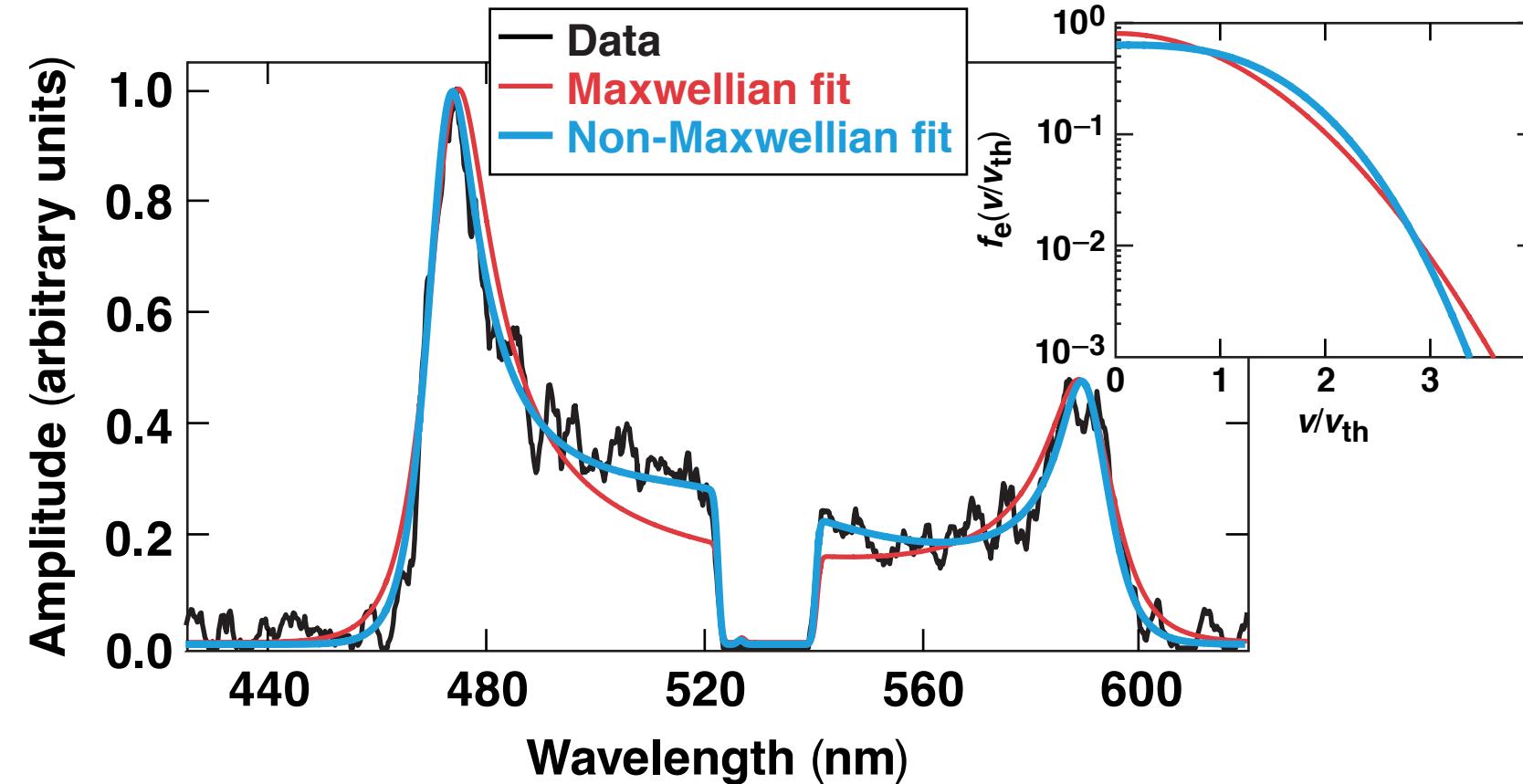


# Measurement of the Langdon Effect in Laser-Produced Plasma Using Collective Thomson Scattering



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# Experiments show evidence of the Langdon effect in a laser-produced plasma using collective Thomson scattering



- Electron plasma wave Thomson-scattering spectra were used to measure non-Maxwellian distribution functions driven by the Langdon effect
- Analyzing non-Maxwellian data as Maxwellian leads to significant errors in the inferred parameters
- The experimentally measured Langdon parameter agrees with theoretical predictions

# Collaborators

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# Inverse-bremsstrahlung (IB) heating is predicted to generate non-Maxwellian electron distribution functions

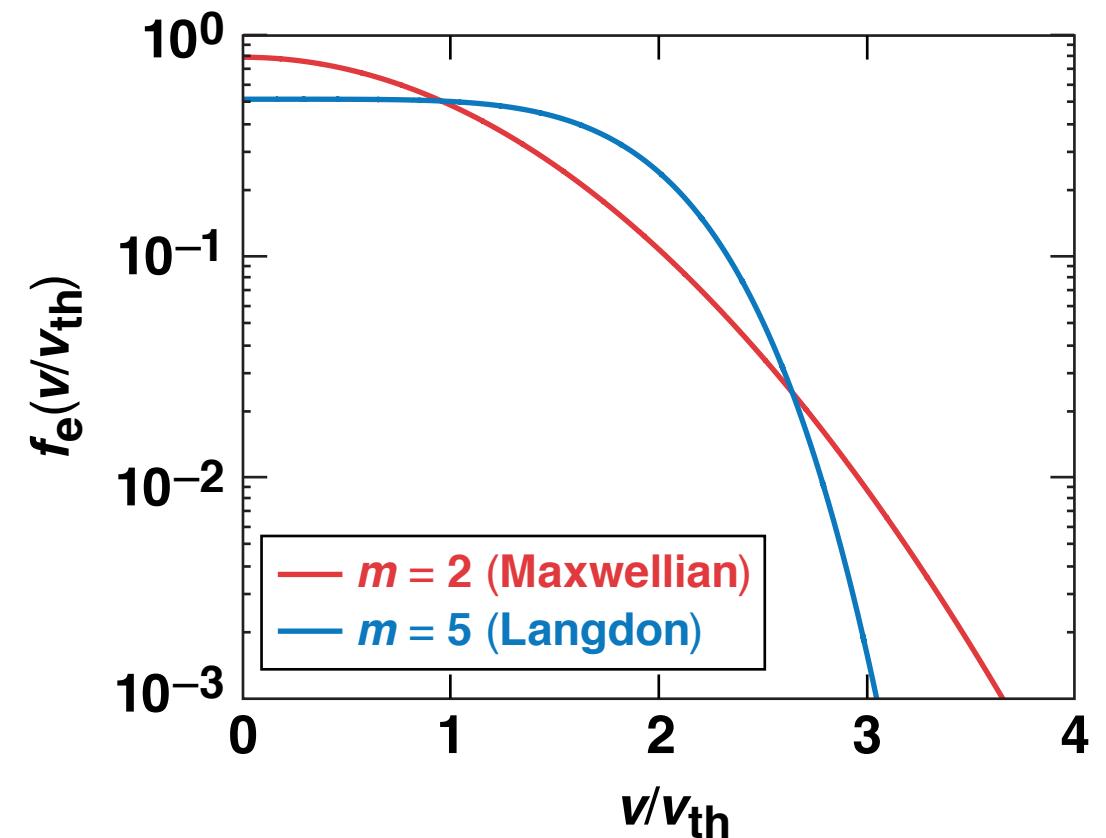
- IB heating causes the electron distribution function to go toward a fifth-order super-Gaussian\* (Langdon Effect)

$$f_m(x, v, t) = C_m \exp[-(v/v_m)^m]$$

$$v_m^2 = \frac{3k_B T_e}{M_e} \frac{\Gamma(3/m)}{\Gamma(5/m)} \quad \text{and} \quad C_m = \frac{n_e}{4\pi} \frac{m}{\Gamma(3/m)v_m^3}$$

- Super-Gaussian order varies continuously with the Langdon parameter\*\*

$$L = Z \left( \frac{v_{\text{osc}}}{v_{\text{th}}} \right)^2 \quad m = 2 + \frac{3}{1 + 1.66/L^{0.724}}$$



\*A. B. Langdon, Phys. Rev. Lett. **44**, 575 (1980).

