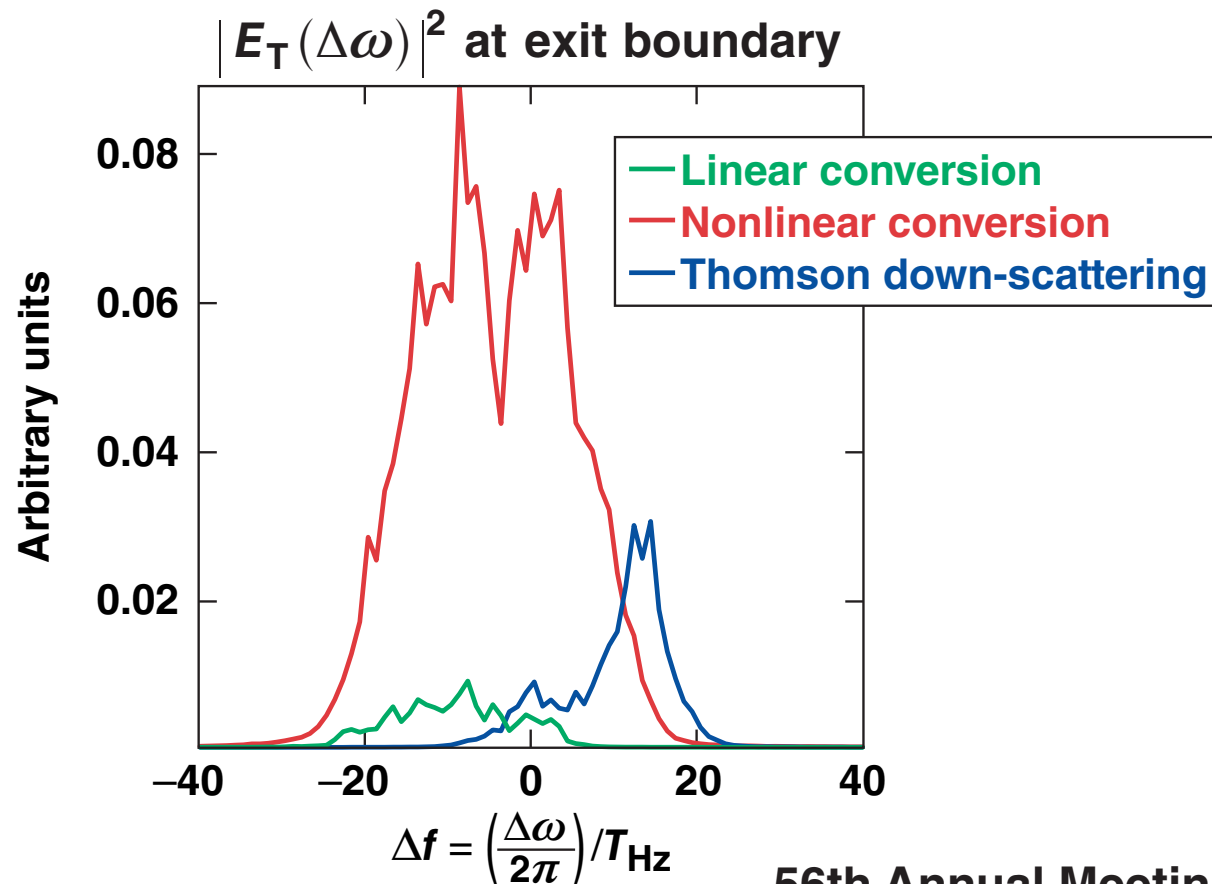


# Calculation of Half-Harmonic Emission Generated by the Two-Plasmon–Decay Instability



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## Summary

# Half-harmonic emission generated by two-plasmon decay (TPD) is calculated with a new code, *EMZAK*



- Half-harmonic emission is one of the few experimental\* observables of TPD
- The Zakharov equations\*\* are expanded to include transverse fields and are solved with a new code
- Half-harmonic emission can be generated by three different mechanisms
  - linear conversion
  - nonlinear conversion
  - Thomson down-scattering

**For the case shown, nonlinear-mode conversion is dominant.**

\* W. Seka *et al.*, Phys. Rev. Lett. **112**, 145001 (2014).

