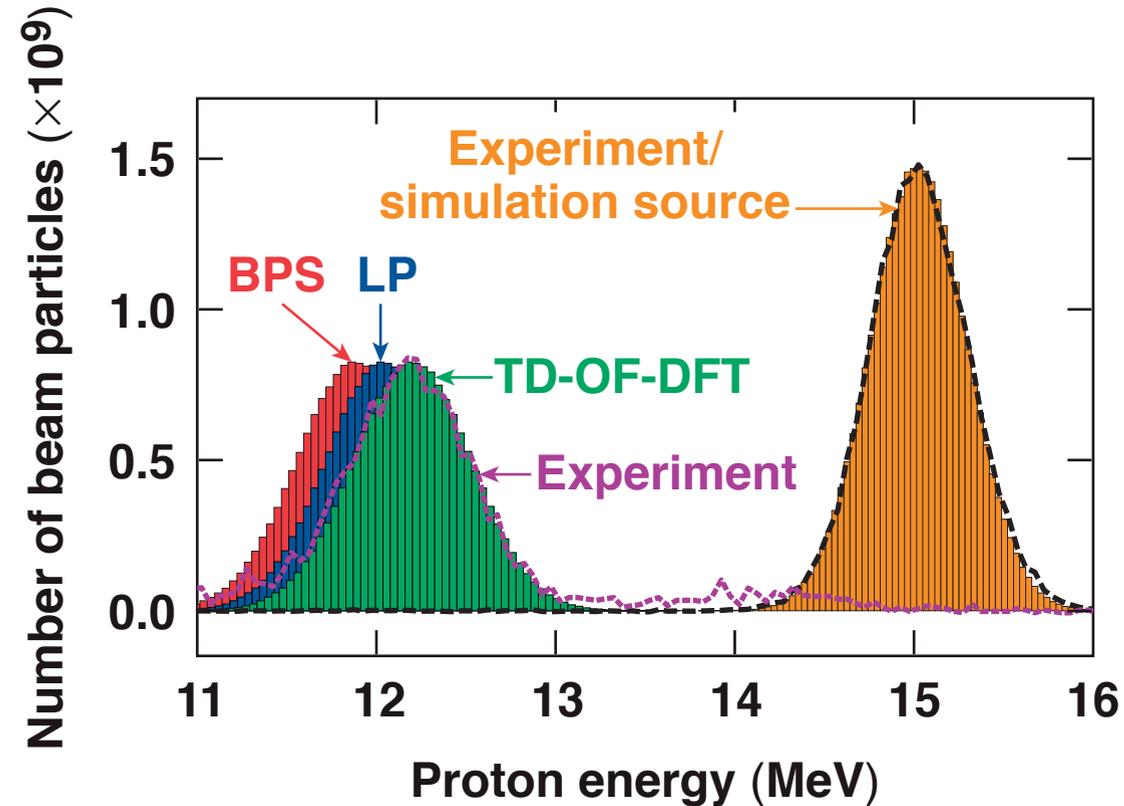


# Ab Initio Studies on Stopping Power of Warm Dense Matter with Time-Dependent Orbital-Free Density Functional Theory



Y. H. Ding  
University of Rochester  
Laboratory for Laser Energetics  
Department of Mechanical Engineering

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## Summary

# A time-dependent orbital-free density functional theory (TD-OF-DFT) code has been developed for *ab initio* investigations of transport properties of warm dense plasmas



- The electron dynamic has been implemented to OF-DFT for first-principles simulations of the transport properties of dense plasma
- Our current-dependent TD-OF-DFT calculations have reproduced the recently well-characterized stopping-power experiment in warm dense beryllium
- For  $\alpha$ -particle stopping in warm and solid-density DT plasmas, the *ab initio* TD-OF-DFT shows a lower stopping power (up to 25%) in comparison with three stopping-power models often used in the high-energy-density physics community

