27, 31978–31988 (2019).

# High density I WAV's can reflect a counter-propagating laser pulse and cause extreme frequency up-shifts and pulse compression

- Frequency shift:

$$\frac{\omega_r}{\omega_i} = \frac{1 + \beta}{1 - \beta}$$



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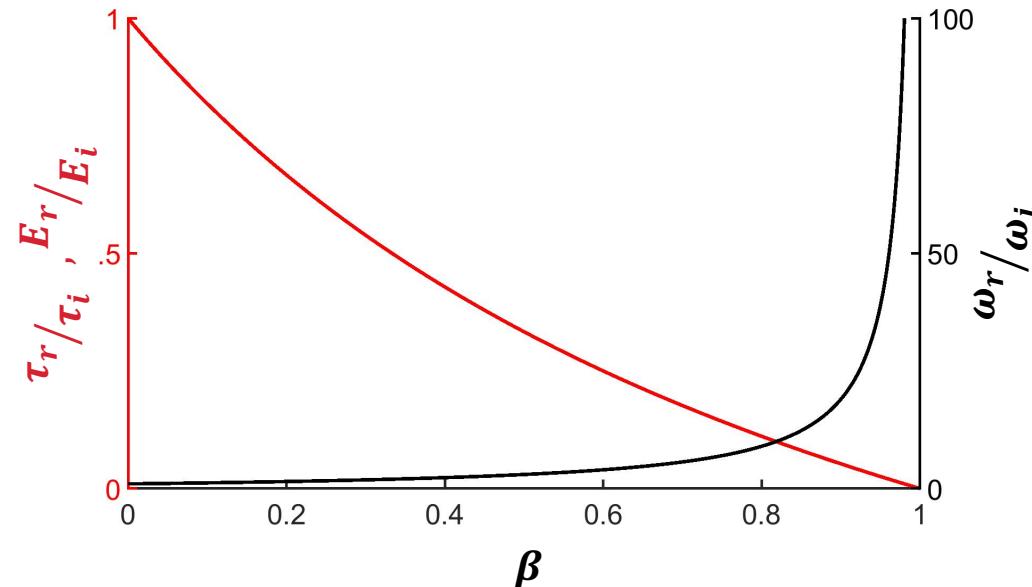
$$\frac{\omega_r}{\omega_i} = \frac{1 + \beta}{1 - \beta}$$

- Pulse duration:

$$\frac{\tau_r}{\tau_i} = \frac{\omega_i}{\omega_r}$$

- Pulse energy:

$$\frac{E_r}{E_i} = \frac{\omega_i}{\omega_r}$$



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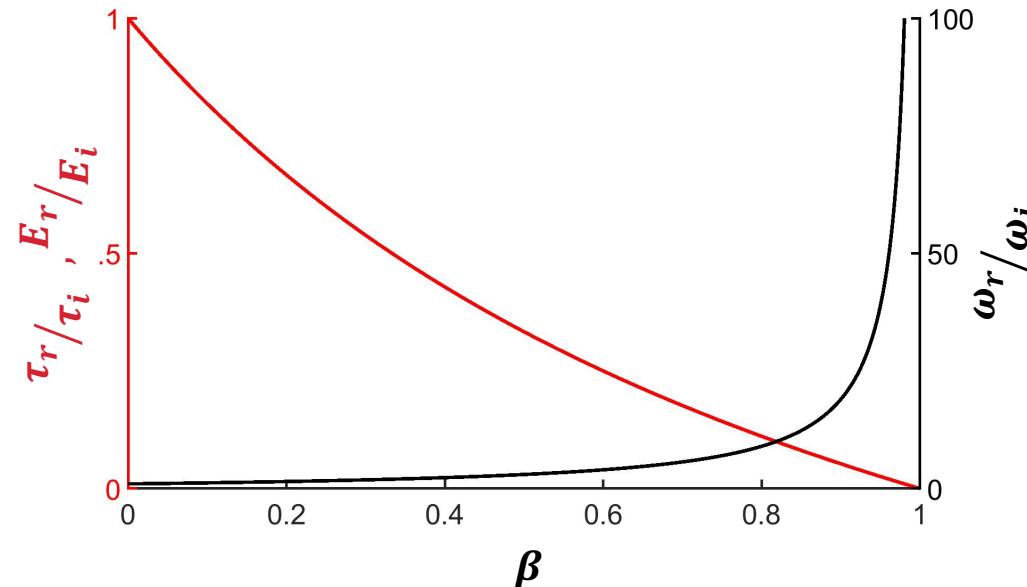
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- Full reflection condition:

$$\frac{\omega_p}{\omega_i} > \left[ \frac{1 + \beta}{1 - \beta} \right]^{1/2}$$

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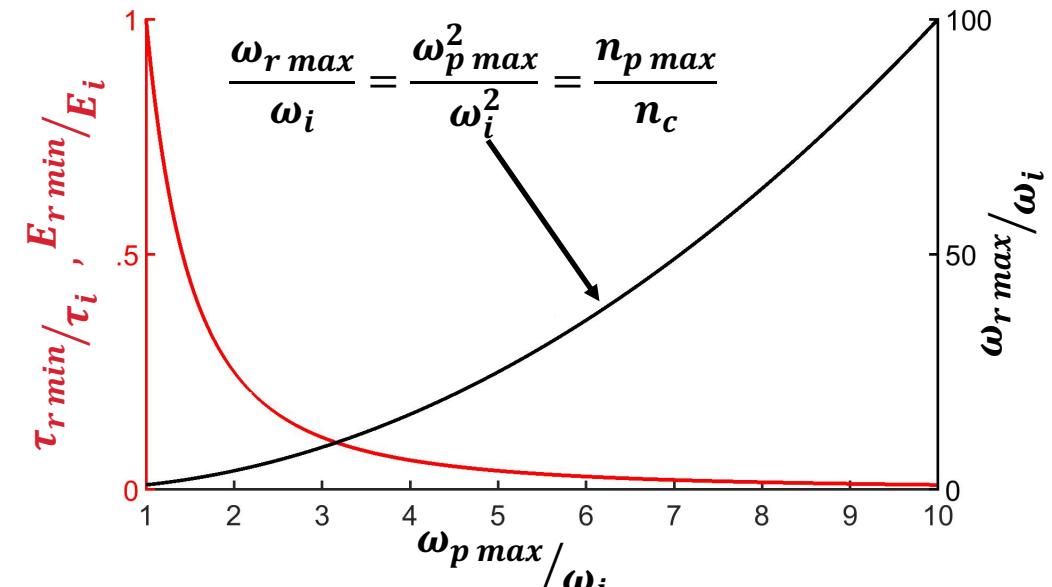
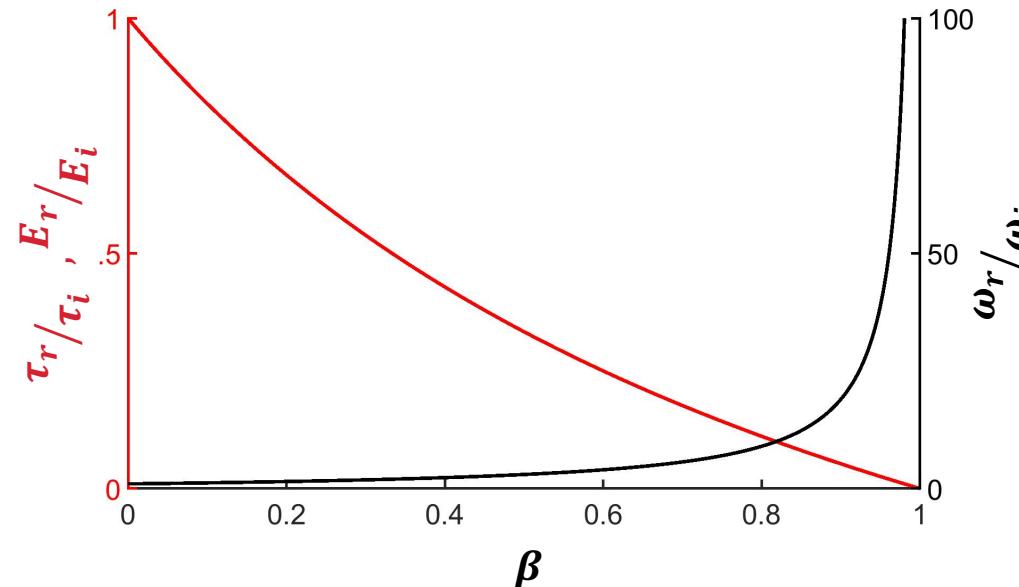
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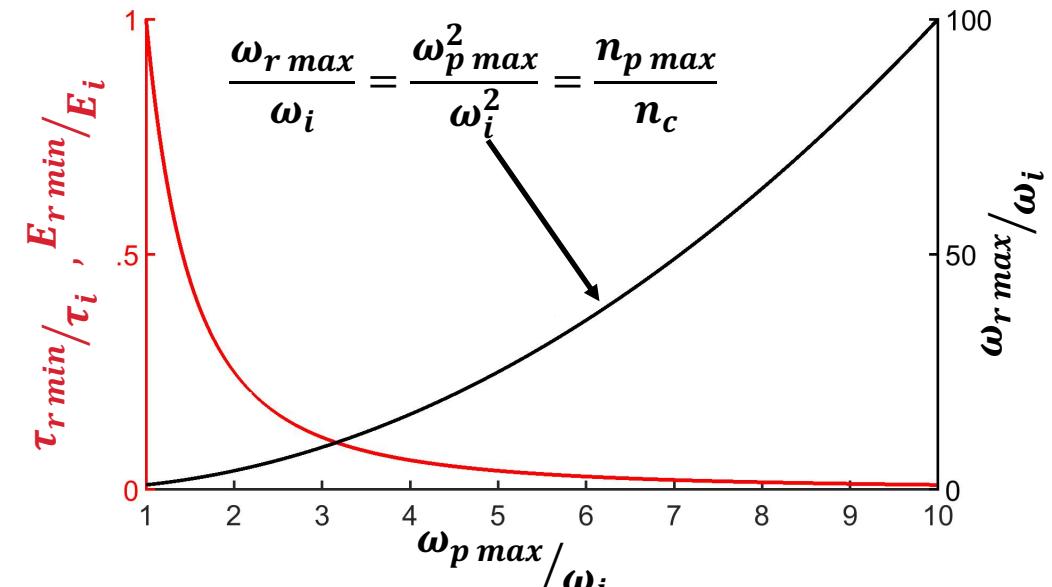
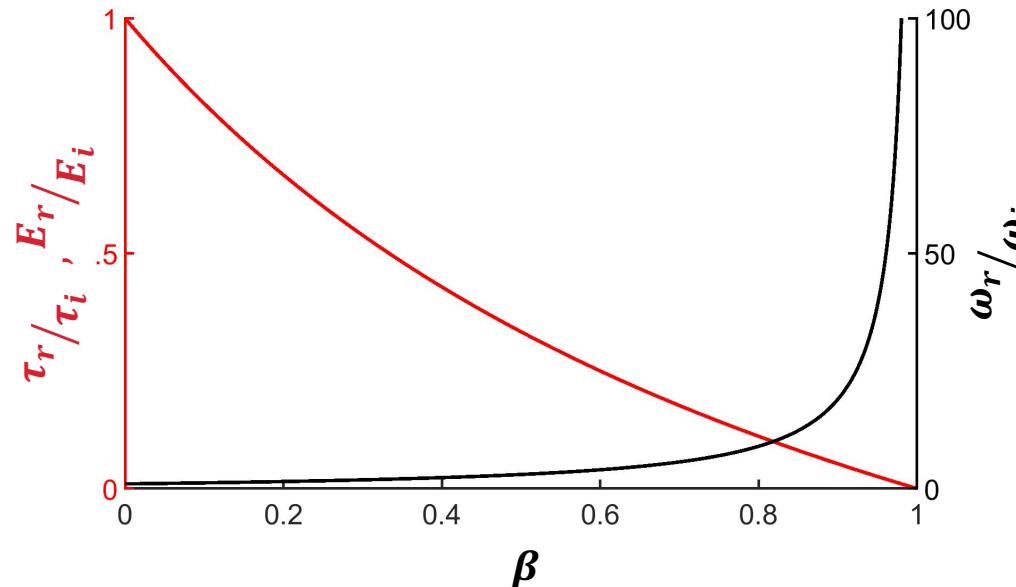
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$$\omega_{r max} = \frac{\omega_{p max}^2}{\omega_i}$$