\*\* D. F. DuBois, D. A. Russell, and H. A. Rose, Phys. Rev. Lett. **74**, 3983 (1995);  
D. A. Russell and D. F. DuBois, Phys. Rev. Lett. **86**, 428 (2001);  
J. Zhang *et al.*, Phys. Rev. Lett. **113**, 105001 (2014).

# Collaborators

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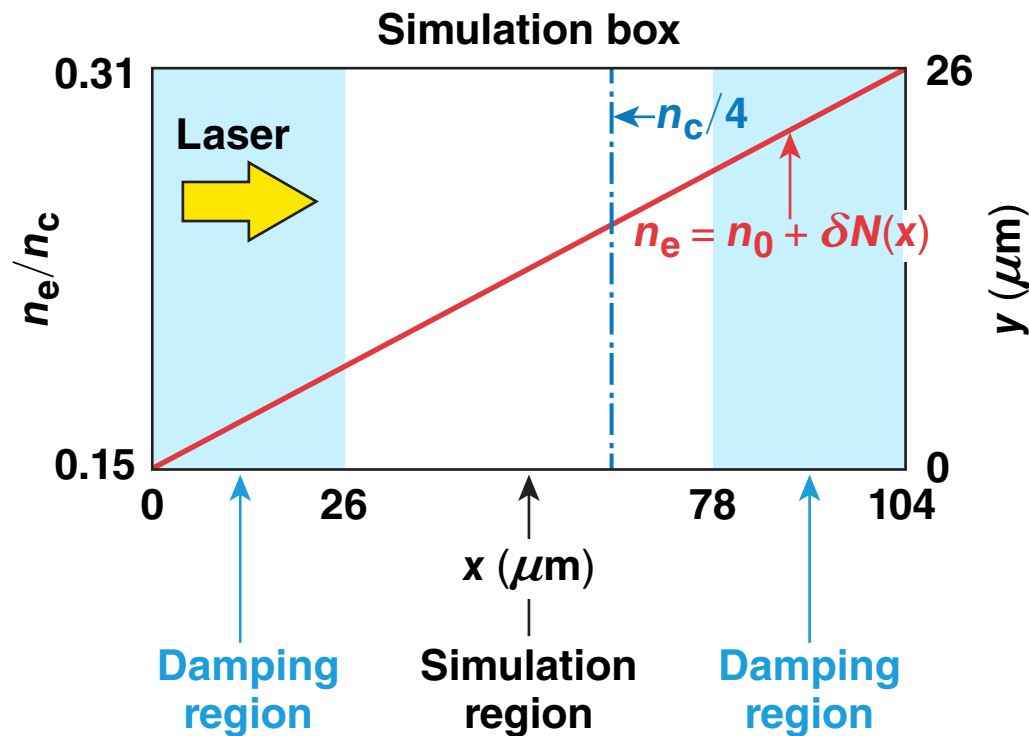
**H. X. Vu**

**University of California, San Diego, CA**

**D. F. DuBois and D. A. Russell**

**Lodestar Research Corporation, Boulder, CO**

# The generation of half-harmonic transverse waves occurs near quarter-critical density where TPD Langmuir waves (LW's) turn