\*\*J. P. Matte *et al.*, Plasma Phys. Control. Fusion **30**, 1665 (1988).

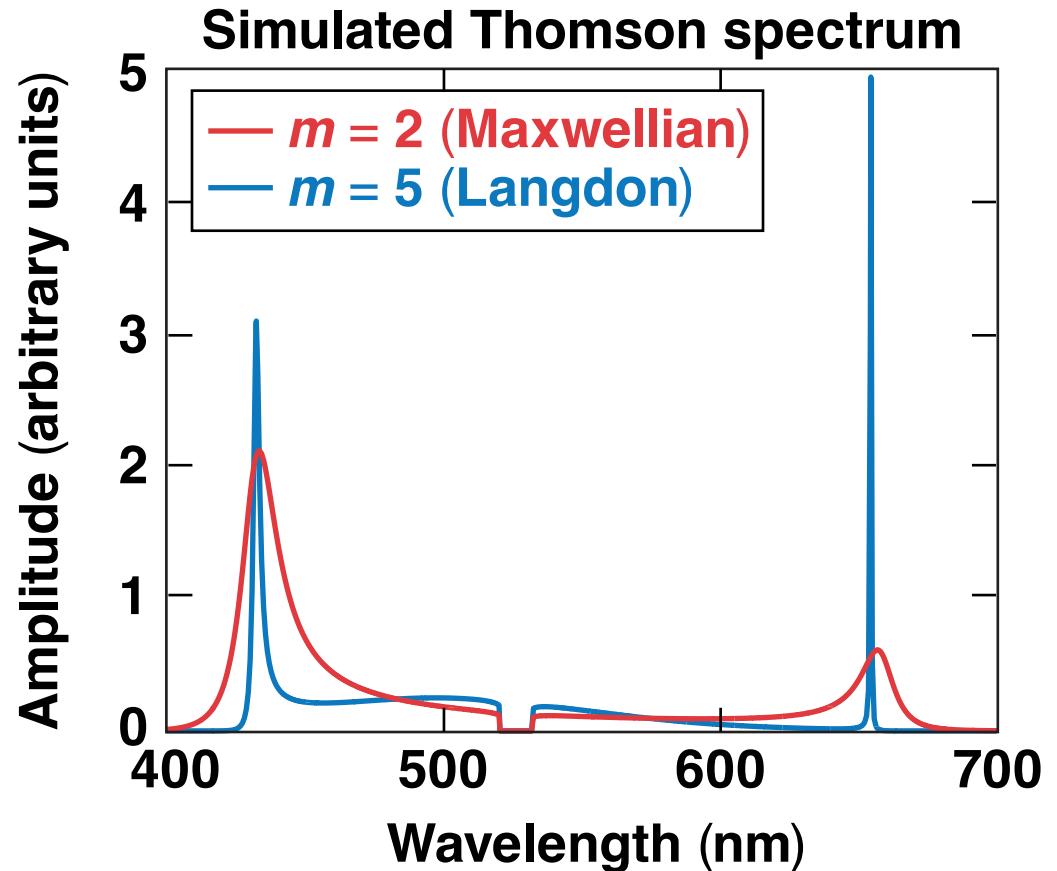
# The Thomson-scattering spectrum can be used to determine a unique electron distribution function

- The spectral density function determines the shape of the scattered spectrum

$$S(\vec{k}, \omega) \approx \frac{2\pi}{k} \frac{f_e(\omega/k)}{\left|1 + \chi_e\right|^2}$$

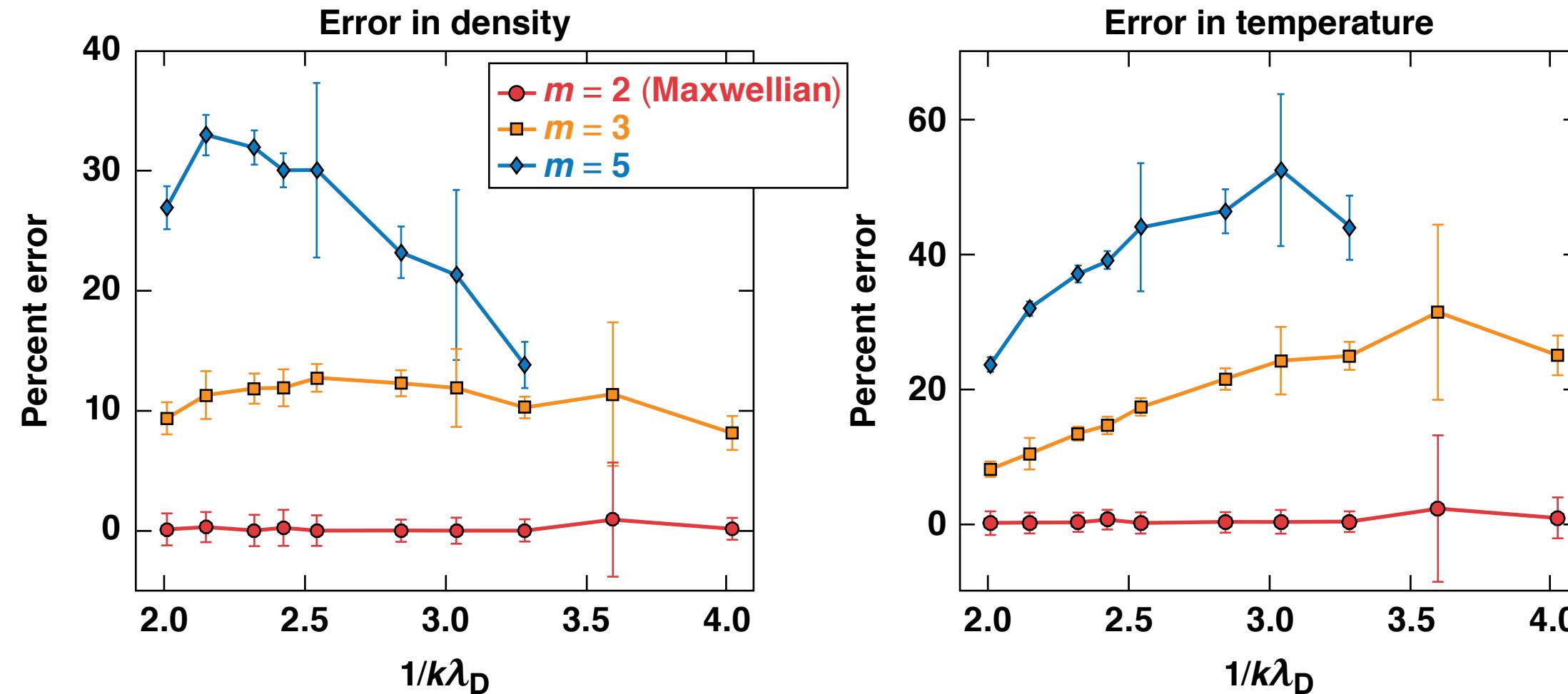
$$\chi_e(\vec{k}, \omega) = \int_{-\infty}^{\infty} d\vec{v} \frac{4\pi e^2 n_e}{m_e k^2} \frac{\vec{k} \cdot \partial f_e / \partial \vec{v}}{\omega - \vec{k} \cdot \vec{v} - i\gamma}$$