Increase Maximum Density

Decrease Initial Frequency

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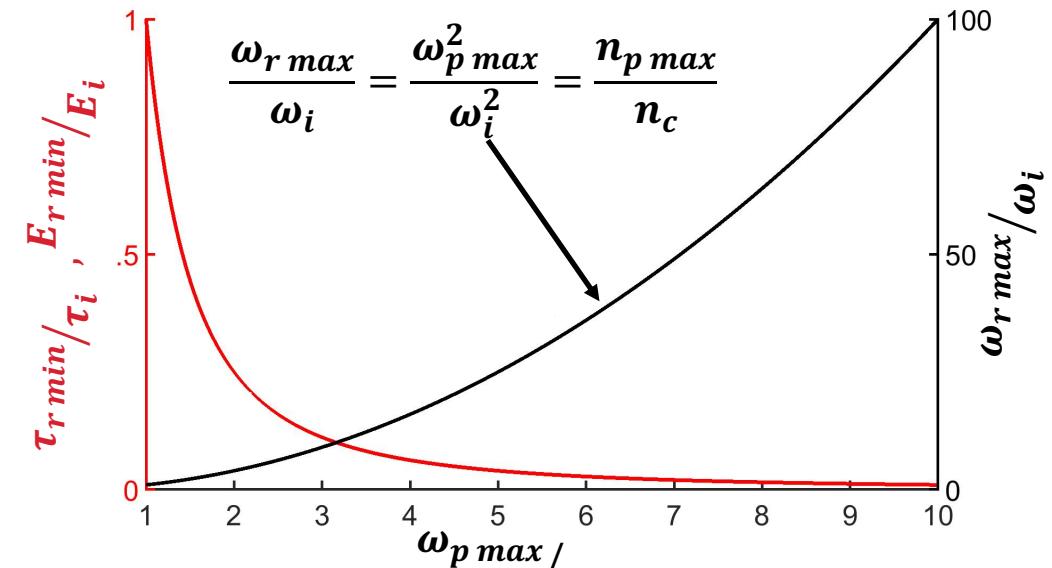
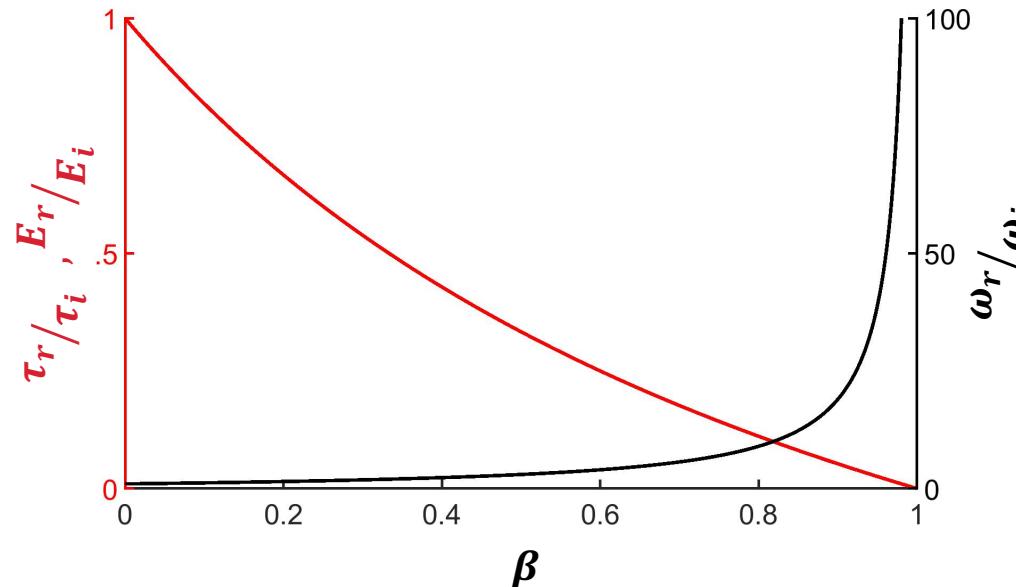
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*Nd: YLF (3ω)*

$$\omega_{r \max} = \frac{\omega_{p \max}^2}{\omega_i} = \frac{\omega_c^2 (351 \text{nm})}{\omega_i (10 \mu\text{m})}$$