- Parameters are relevant to an OMEGA spherical implosion
- Single laser beam

$$I_{14} = 8; L_n = 150 \mu\text{m};$$

$$T_{e, \text{keV}} = T_{i, \text{keV}} = 2;$$

$$\eta = \frac{L_n \lambda_{\mu\text{m}} I_{14}}{T_{e, \text{keV}}} \approx 2;$$

$$\nu_{ei} = 1.88 \times 10^{-4} \omega_0$$

# The electrostatic Zakharov equations are extended\* to include the transverse field (in 2-D so far)



- Electromagnetic Zakharov equations
  - here  $E = E_L + E_T$  contains both longitudinal and transverse components
    - $\delta N$  density inhomogeneity
    - $\delta n$  density fluctuation

$$\left[ 2i\omega_{pe0} (\mathbf{D}_t + \nu_e) + 3V_{te}^2 (\nabla\nabla \cdot) - c^2 (\nabla \times \nabla \times) - \frac{4\pi e^2}{m_e} (\delta n + \delta N) \right] \vec{E} =$$

$$\frac{e}{4m_e} \underbrace{\left[ \nabla(\vec{E}_0 \cdot \vec{E}^*) - (\nabla \cdot \vec{E}^*) \vec{E}_0 \right]}_{\text{TPD, stimulated Raman scattering (SRS), and Thomson down-scattering (TDS)}} e^{-i\Delta\omega_i t} + \mathbf{S}_E$$

TPD, stimulated Raman scattering (SRS),  
and Thomson down-scattering (TDS)

$$[\mathbf{D}_t^2 + 2\nu_i \cdot \mathbf{D}_t - c_s^2 \nabla^2] \delta n = \frac{\nabla^2 |\mathbf{E}|^2}{16\pi m_i} + \frac{1}{4} \frac{\nabla^2 |\mathbf{E}_0|^2}{16\pi m_i}$$

# EMZAK is able to simulate the three competing half-harmonic-generation mechanisms



$(\delta n \vec{E}_L)_T$ : linear-mode conversion  
(inverse resonance absorption);

$$\omega_T = \omega_L$$
$$(\mathbf{k}_T)_\perp = (\mathbf{k}_L)_\perp$$

$(\delta n \vec{E}_L)_T$ : nonlinear-mode conversion;