$$f_m(x, v, t) = C_m \exp[-(v/v_m)^m]$$



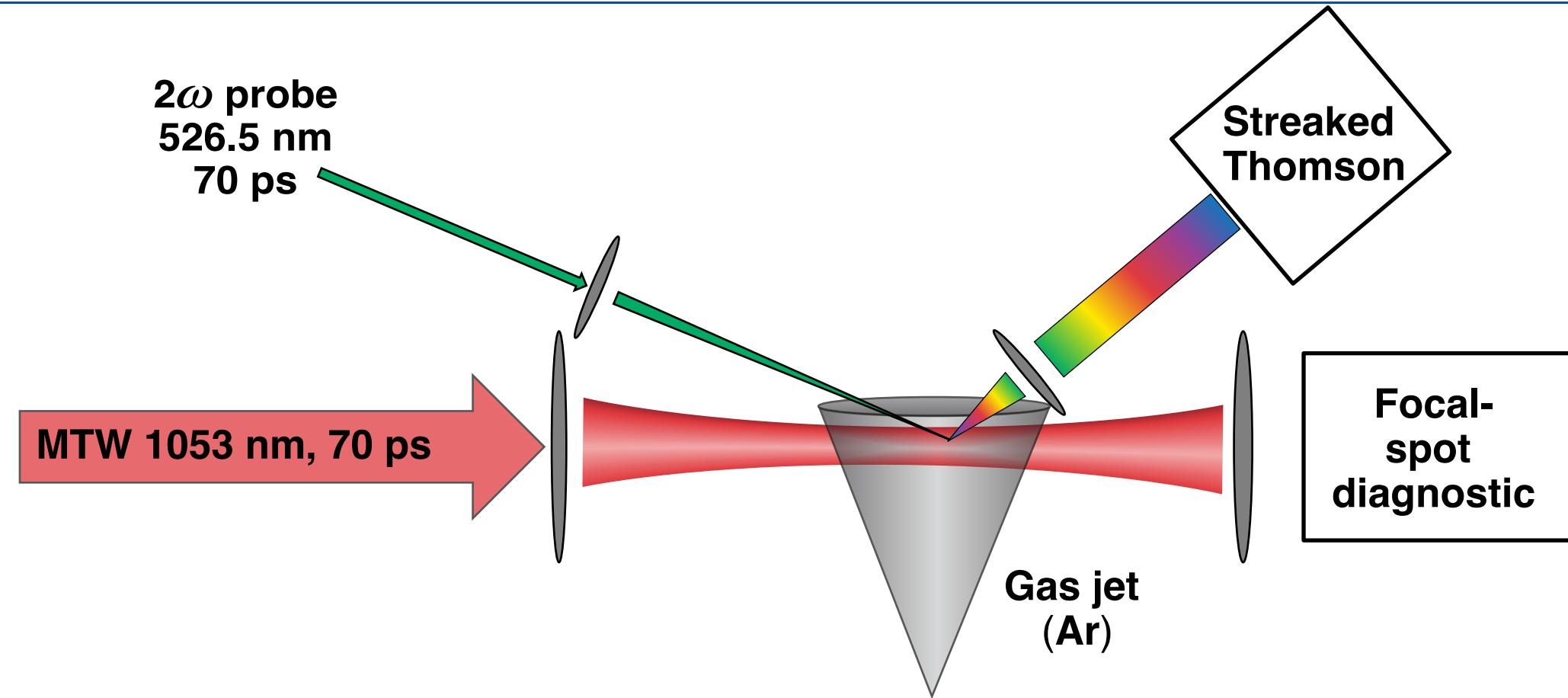
**The Langdon effect has a large impact on the electron plasma wave spectrum.**

# Assuming a Maxwellian electron distribution function can result in large errors in the inferred electron temperature and density