# Collaborators

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**S. X. Hu**

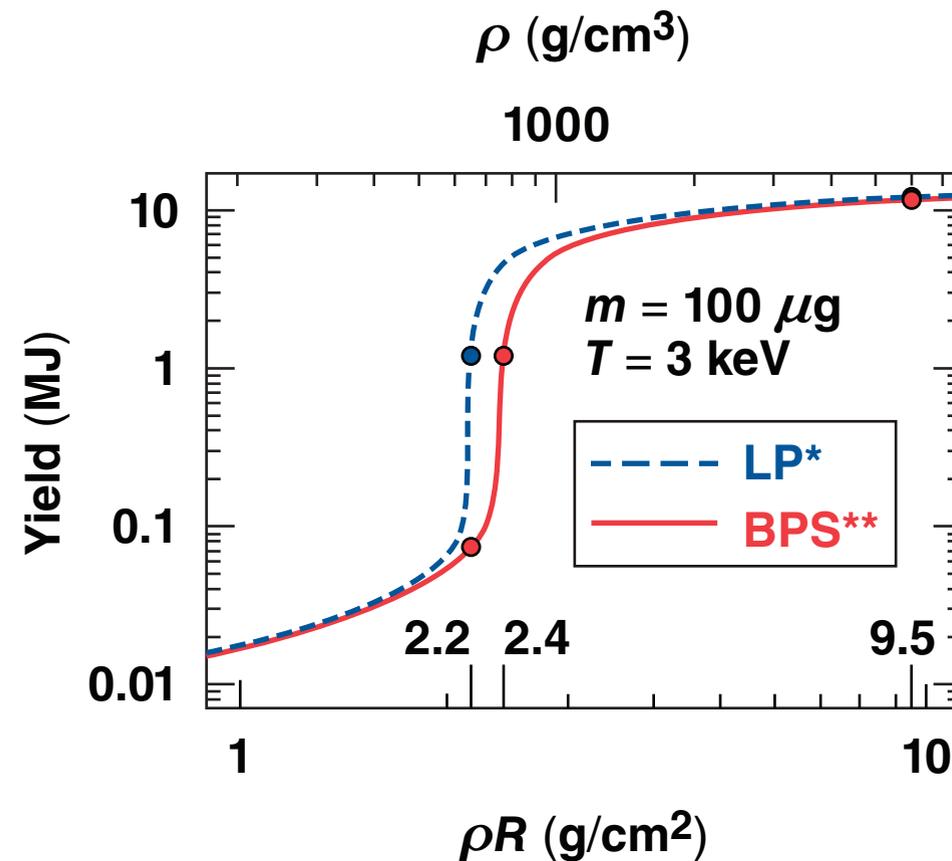
**University of Rochester  
Laboratory for Laser Energetics  
and Department of Mechanical Engineering**

**A. J. White, O. Certik, and L. A. Collins**

**Los Alamos National Laboratory**

## Motivation

Transport properties (thermal/electrical conductivity and stopping power) of dense plasmas are crucial for accurately modeling ICF and HED experiments

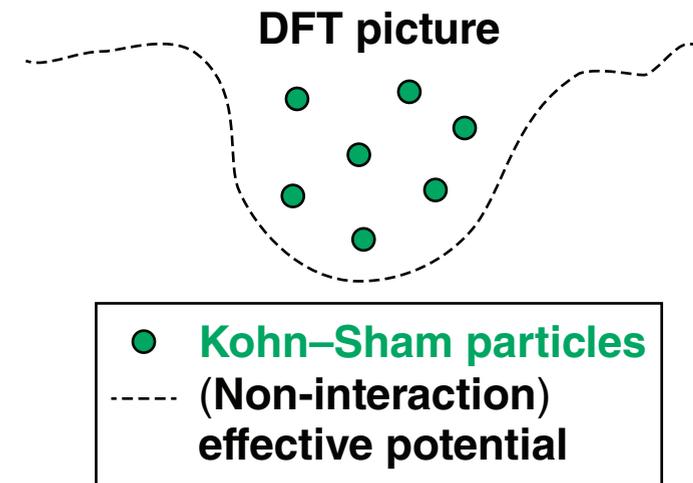
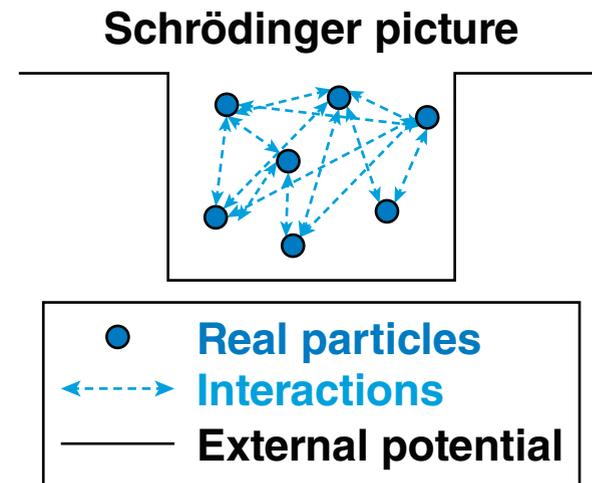


Differences in stopping power will influence energy delivered from  $\alpha$  particles to the dense shell, which will also influence the yield

ICF: inertial confinement fusion  
HED: high-energy density  
LP: Li–Petrasso  
BPS: Brown–Preston–Singleton

\*C. K. Li and R. D. Petrasso, Phys. Rev. Lett. **70**, 3059 (1993); **114**, 199901(E) (2015).  
\*\*L. S. Brown, D. L. Preston, and R. L. Singleton, Jr., Phys. Rep. **410**, 237 (2005);  
R. L. Singleton, Jr., Phys. Plasmas **15**, 056302 (2008).  
†S. X. Hu *et al.*, Phys. Plasmas **23**, 042704 (2016).