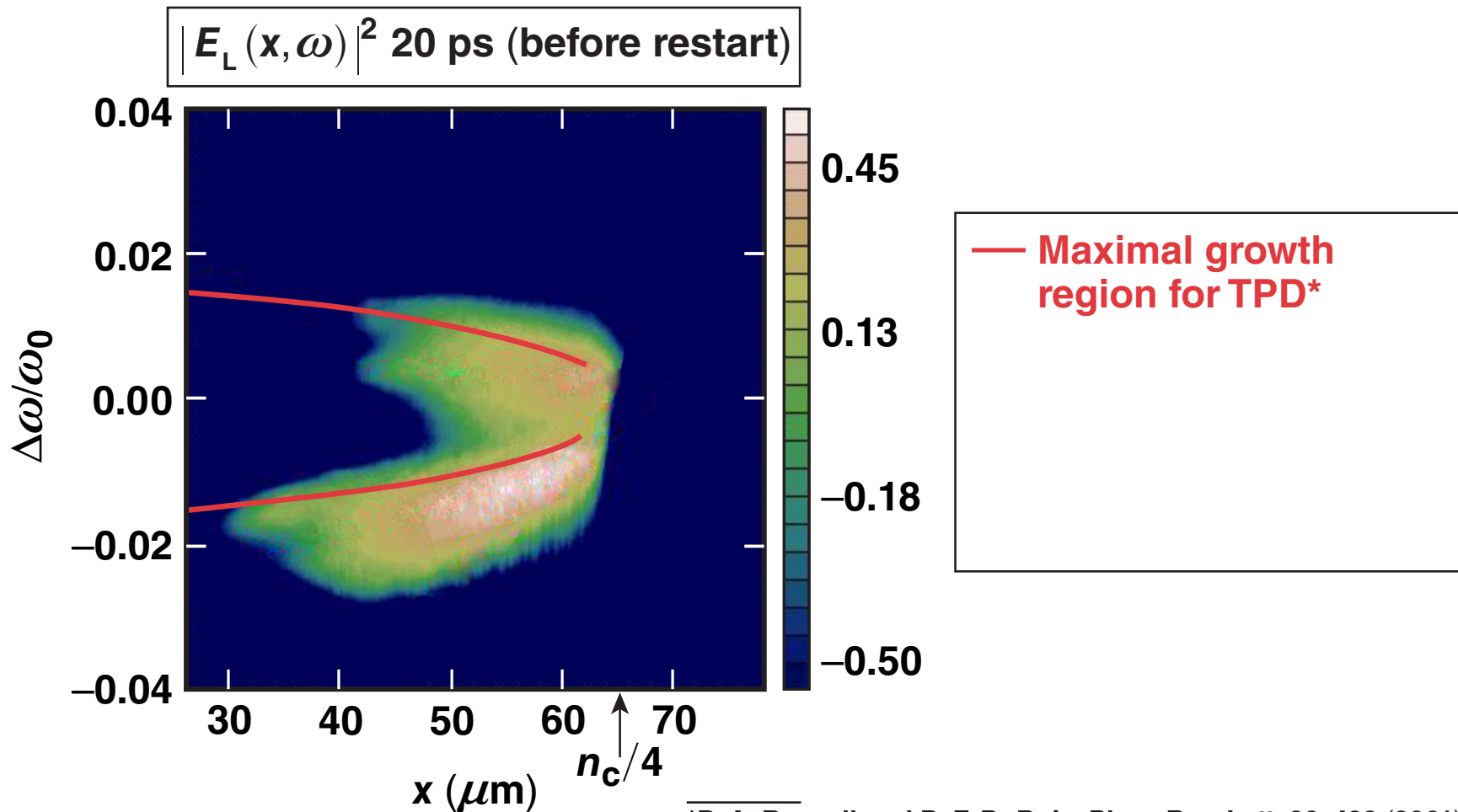
$$\omega_T \approx \omega_L$$
$$\mathbf{k}_T = \mathbf{k}_{IAW} + \mathbf{k}_L$$

$[(\nabla \cdot \vec{E}^*) \vec{E}_0]_T$ : Thomson down-scattering;

$$\omega_T = \omega_0 - \omega_L$$
$$\mathbf{k}_T = \mathbf{k}_0 - \mathbf{k}_L$$