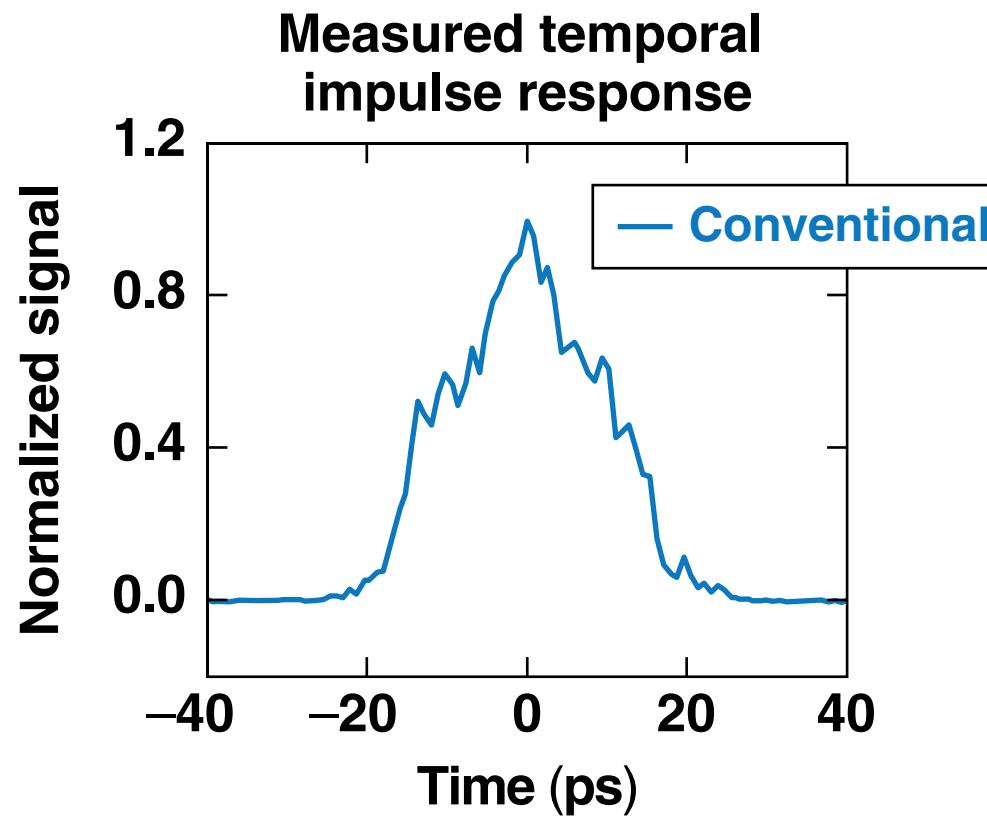
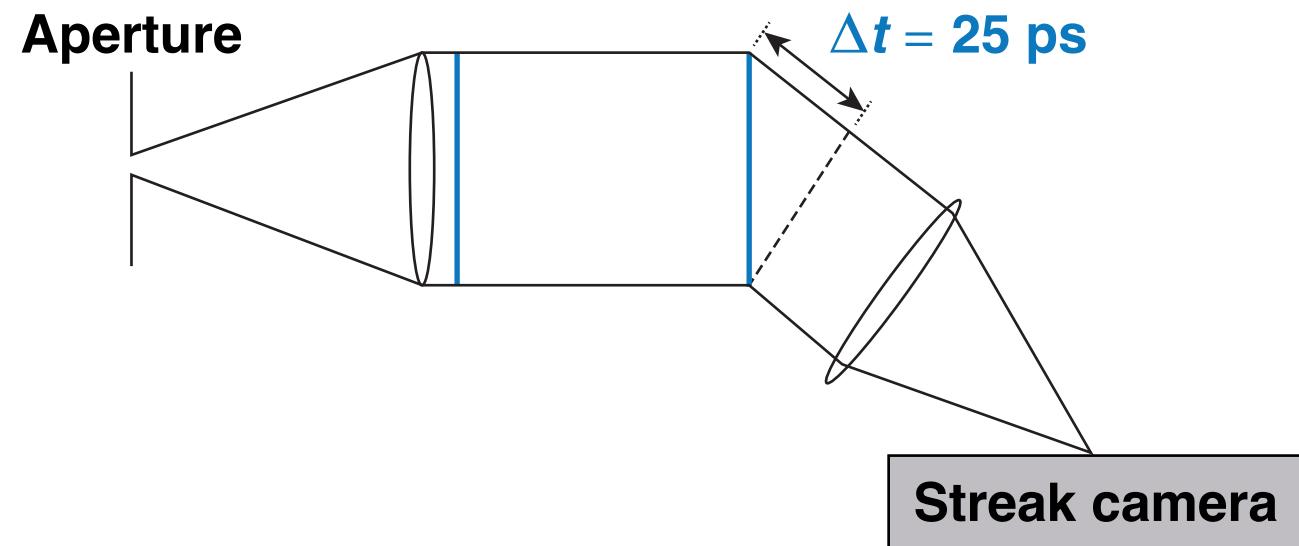
Including the super-Gaussian order in the fit recovers accurate measurements of the plasma conditions.

To measure non-Maxwellian electron distribution functions experimentally, Thomson scattering was performed on gas-jet plasmas using the Multi-Terawatt (MTW) laser

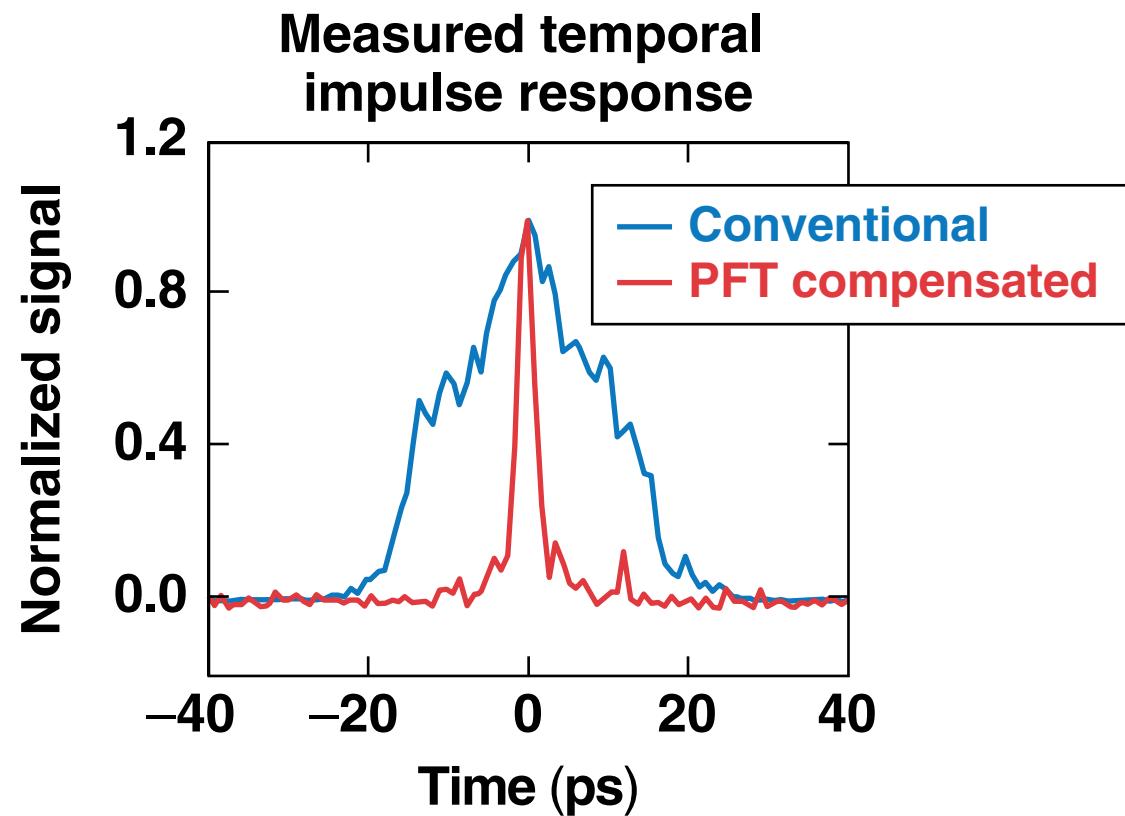
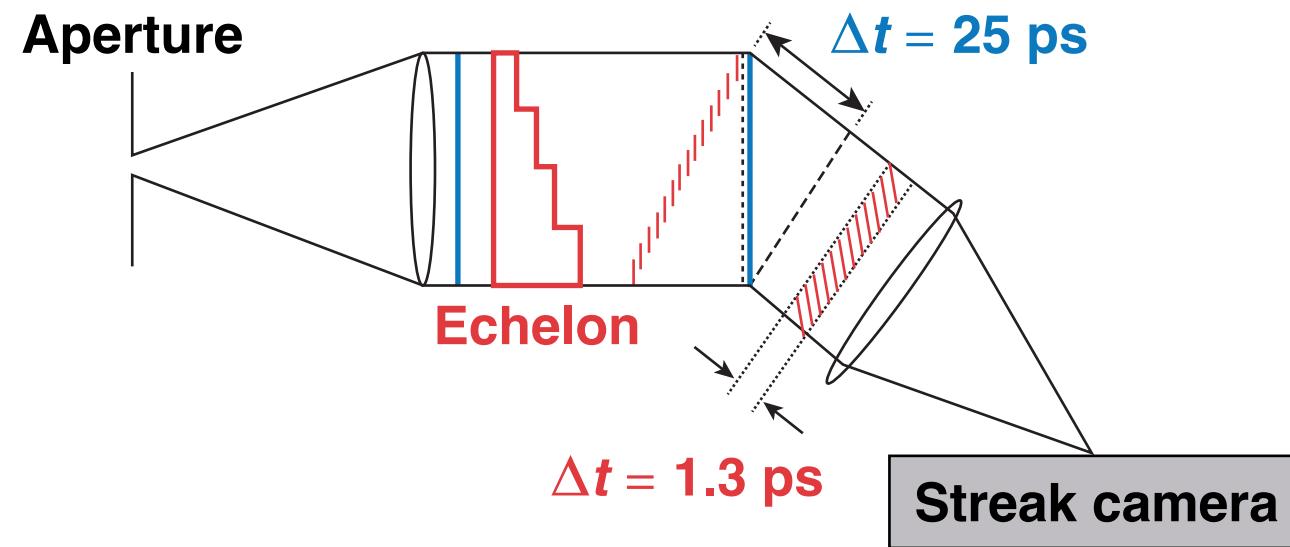


Laser intensity and gas were varied to study the Langdon effect.