# Orbital-free DFT can be used to investigate relatively high-temperature and dense plasmas



$$n(\vec{r}) = \sum_{i=0}^N |\phi_i(\vec{r})|^2 \quad \xrightarrow{\text{Simplify to}} \quad n(\vec{r}) = |\phi(\vec{r})|^2$$

**OF-DFT: only one orbital basis**

The transport properties of warm dense plasmas can be studied by the time-dependent OF-DFT code

# The split-operator (SO) scheme is used to solve the TD-OF-DFT equation

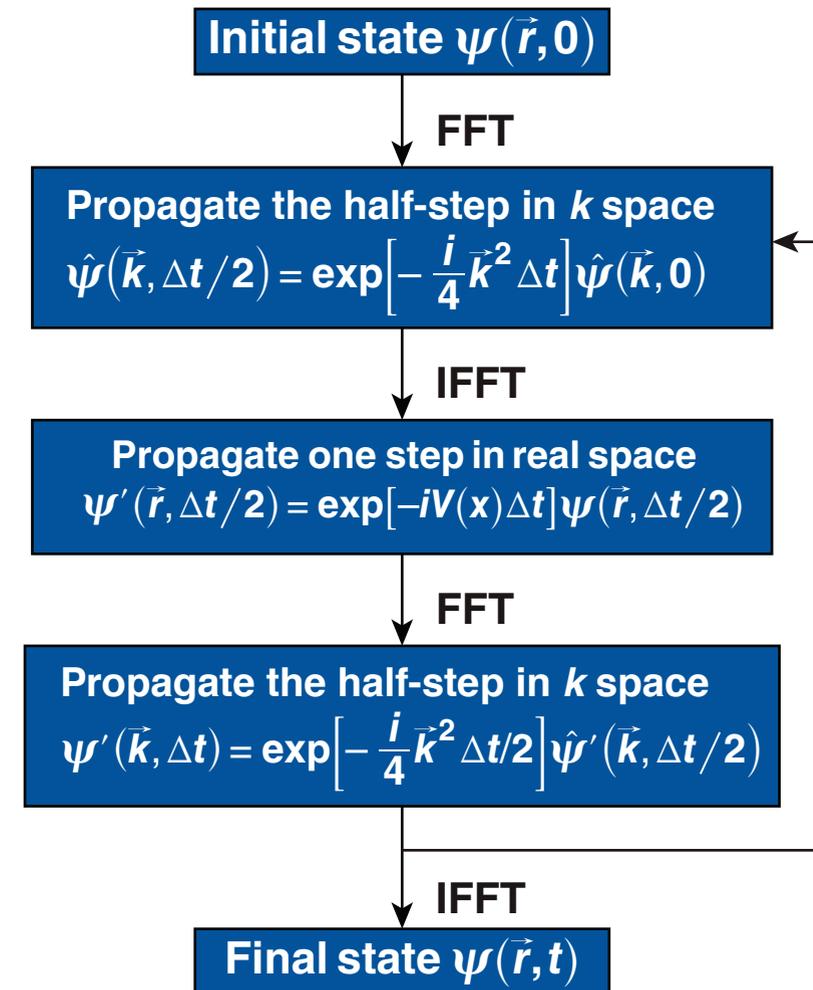
TD-OF-DFT equation:

$$i \frac{\partial \psi(\vec{r}, t)}{\partial t} = \left[ -\frac{1}{2} \nabla^2 + V_{\text{eff}}(\vec{r}, t) + V_{\text{dyn}}(\vec{r}, t) \right] \psi(\vec{r}, t)$$

To capture the low-frequency, long-wavelength current response, we introduce a current-dependent\* (CD) dynamic kinetic energy potential (functional derivative)