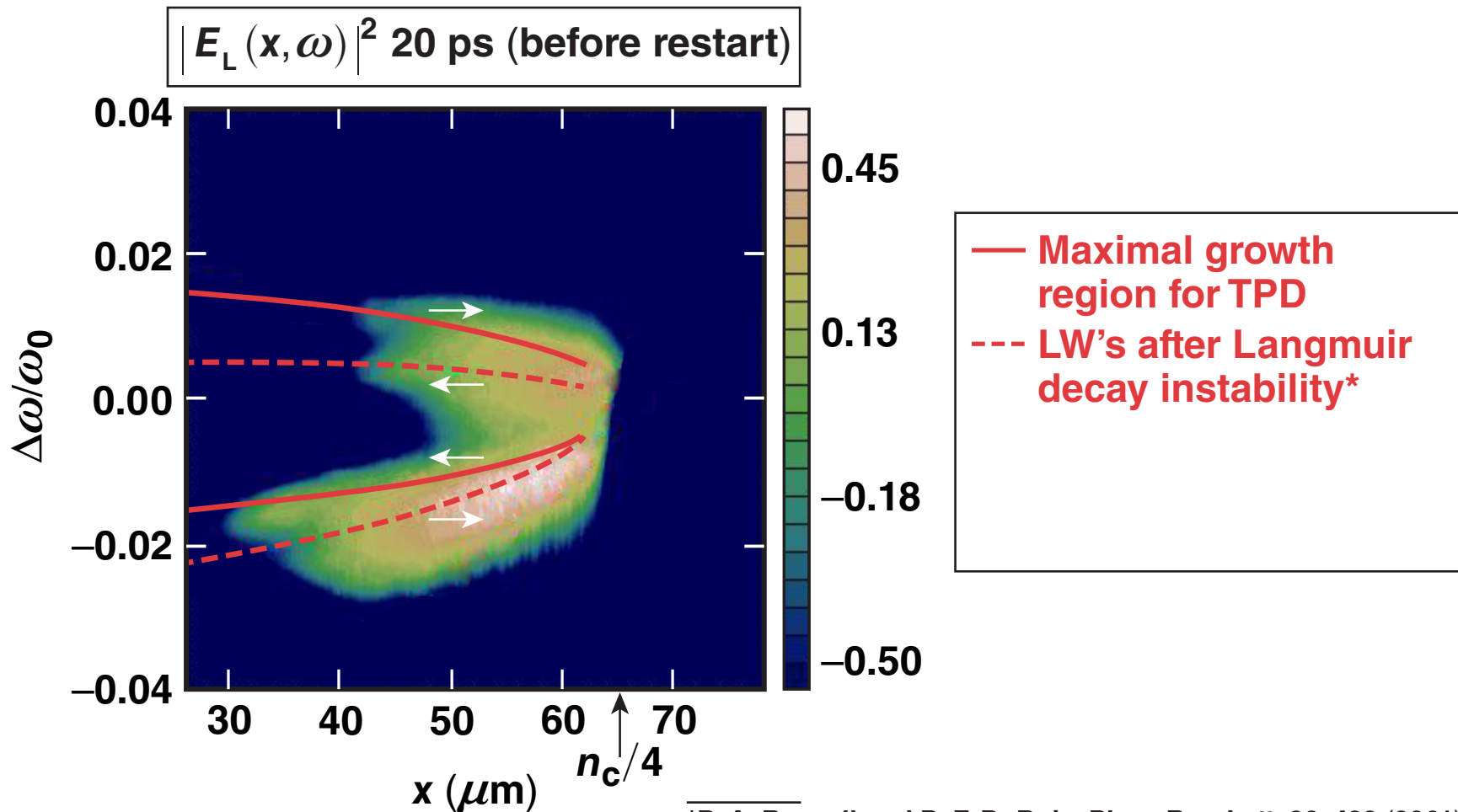
# The simulation is first run without coupling to transverse fields to obtain the saturation stage of TPD

$$|E_L(x, \omega)|^2 = \left( \int \left| \int E_L(x, y) e^{i\omega t} dt \right| dy \right)^2; \Delta\omega = \omega - \omega_0/2$$