# A pulse-front–tilt compensated spectrometer\* was invented to trade unutilized resolving power with temporal resolution

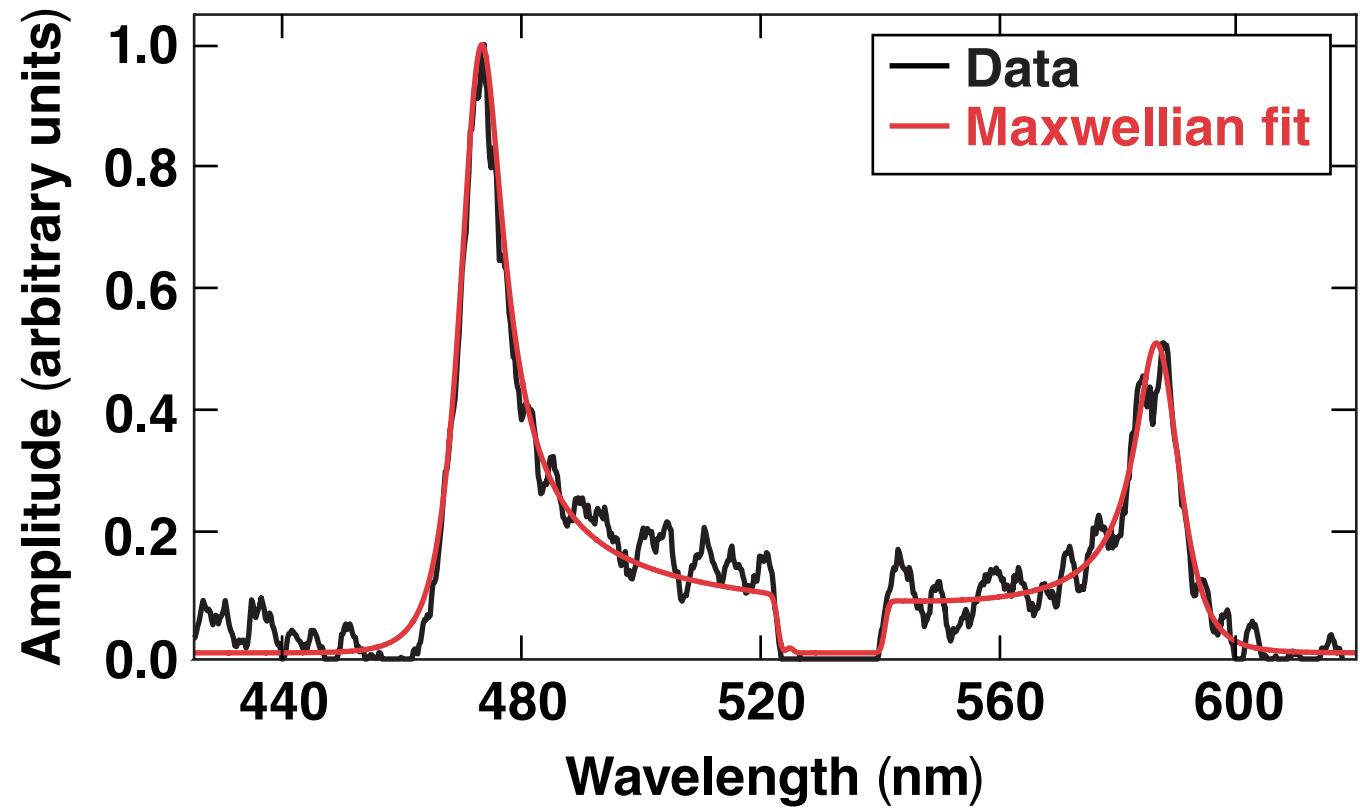
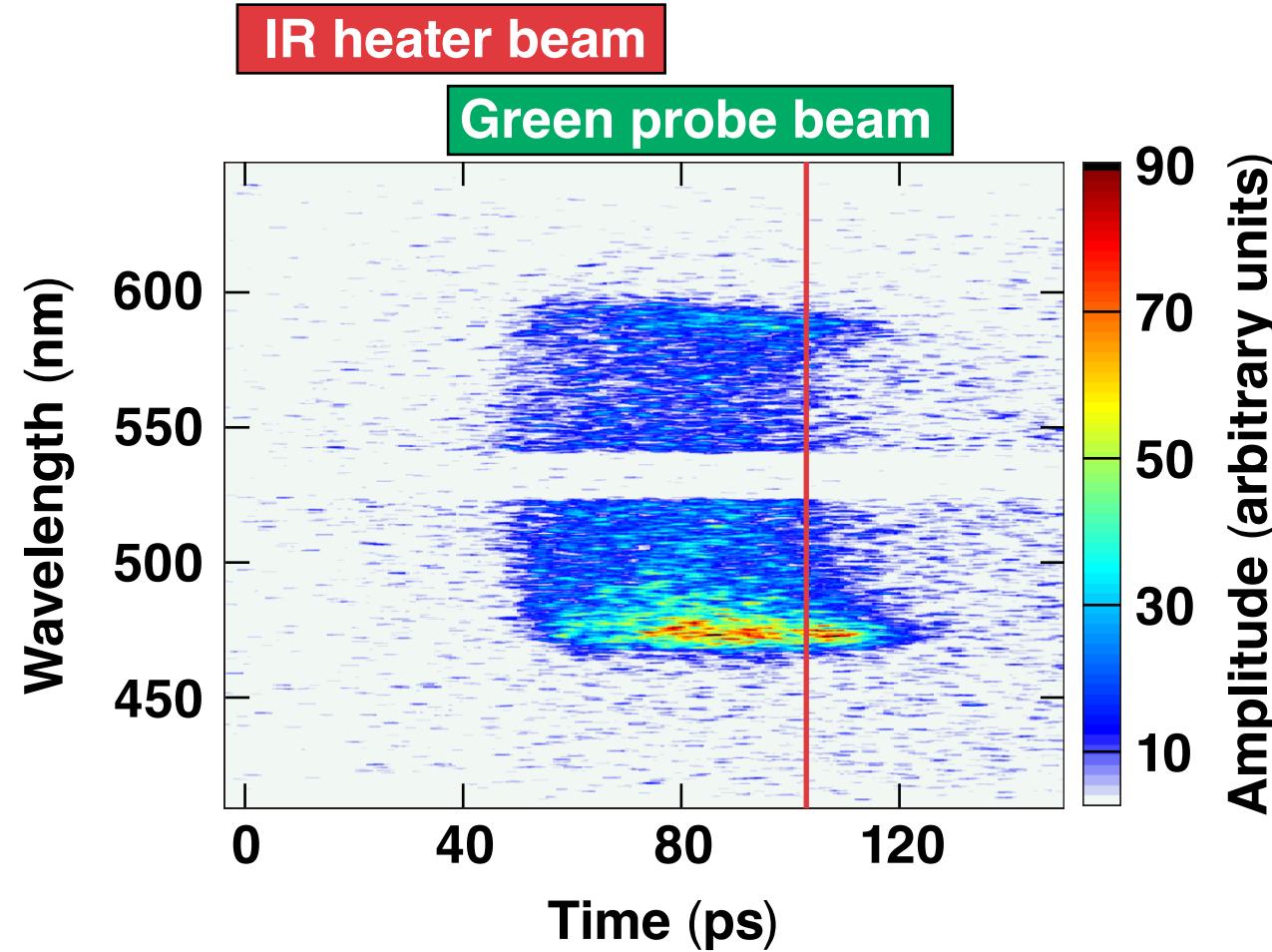