*CO<sub>2</sub> (1ω)*

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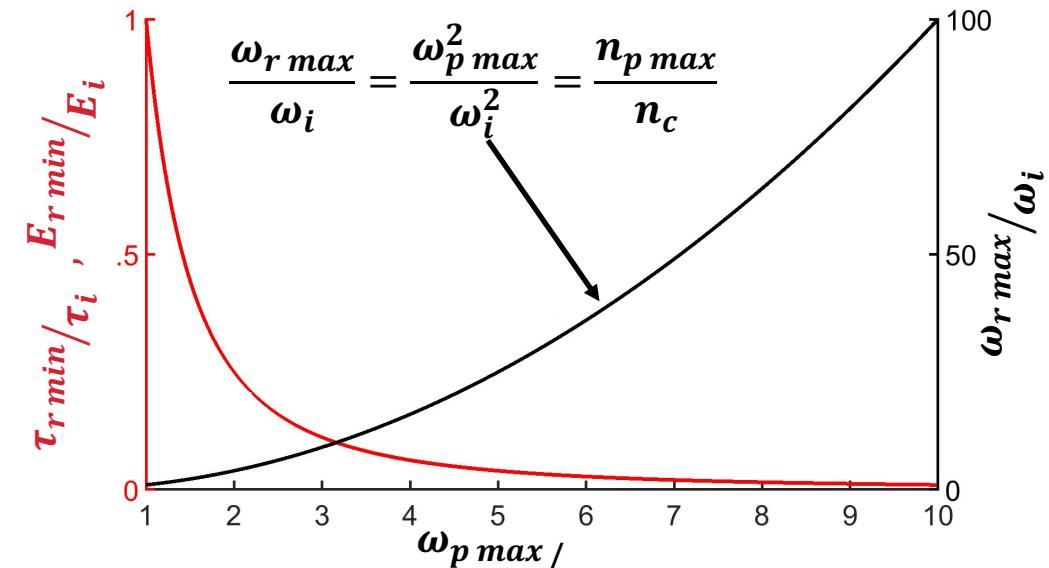
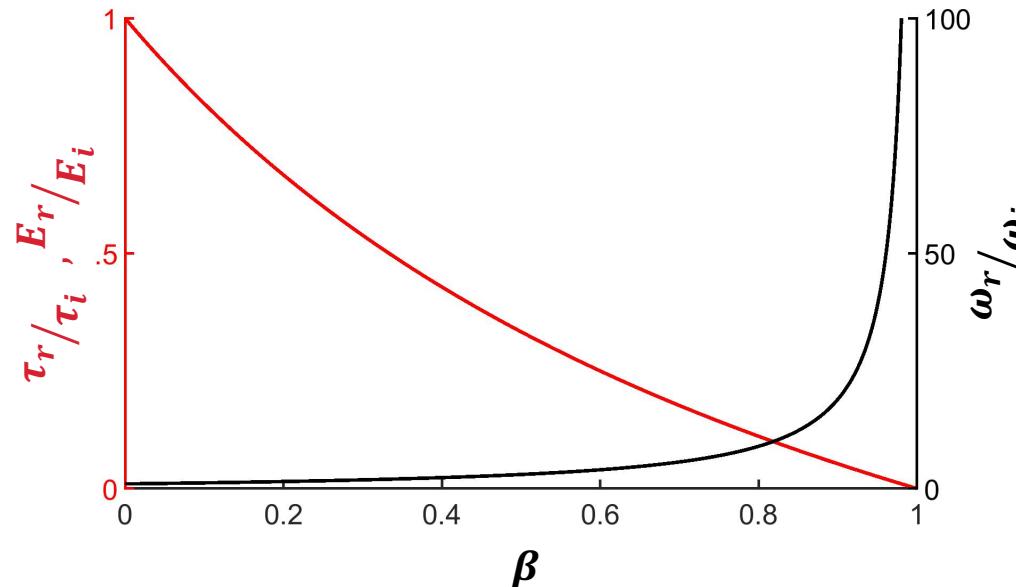
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*CO<sub>2</sub> (1ω)*

# 1D FDTD simulations provide a simple model of laser pulse dynamics in an ideal IAWAV

- **Curl equations + linear current model:**

$$\nabla \times E = -\mu_0 \partial_t H \quad \nabla \times H = -\epsilon_0 \partial_t E + J$$

$$\partial_t J = \epsilon_0 \omega_p^2 E$$

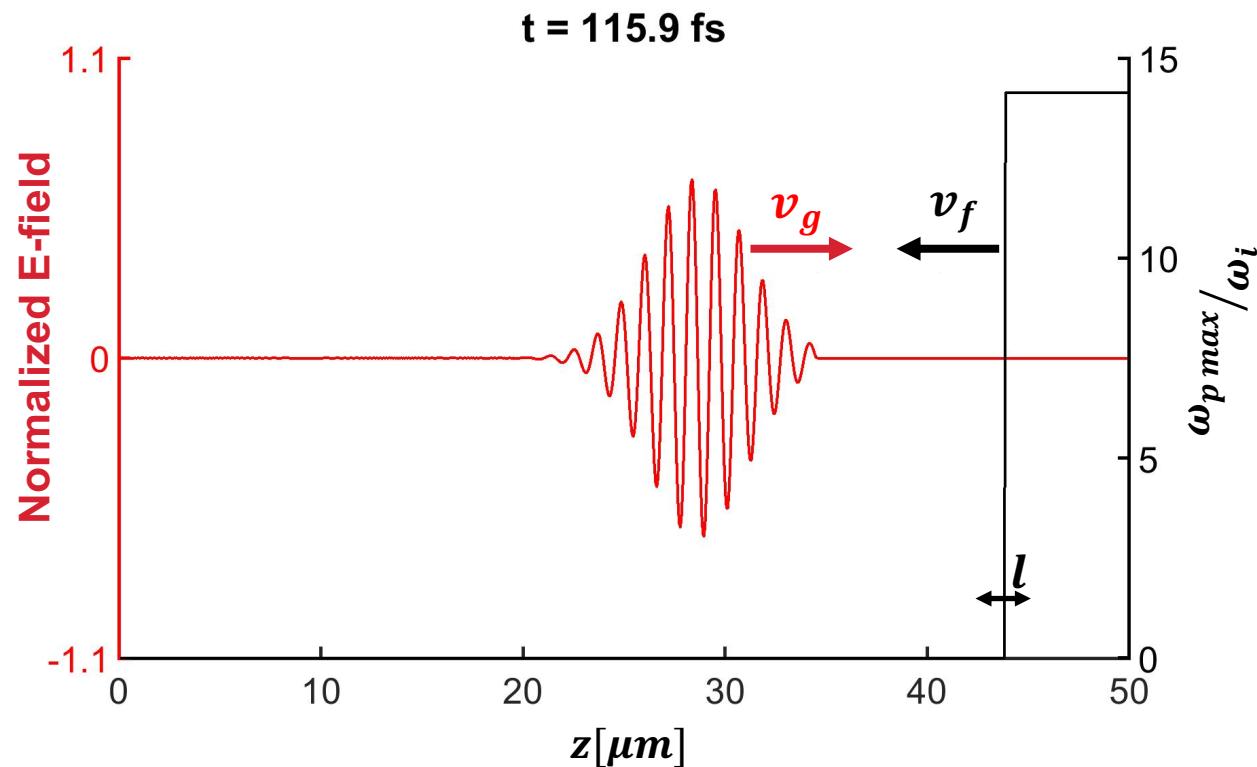
- **Specify density profile:**

$$\omega_p(z,t) = \frac{\omega_{p\max}}{2} \left\{ 1 + \tanh \left[ l^{-1} (z - v_f t) \right] \right\}$$