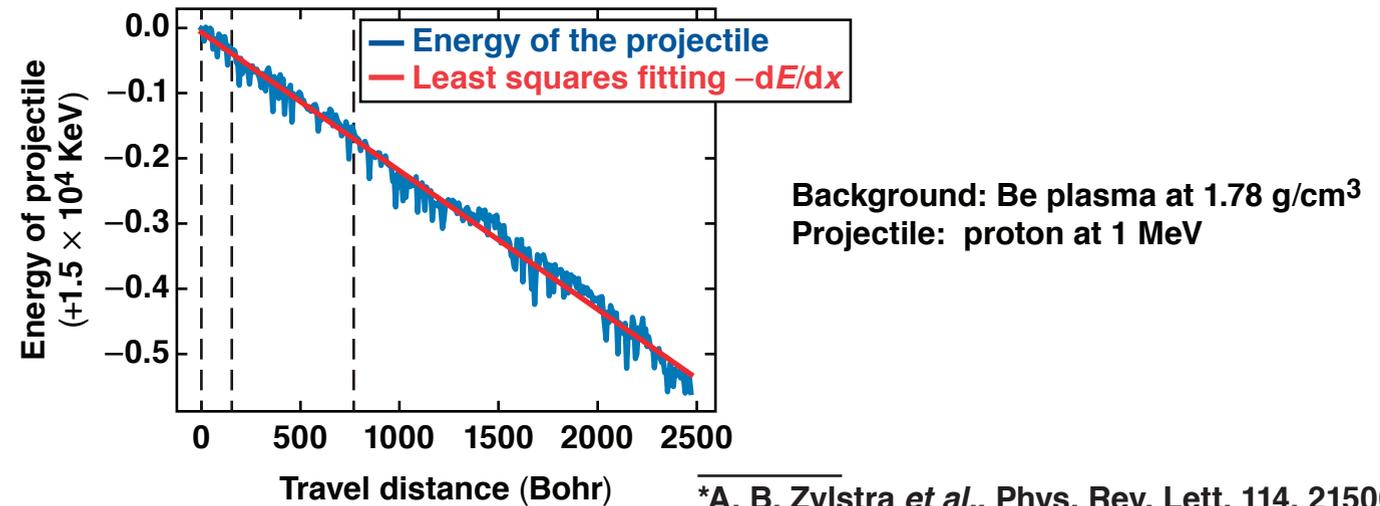
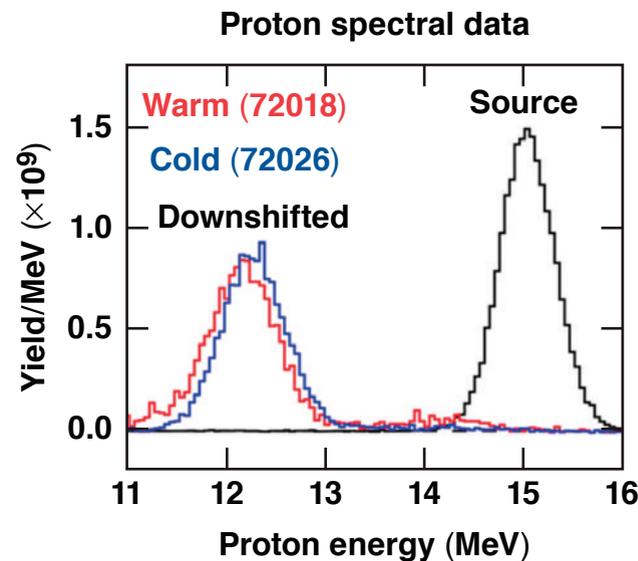
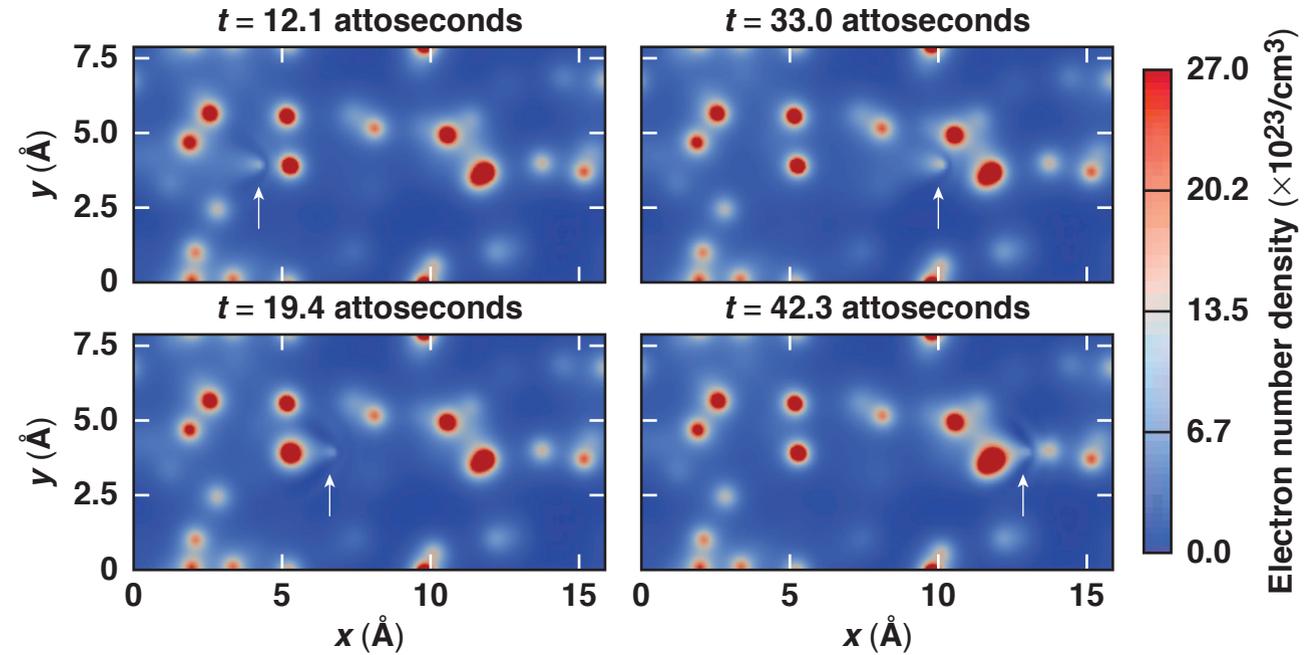
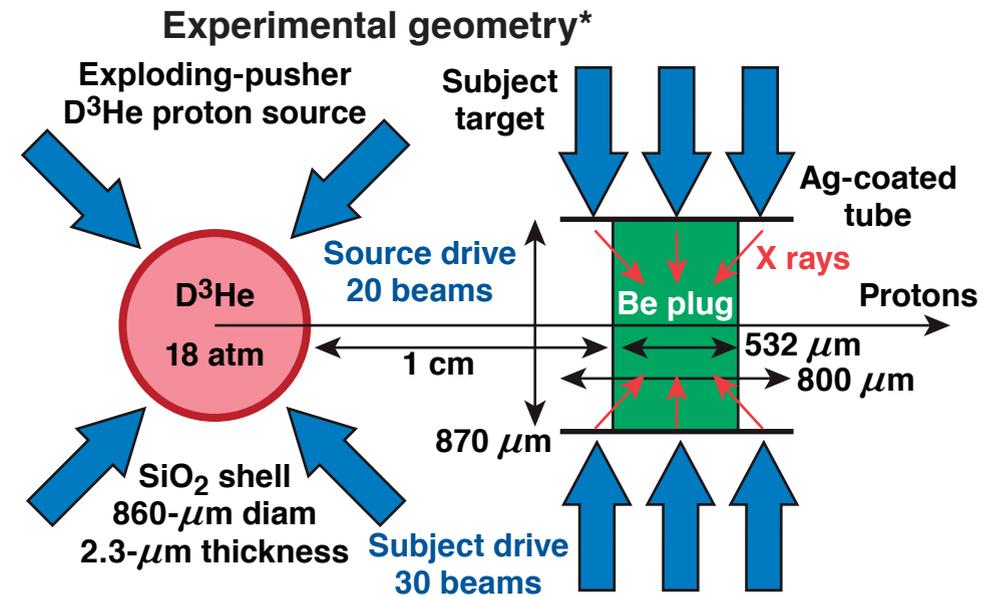
$$V_{\text{dyn}}(\vec{r}, t) = \frac{\pi^3}{2k_F^2(\vec{r}, t)} \mathcal{F}^{-1} \left[ i\vec{q} \cdot \mathbf{J}(\vec{q}, t) / \|\mathbf{q}\| \right](\vec{r})$$