# A pulse-front–tilt (PFT) compensated spectrometer\* was invented to trade unutilized resolving power with temporal resolution



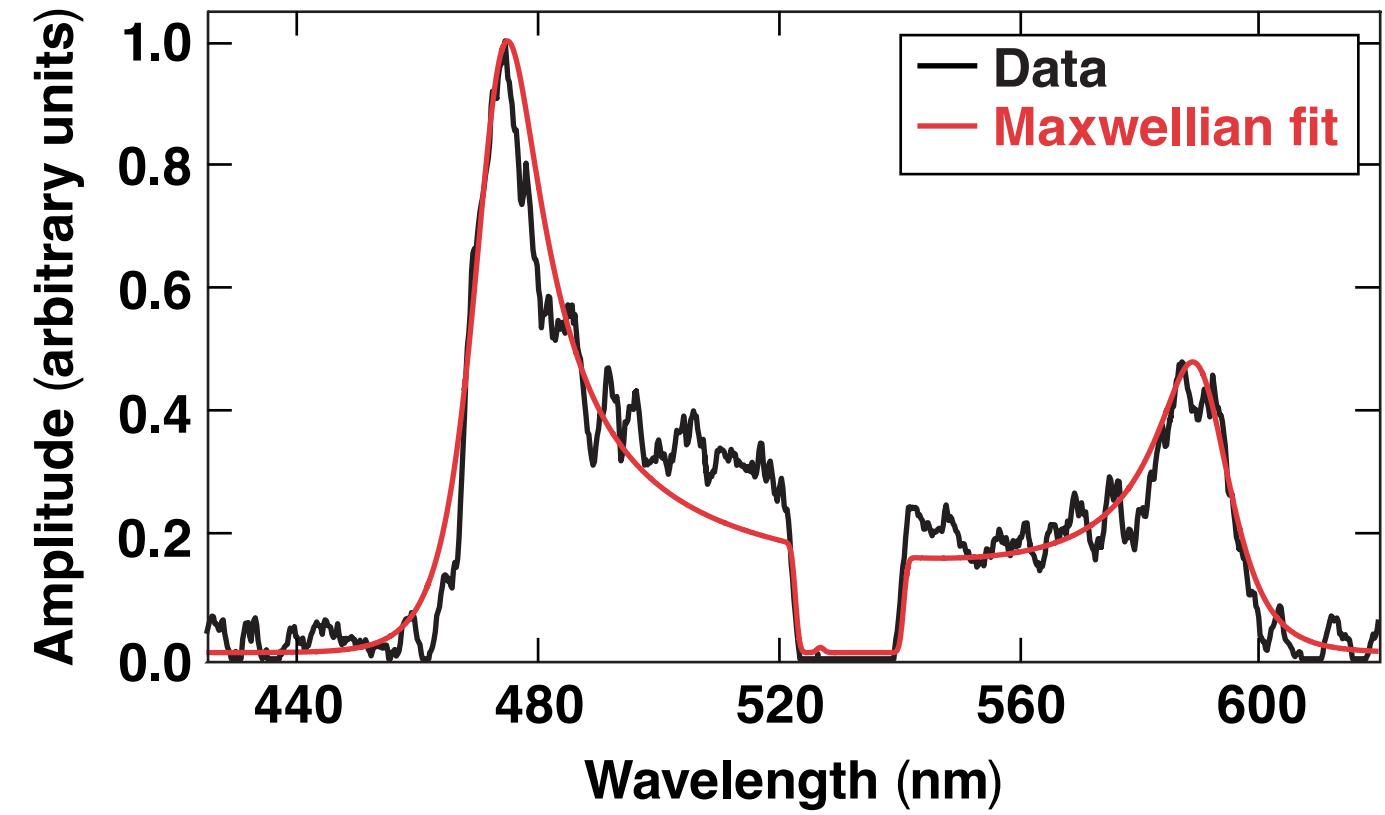
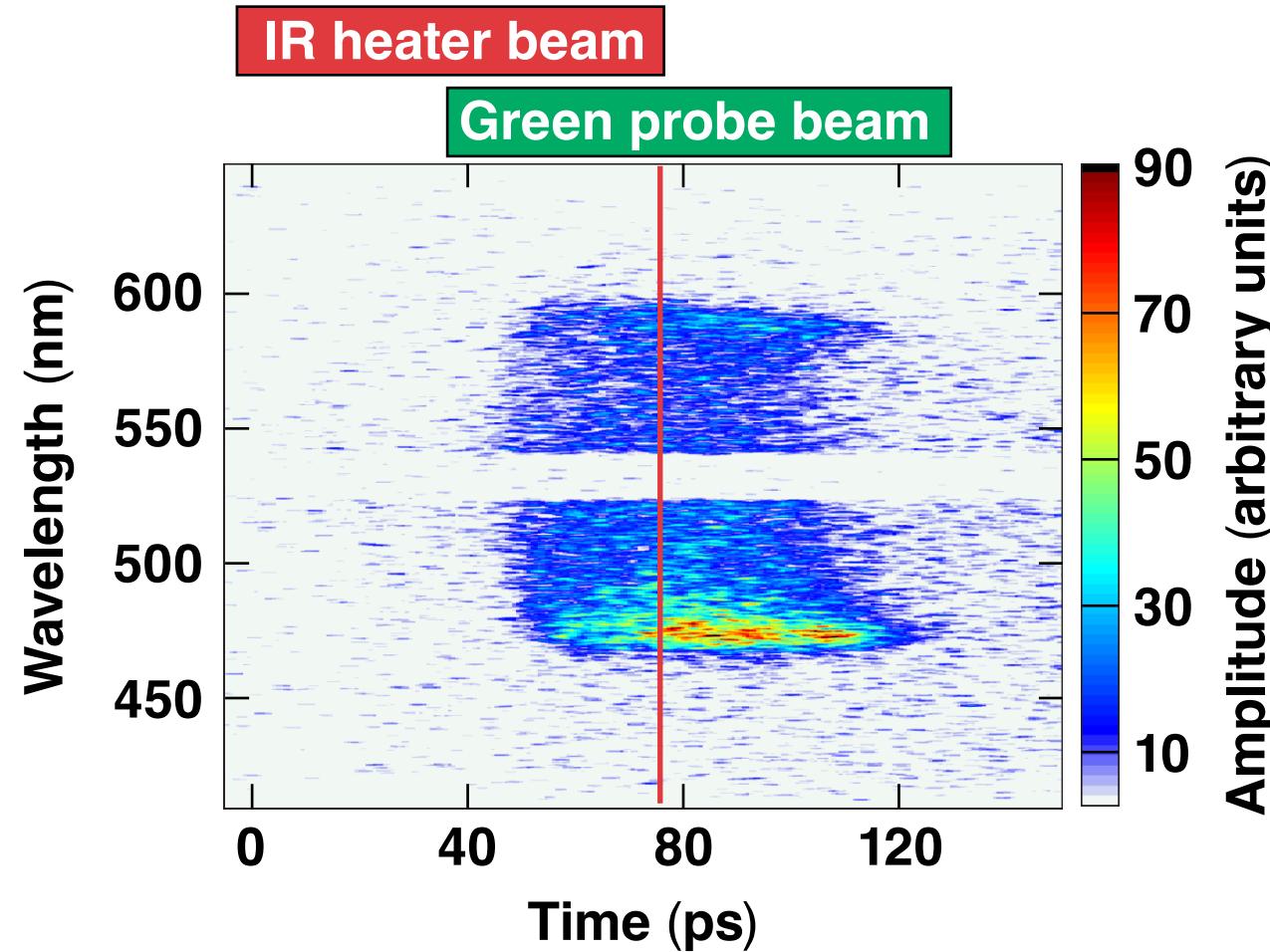
This system is greater than 10 $\times$  faster than an equivalent ( $f/5$ ) conventional streaked-spectrometer diagnostic while maintaining 1-nm spectral resolution.