Vary:  $\omega_{p\max}, l, v_f$

- **Specify (Gaussian) source parameters:**

Vary:  $\lambda_0, \delta\lambda (\tau_{T.L.}), \text{chirp}$



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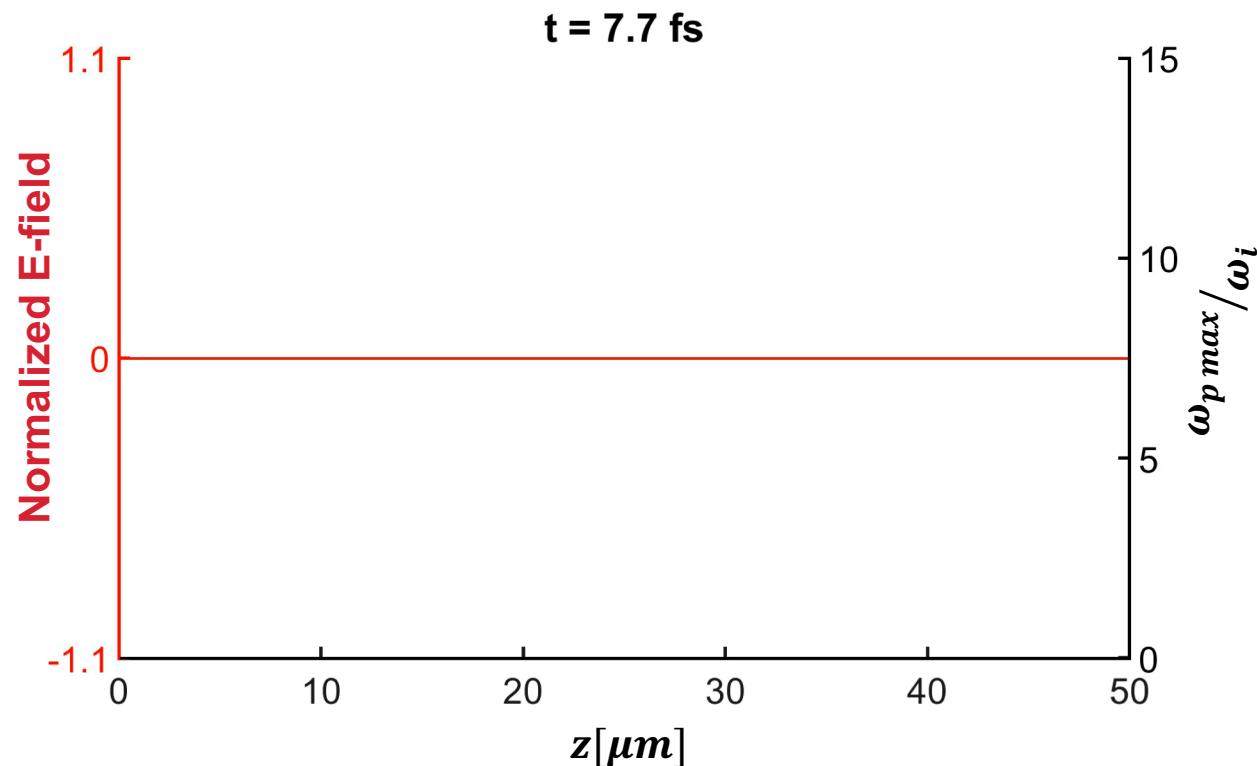
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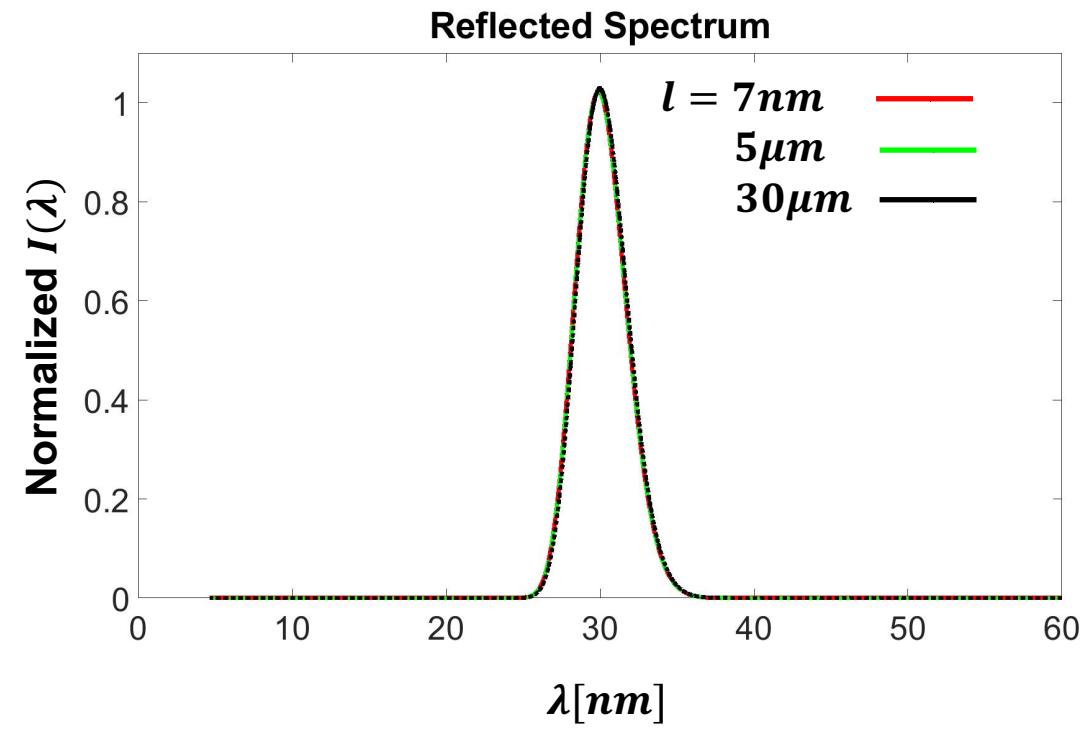
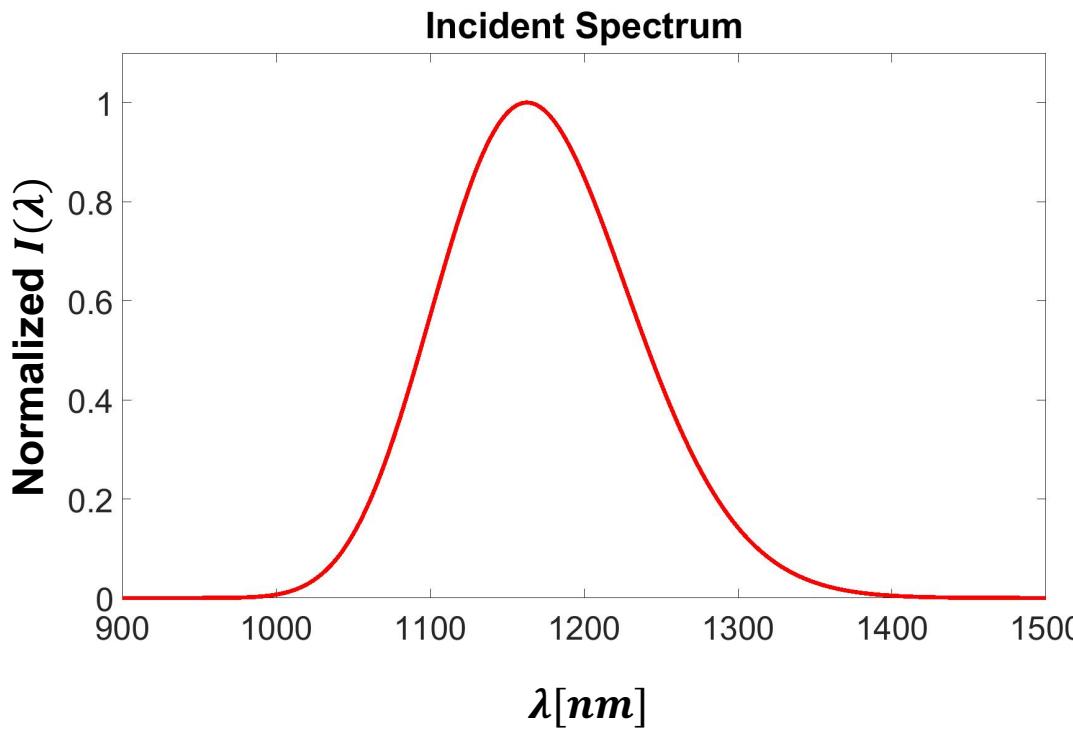
# Reflected spectra and energies are consistent with the simple analytic theory for all ionization front density scale lengths



$$\begin{aligned}\lambda_i &= 1170\text{nm} \\ \delta\lambda_i &= 150\text{nm} \\ \tau_i &= 13\text{fs}\end{aligned}$$