# The wave spectrum shows strong signatures of the Langmuir wave decay instability

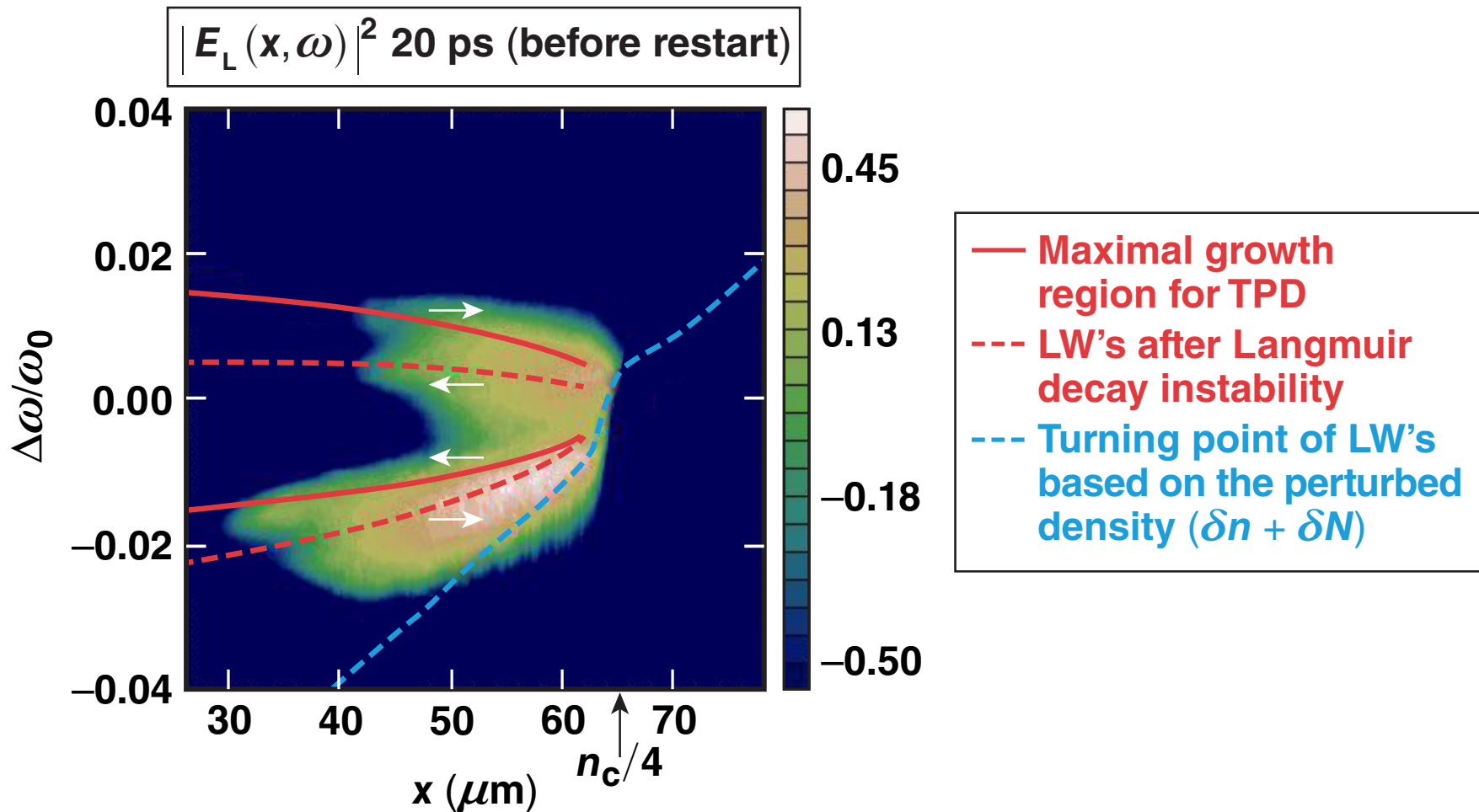
$$|E_L(x, \omega)|^2 = \left( \int \left| \int E_L(x, y) e^{i\omega t} dt \right| dy \right)^2; \Delta\omega = \omega - \omega_0/2$$





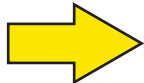
# The frequency spectrum of LW's at their turning points can be determined

$$|E_L(x, \omega)|^2 = \left( \int \left| \int E_L(x, y) e^{i\omega t} dt \right| dy \right)^2; \Delta\omega = \omega - \omega_0/2$$