**Maxwellian theory shows good agreement with measurements late in time and allows an accurate measurement of the plasma conditions**



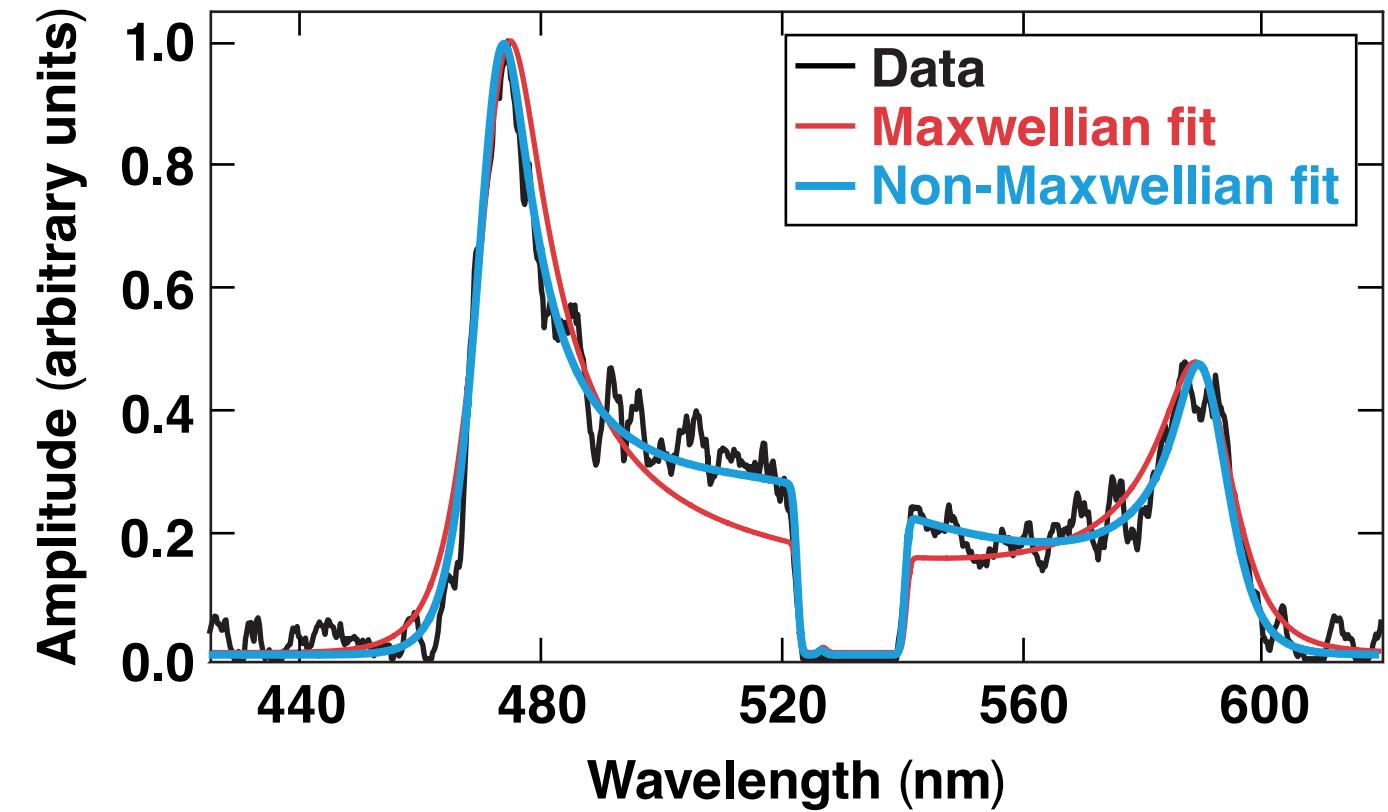
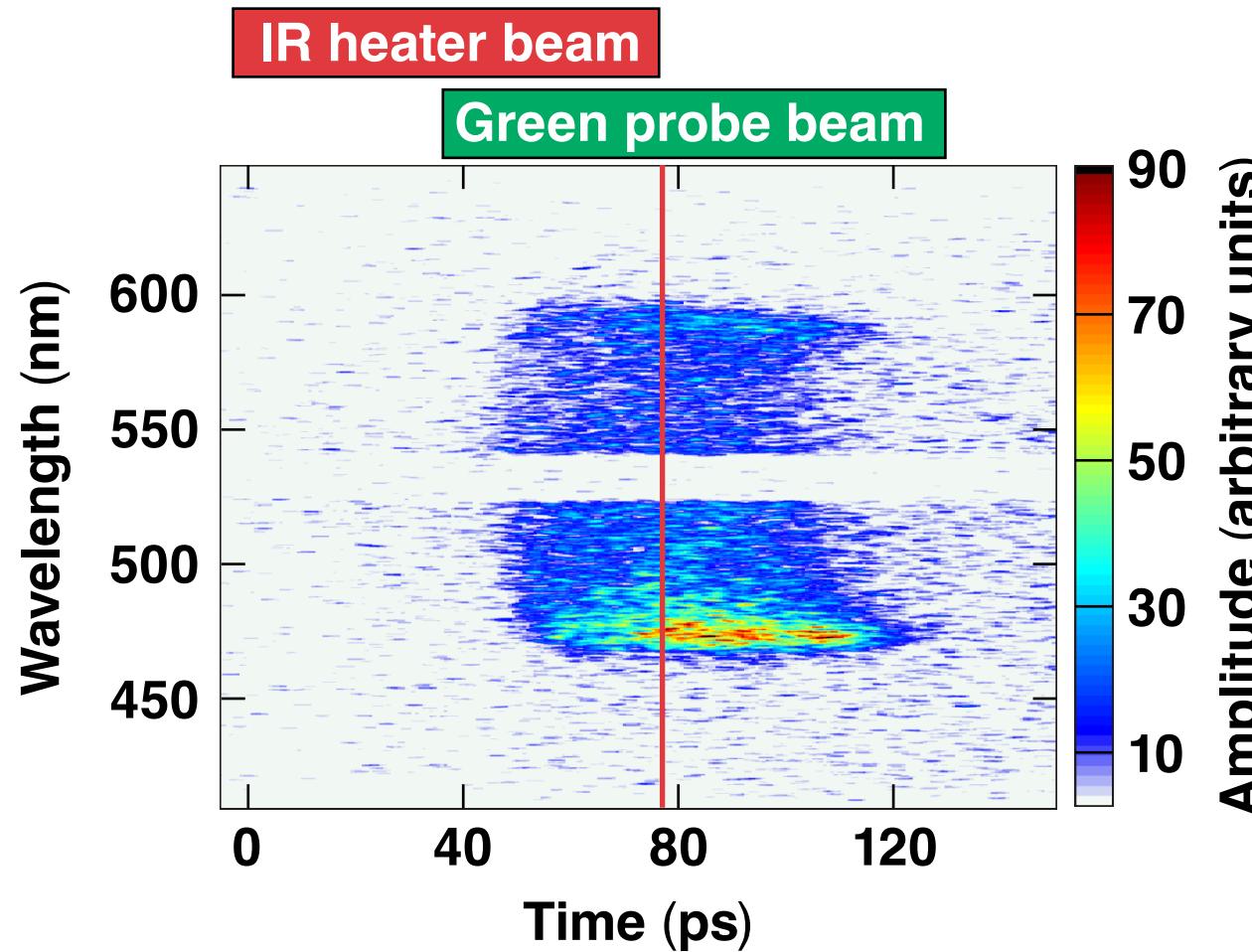
$$n_e = 2.71 \pm 0.04 \times 10^{19} \text{ 1/cm}^3 \quad T_e = 288 \pm 5 \text{ eV}$$