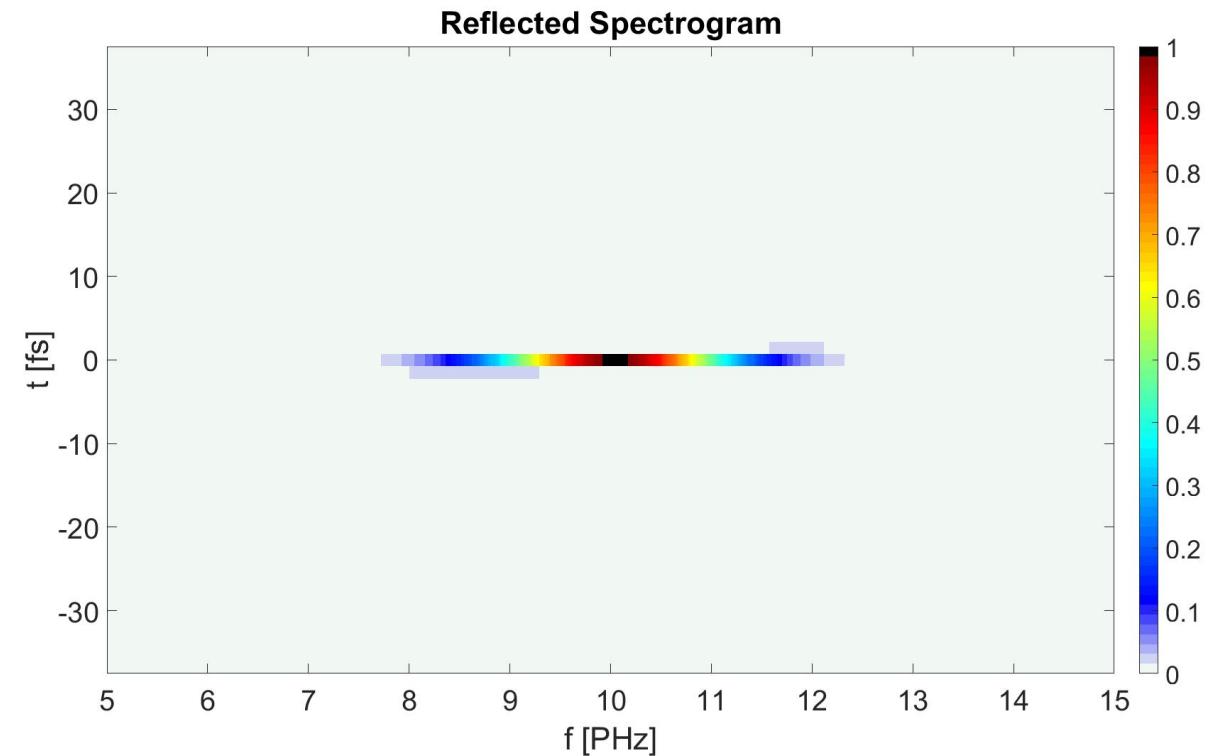
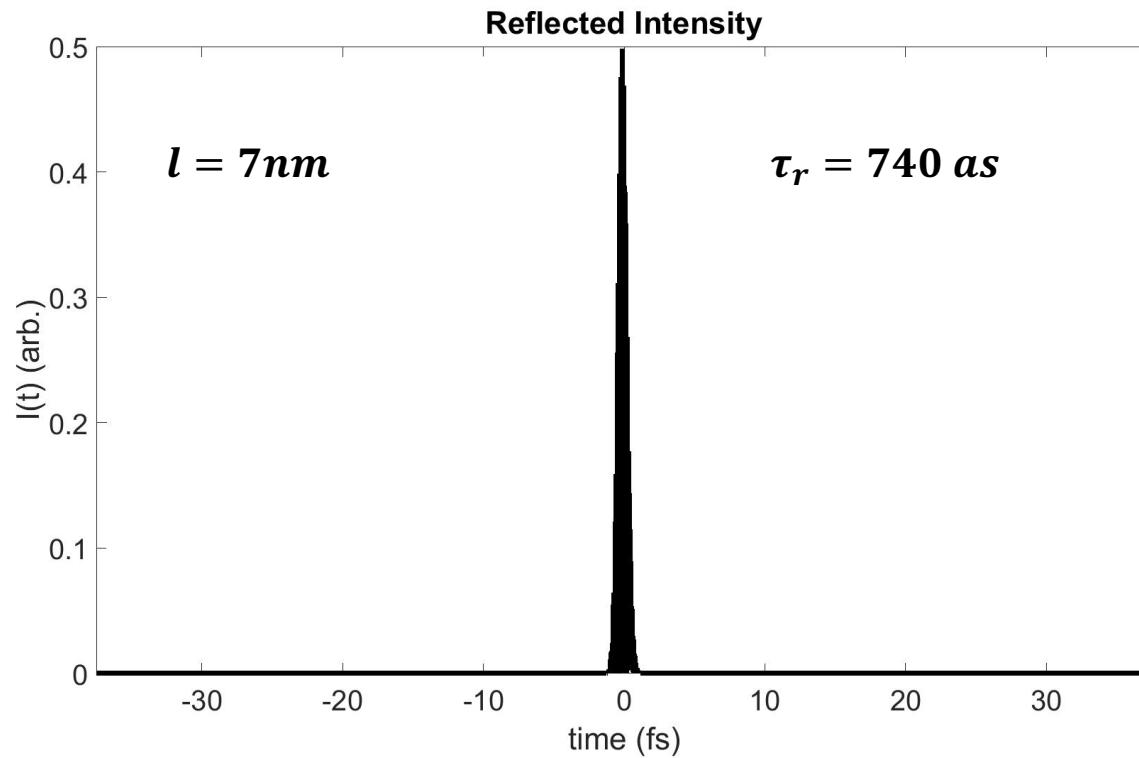
$$\begin{aligned}\beta &= .95 \\ l &= 7\text{nm} - 30\mu\text{m}\end{aligned}$$

$$\begin{aligned}\lambda_r &= \frac{1-\beta}{1+\beta}\lambda_i = 30\text{nm} \\ \delta\lambda_r &= \frac{\lambda_r}{\lambda_i}\delta\lambda_i = 3.8\text{nm}\end{aligned}$$



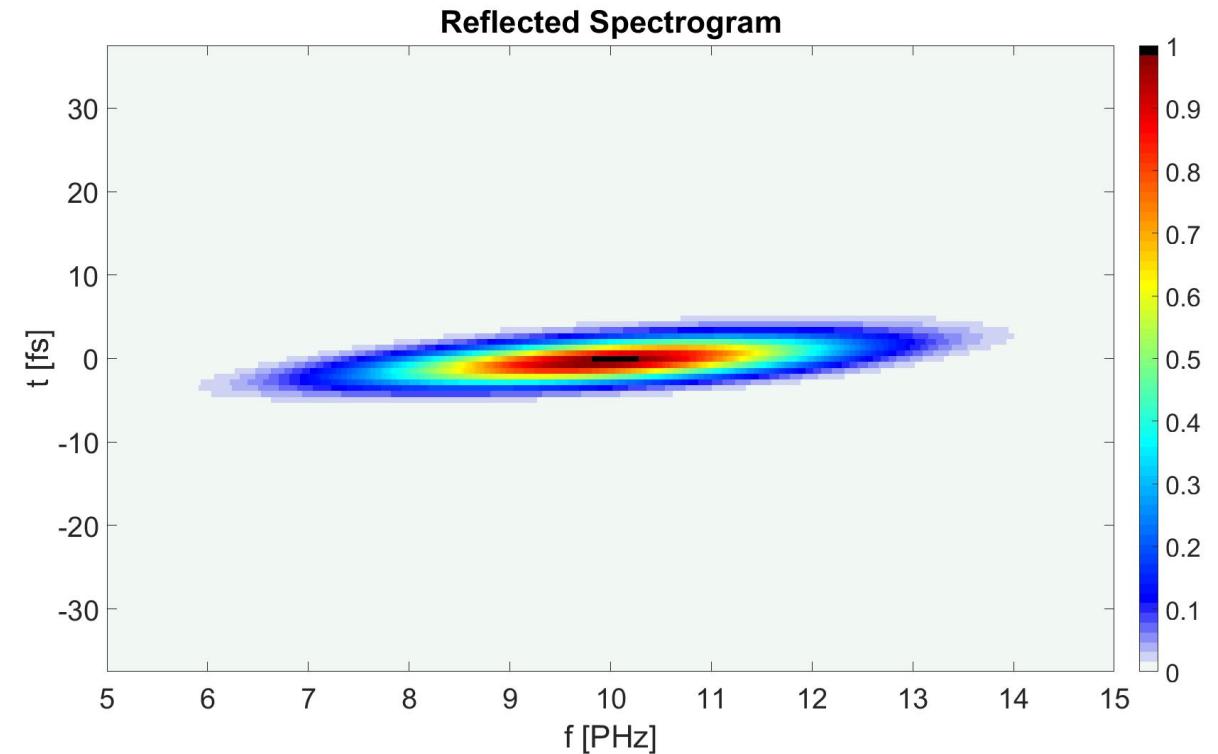
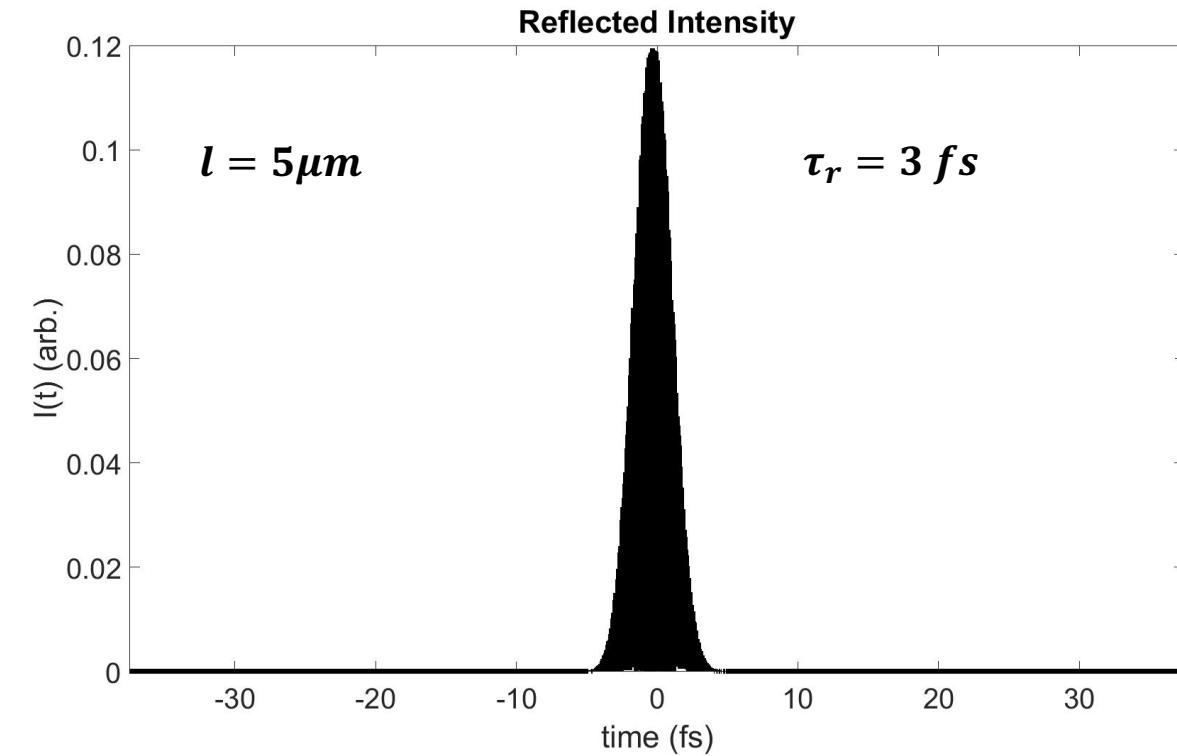
# Reflected pulses remain coherent and ultrashort, but finite scale lengths and bandwidths contribute to temporal broadening