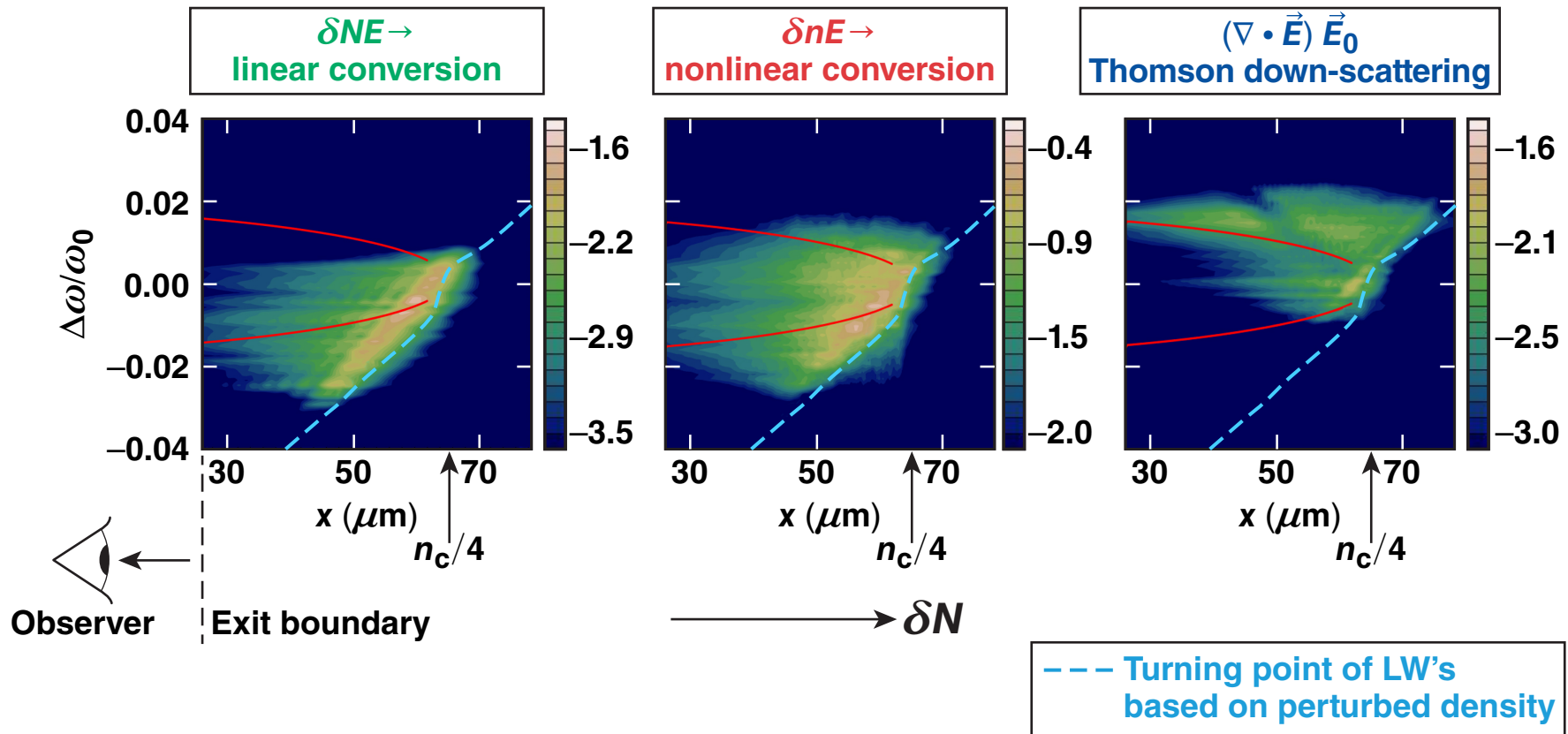
# The simulation is restarted with coupling to the half-harmonic emission enabled