# Maxwellian theory shows discrepancies with the measurements early in time



$$n_e = 2.41 \pm 0.04 \times 10^{19} \text{ 1/cm}^3 \quad T_e = 364 \pm 5 \text{ eV}$$

# Data early in time is fit well when including non-Maxwellian electron distribution functions



$$\begin{aligned} n_e &= 2.41 \pm 0.04 \times 10^{19} \text{ 1/cm}^3 & T_e &= 364 \pm 5 \text{ eV} & \chi^2 &= 11.518 \\ n_e &= 2.30 \pm 0.04 \times 10^{19} \text{ 1/cm}^3 & T_e &= 379 \pm 5 \text{ eV} & m &= 2.9 \pm 0.2 & \chi^2 &= 4.434 \end{aligned}$$

# The non-Maxwellian electron distribution functions measured from the early time data are in good agreement with Langdon theoretical predictions



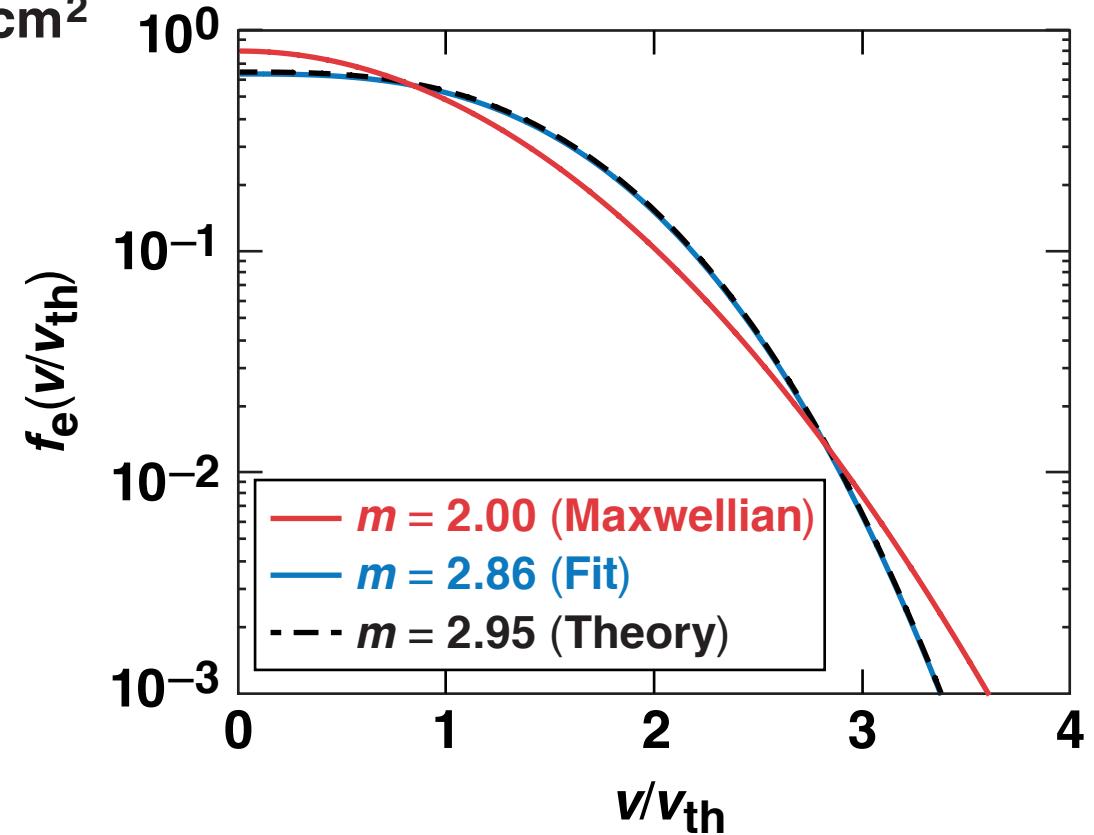
$$L = 0.042 \frac{I_0}{10^{14} \text{ W/cm}^2} \frac{\lambda_0^2}{(1.06 \mu\text{m})^2} \frac{1}{k_B T_e (\text{keV})} Z$$

$$m = 2 + \frac{3}{1 + 1.66/L^{0.724}}$$

$$\begin{aligned} I_0 &= 1.3 \times 10^{14} \text{ W/cm}^2 \\ \lambda_0 &= 1053 \text{ nm} \end{aligned}$$

$$\begin{aligned} Z &= 5 \\ T_e &= 377 \text{ eV} \end{aligned}$$

The fit shown gives  $m = 2.86$  while the formula gives  $m = 2.95$ .



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# Theory including Maxwellian tails does a worse job fitting data

- This is likely because the data are at low  $\alpha$
- This example is at  $\alpha = 1.75$  while crossover appears to be around 2.35