$$\tau_r = \frac{\lambda_r}{\lambda_i} 13 \text{ fs} = 333 \text{ as}$$



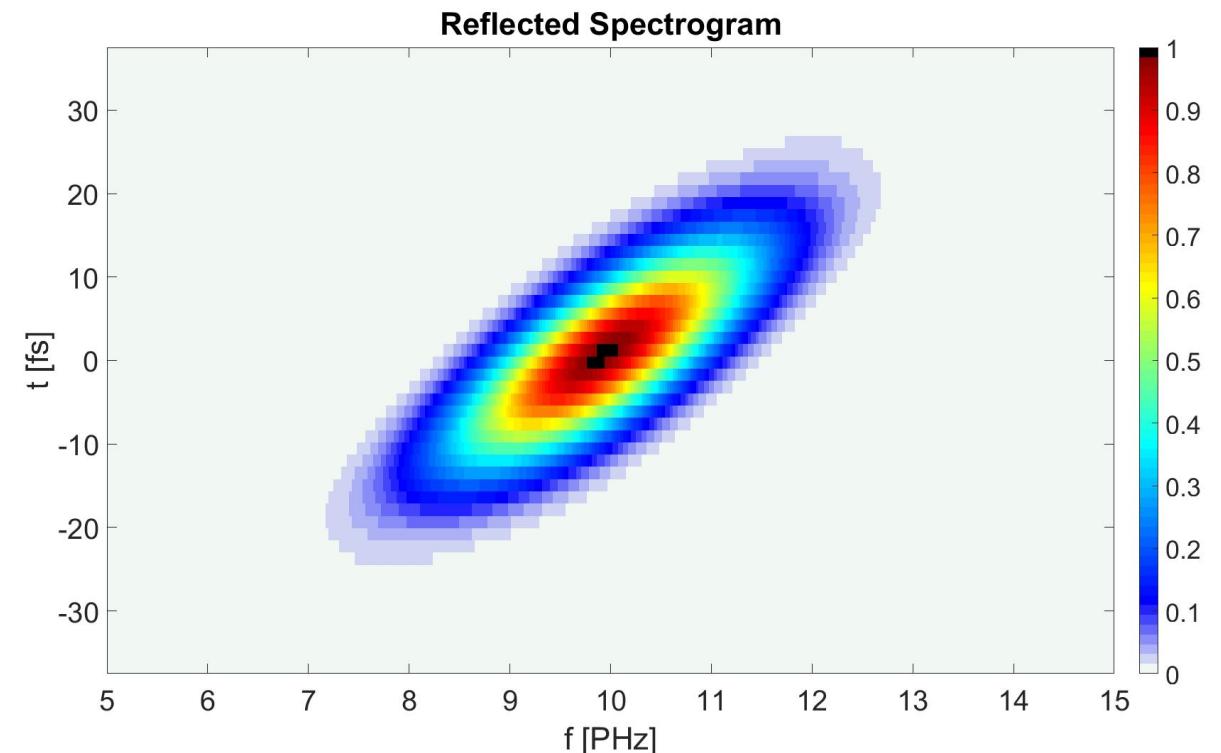
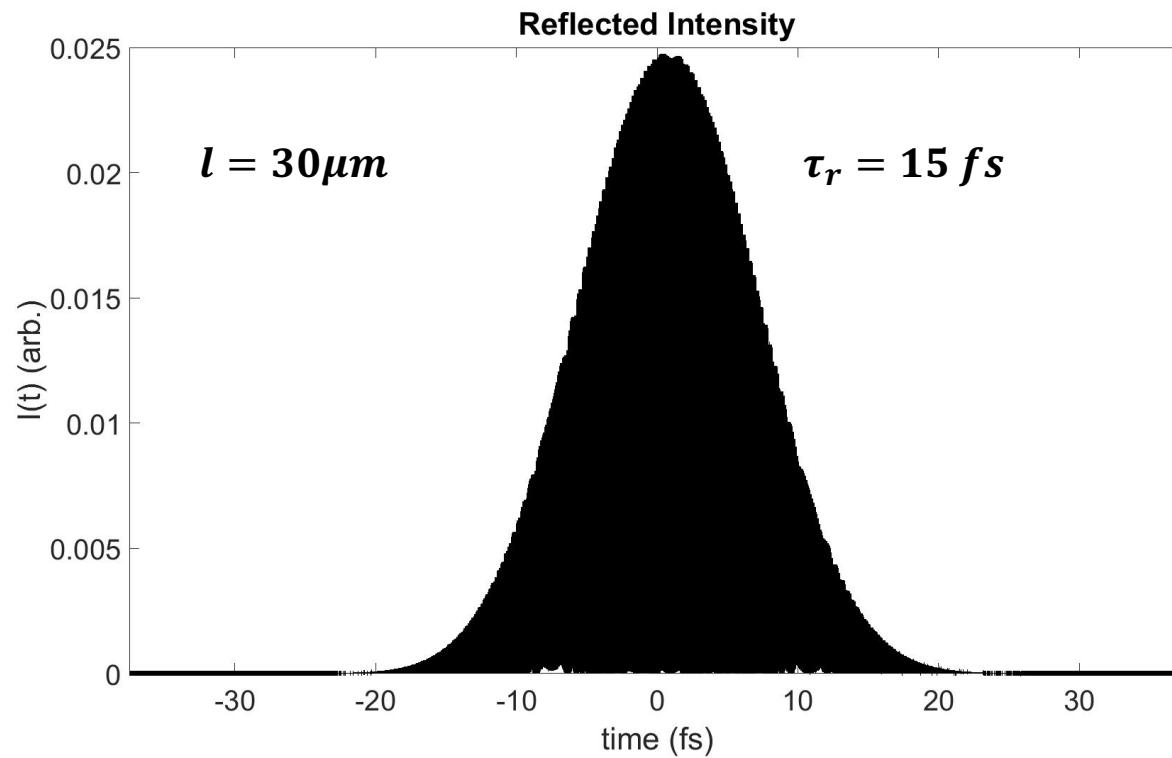
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Dispersion can be mitigated by pre-chirping the incident pulse