derived using the Lindhard response function match method



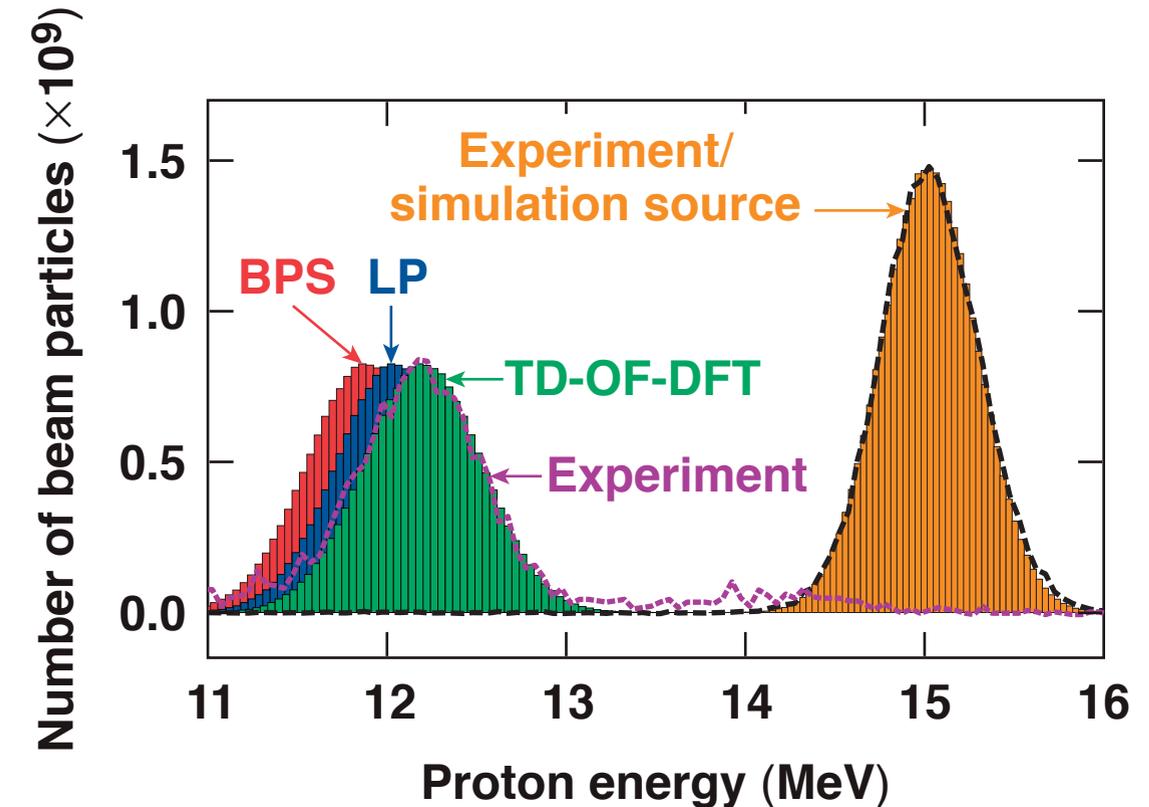
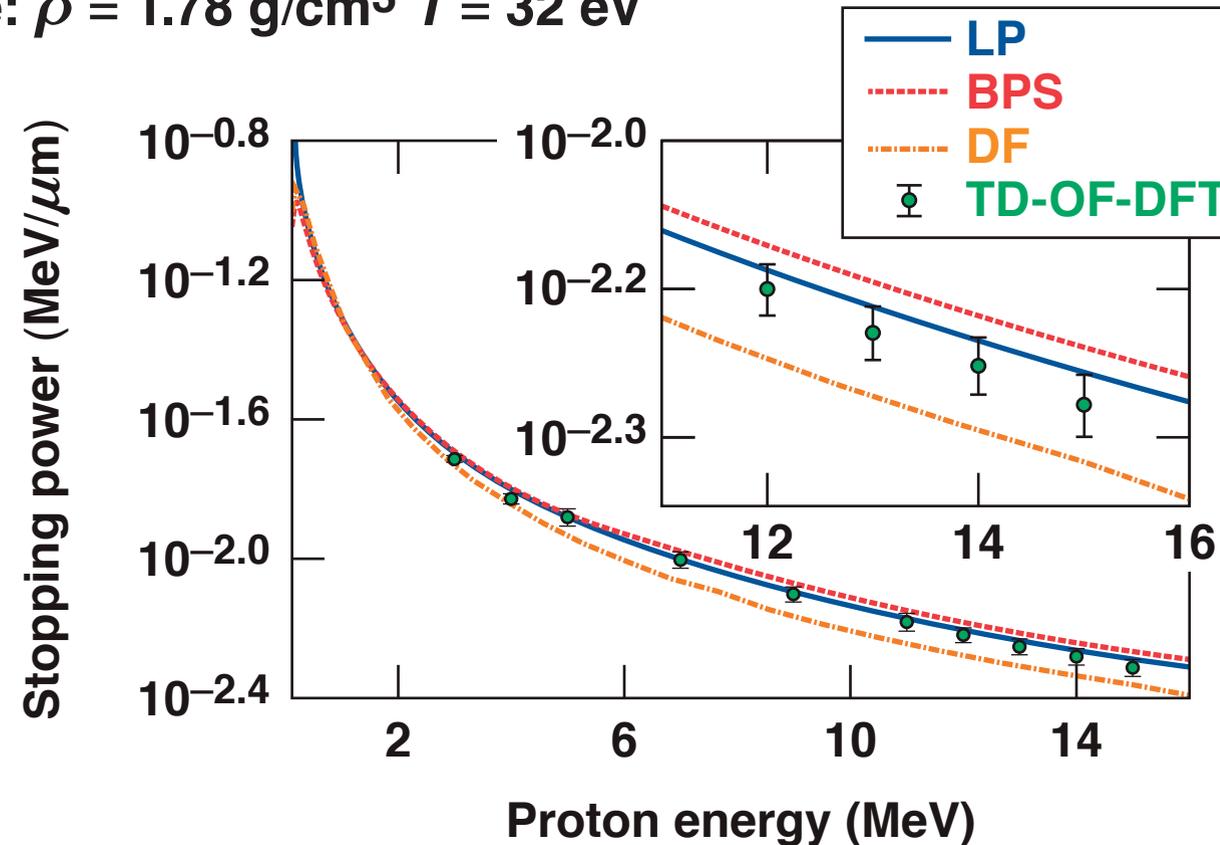
FFT: fast Fourier transform  
IFFT: inverse fast Fourier transform