Laser

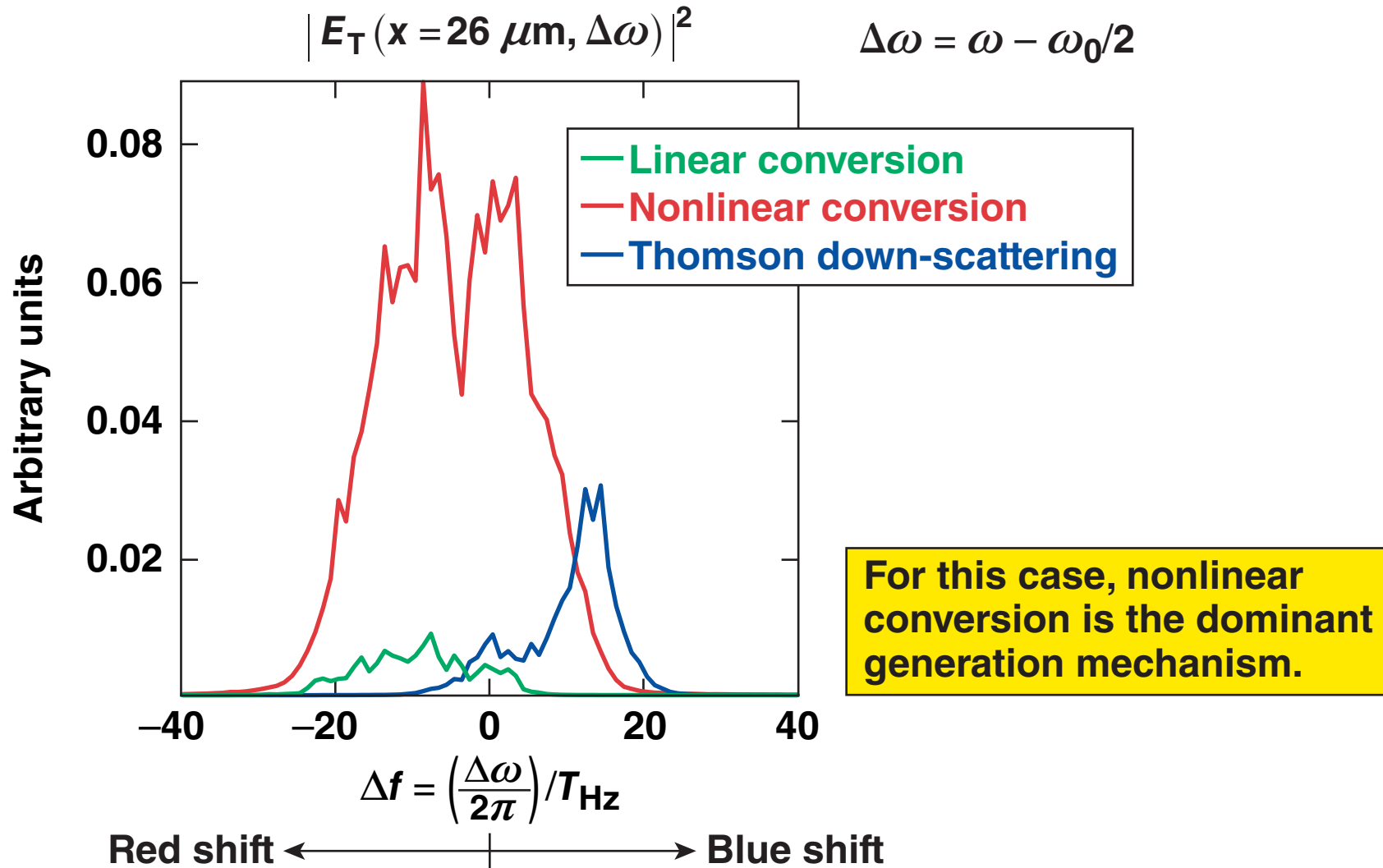


$$|E_T(x, \omega)|^2 \text{ 1 ps (after restart)}$$

$$\Delta\omega = \omega - \omega_0/2$$



# The half-harmonic emission is collected at the left (exit) boundary



# More conclusions can be inferred through manipulating some parameters



- Incorporating all three sources in a single run, half-harmonic emission is the sum of the three shown in the previous slide, indicating that the three sources act independently
- In another set of simulations with smaller collisional damping, the level of half-harmonic emission is higher; the reason is that more LW's are able to propagate to the turning point and convert to half-harmonic light

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