# Laser pulses reflected from flying focus-driven ionization fronts can undergo extreme frequency upshifts



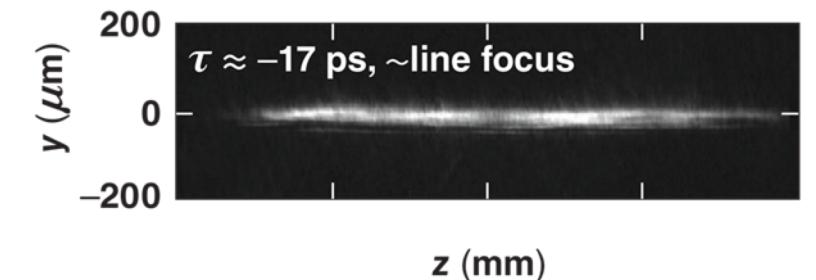
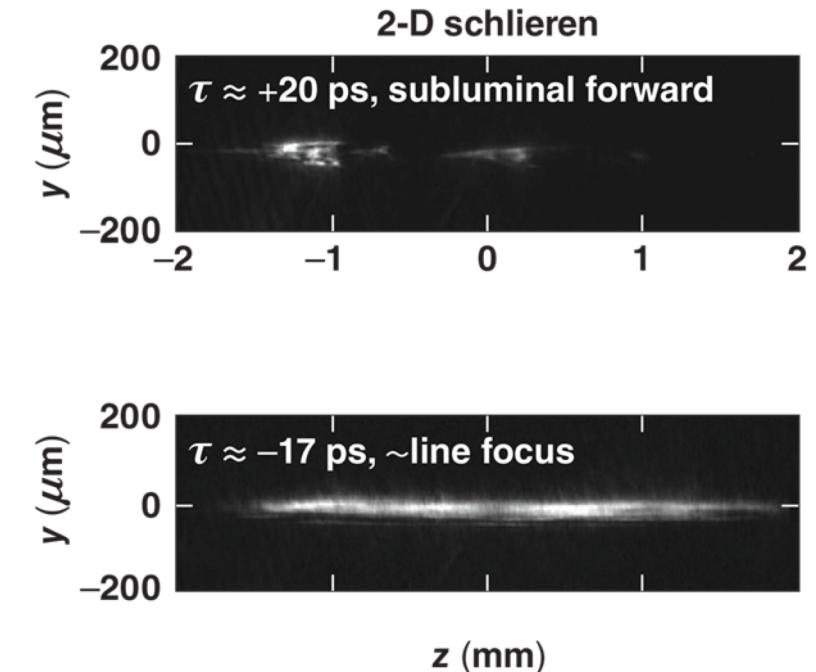
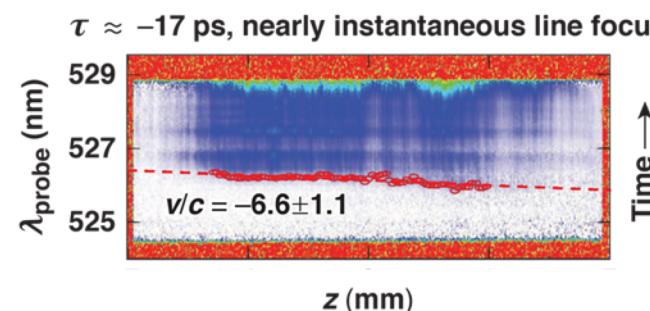
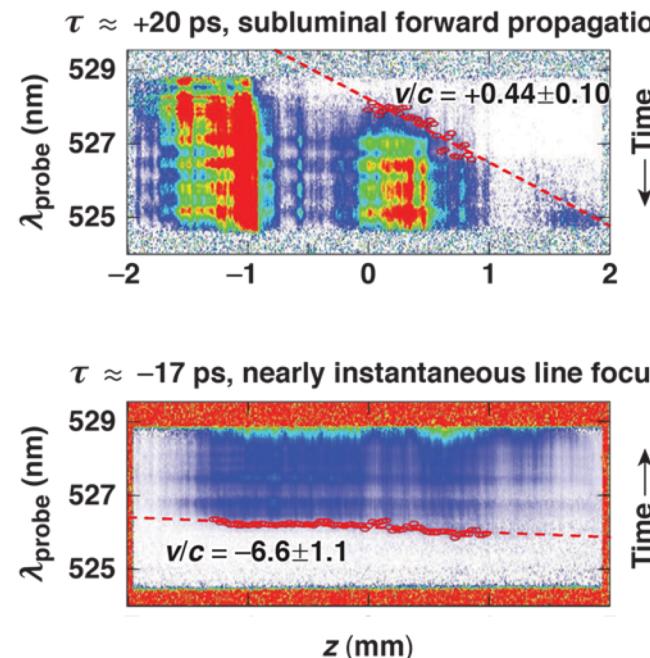
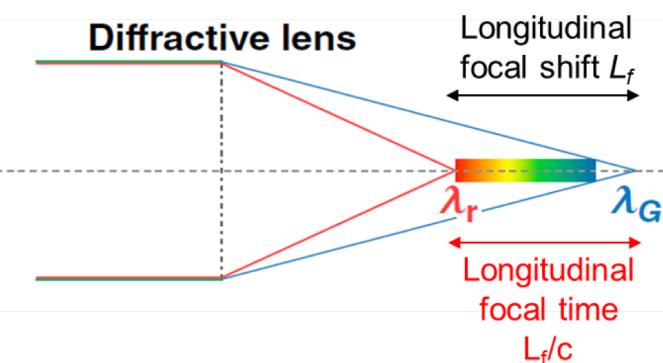
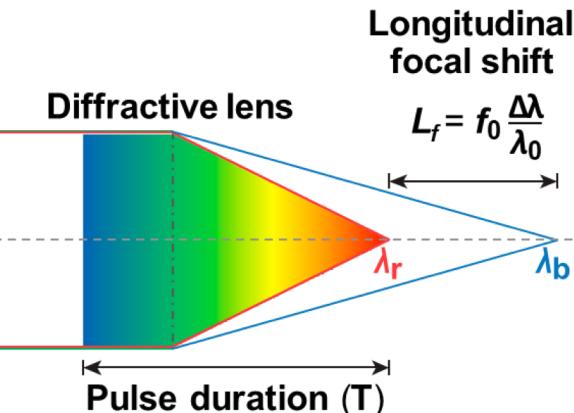
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- Output frequency is easily tuned over a broad range by changing the front velocity

The details of high density IWAV generation are being studied computationally

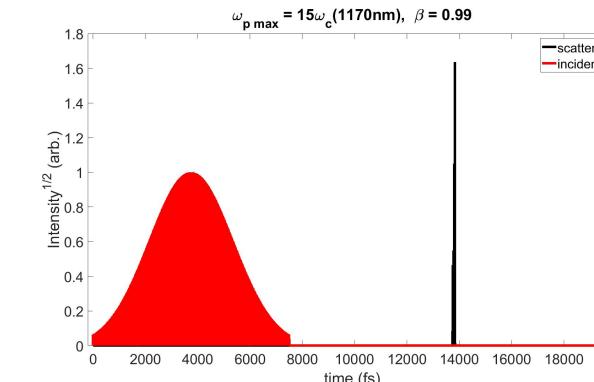
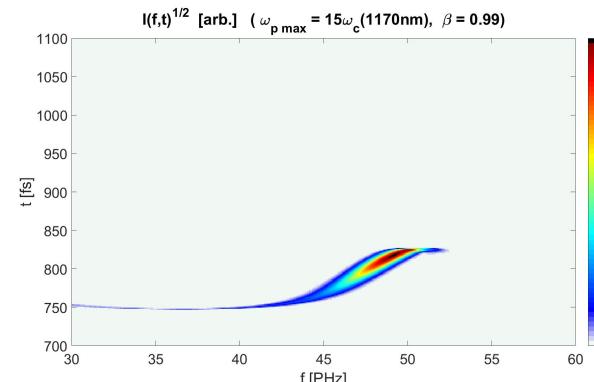
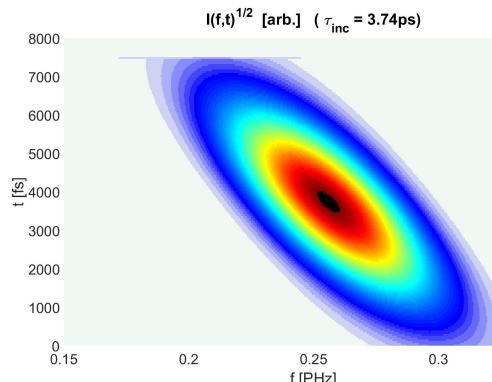
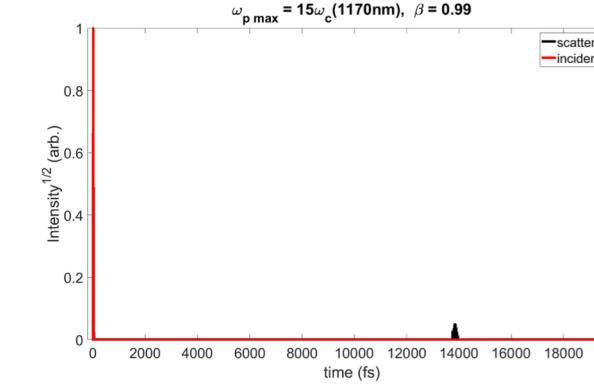
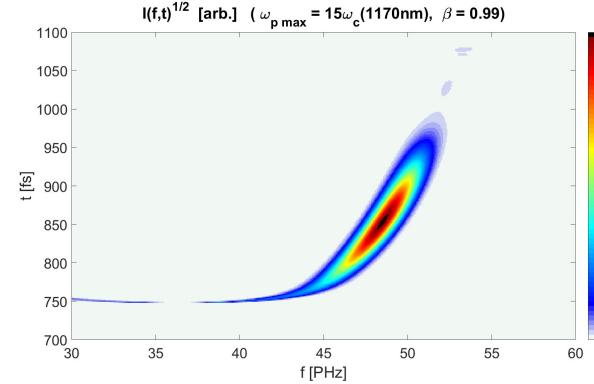
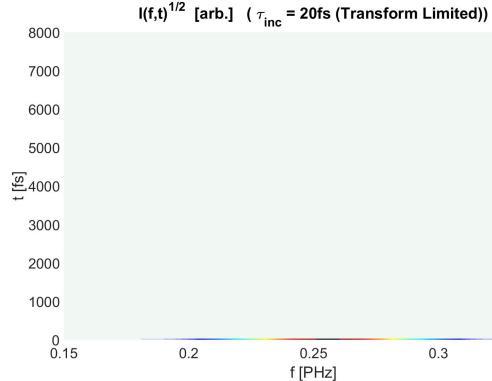
# Backup