# We first simulate the recent stopping-power measurement in warm dense Be conducted on OMEGA



# The TD-OF-DFT-calculated proton stopping power in high velocities in comparison with three stopping-power models

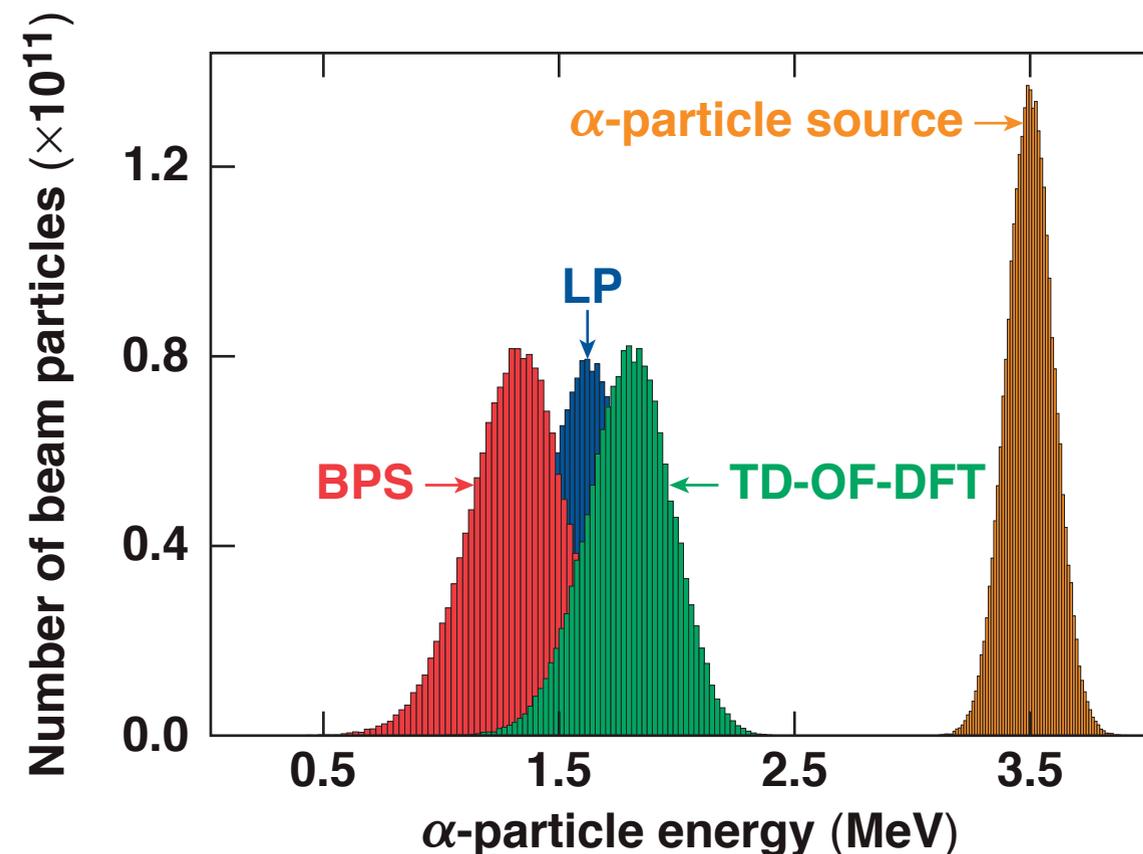
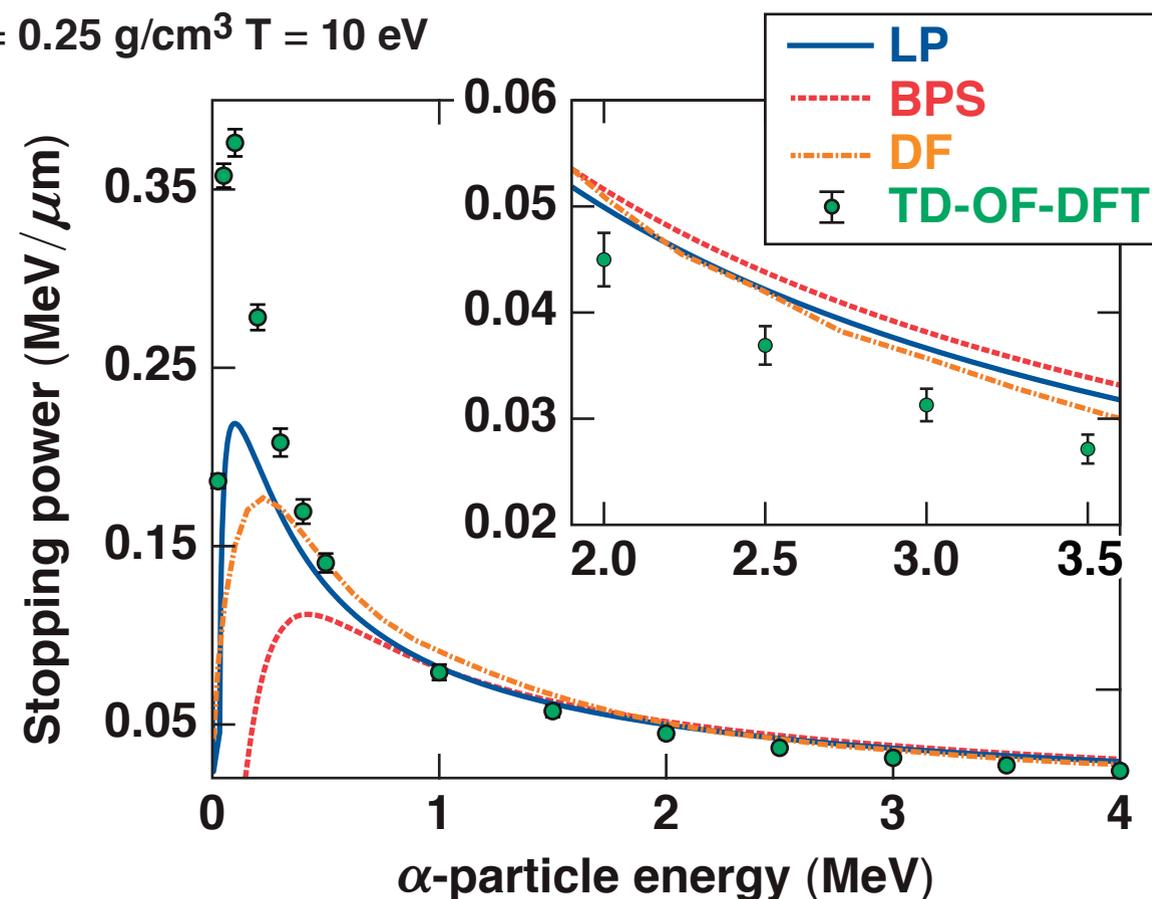
Be:  $\rho = 1.78 \text{ g/cm}^3$   $T = 32 \text{ eV}$



The stopping power calculated by TD-OF-DFT is slightly lower than predictions of the LP and BPS models by  $\sim 5\%$  and  $\sim 11\%$ , respectively, and higher than predicted by DF by 20%.

# TD-OF-DFT calculations indicate that the $\alpha$ -particle stopping power of warm dense DT is less than the LP and BPS models by $\sim 15\%$ to $25\%$ in the ICF-relevant regime

DT:  $\rho = 0.25 \text{ g/cm}^3$   $T = 10 \text{ eV}$



The comparison shows the stopping power from TD-OF-DFT calculations is smaller overall than LP, BPS, and DF models by  $\sim 16\%$ ,  $\sim 25\%$ , and  $15\%$ , respectively. TD-OF-DFT predicts greater stopping from TD-OF-OF-DFT than all the models near the Bragg peak.

# A time-dependent orbital-free density functional theory (TD-OF-DFT) code has been developed for *ab initio* investigations of transport properties of warm dense plasmas

- We have presented a time-dependent orbital-free density-functional-theory formulation to investigate charged-particle stopping power of warm-dense plasmas
- Our comparison to recently measured downshifted spectra of energetic protons passing through the warm dense beryllium plasma agrees to within  $\sim 20$  keV, while the LP and BPS models somewhat overestimated downshift by  $\sim 100$  keV and  $\sim 200$  keV, respectively
- Moreover, our TD-OF-DFT calculations indicate that the  $\alpha$ -particle stopping power of warm dense DT is less than the LP, BPS, and DF models by  $\sim 15\%$  to  $25\%$  in the ICF-relevant regime