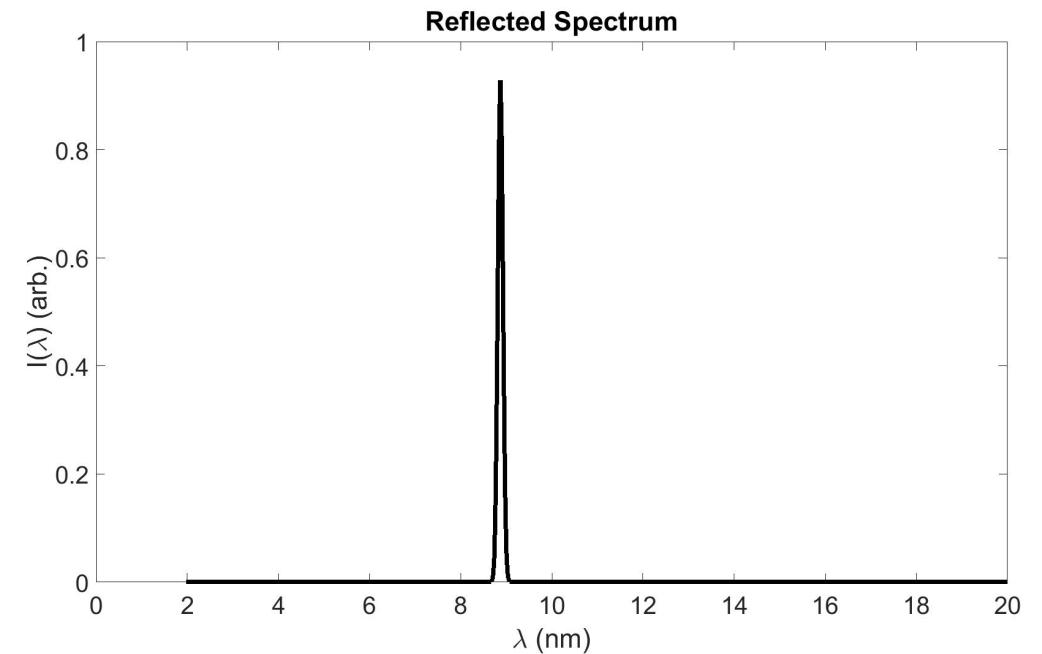
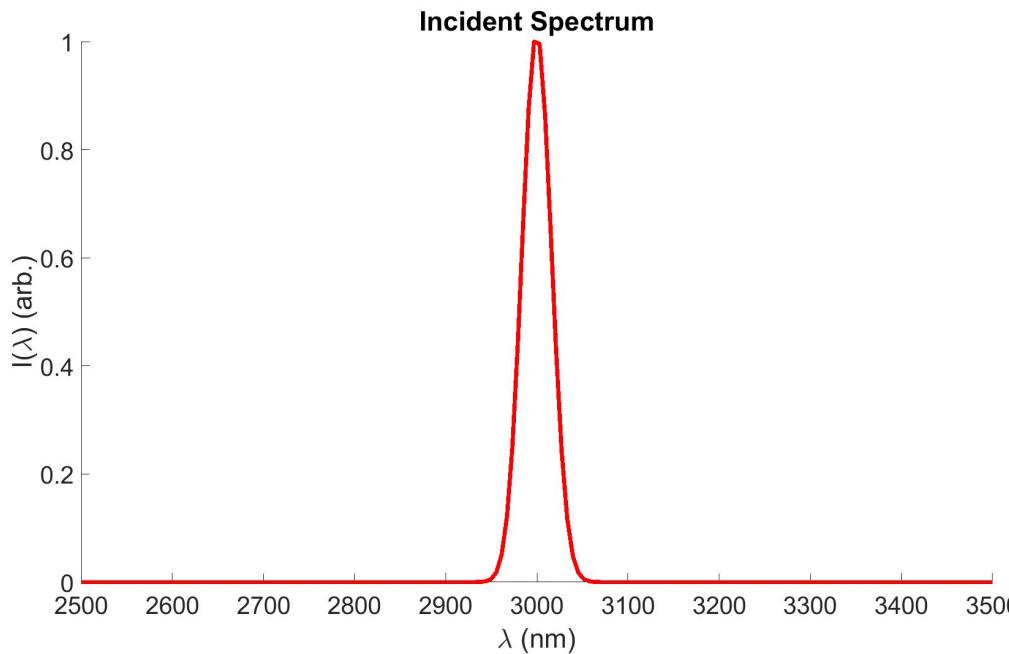
# Backward and/or superluminal focal velocities eliminate the effects of ionization refraction on the IWA V propagation



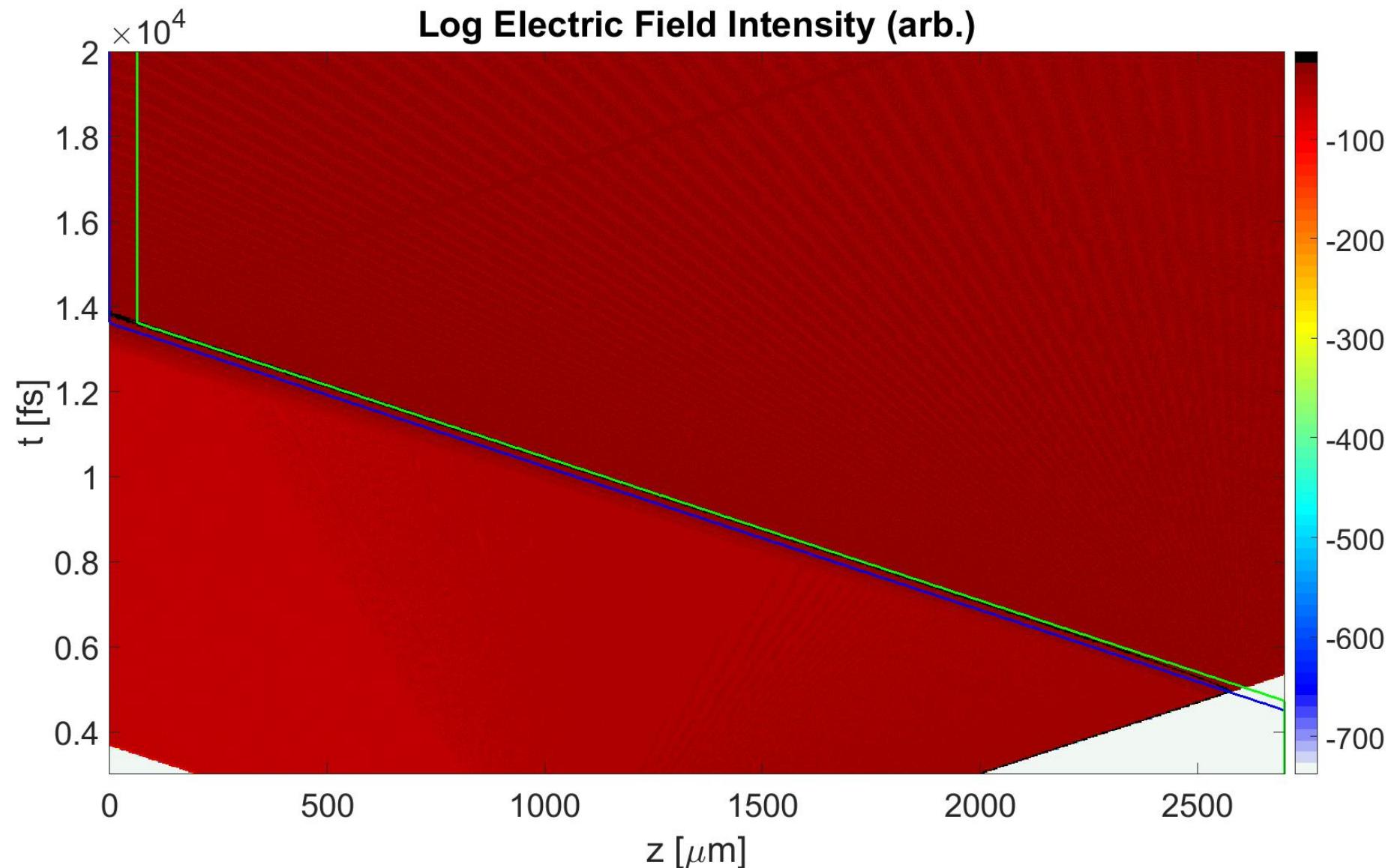
# Introducing a negative chirp to the incident pulse mitigates temporal broadening in the reflected pulse



# Smaller initial frequency and bandwidth permits higher frequency reflected light with the same plasma density



# Fronts of finite width can interact with the test pulse over long distances and durations



# High quality XUV and X-ray sources have broad applicability

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- **HEDP diagnostics**
  - Spectroscopy, radiography, interferometry, scattering
- **Materials science, AMO physics, chemistry and biology**
  - All of the above plus others
- **Industrial applications**
  - Small feature sizes in etching and lithography

# Collaborators

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