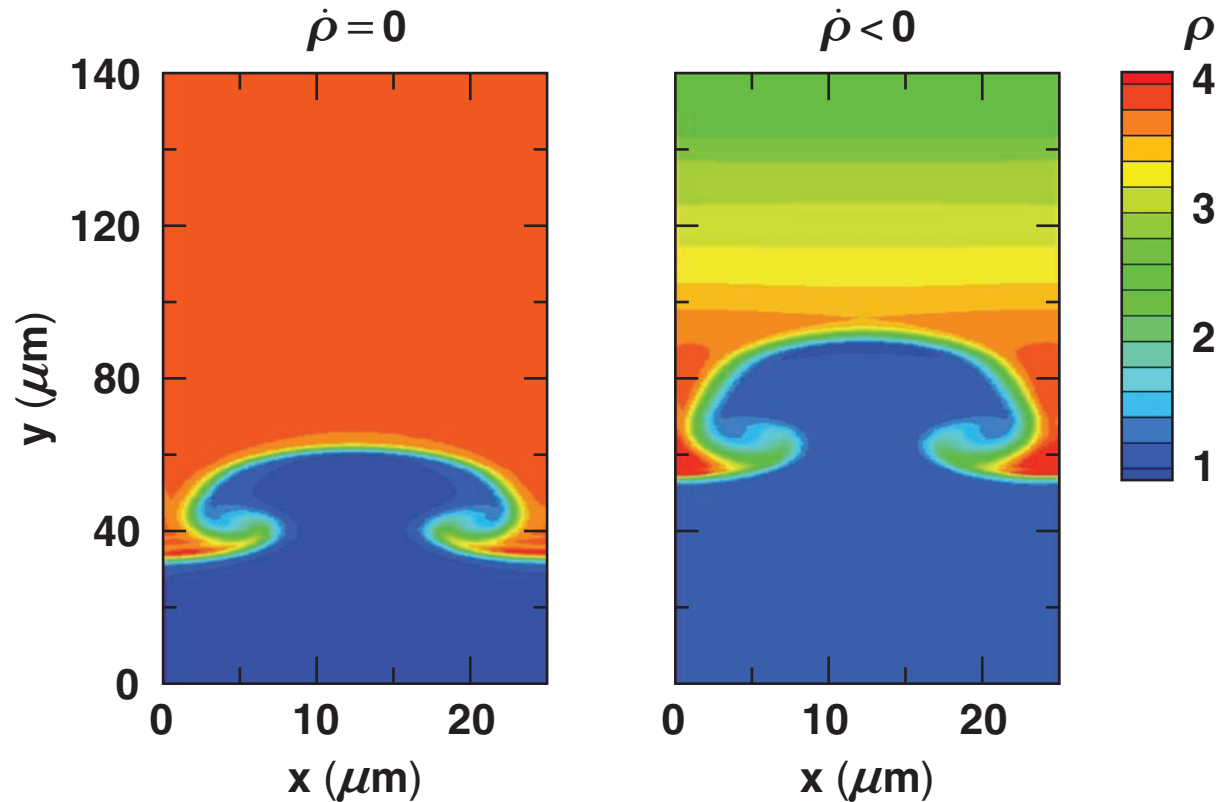


# Numerical Study of Temporal Density Variation on Nonlinear Evolution of Classical Rayleigh–Taylor Instability



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## Summary

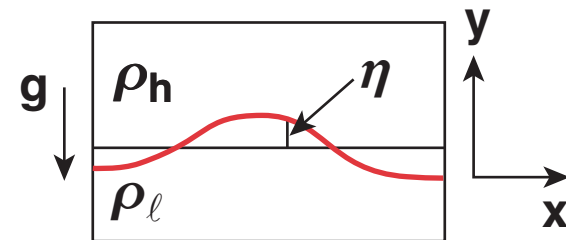
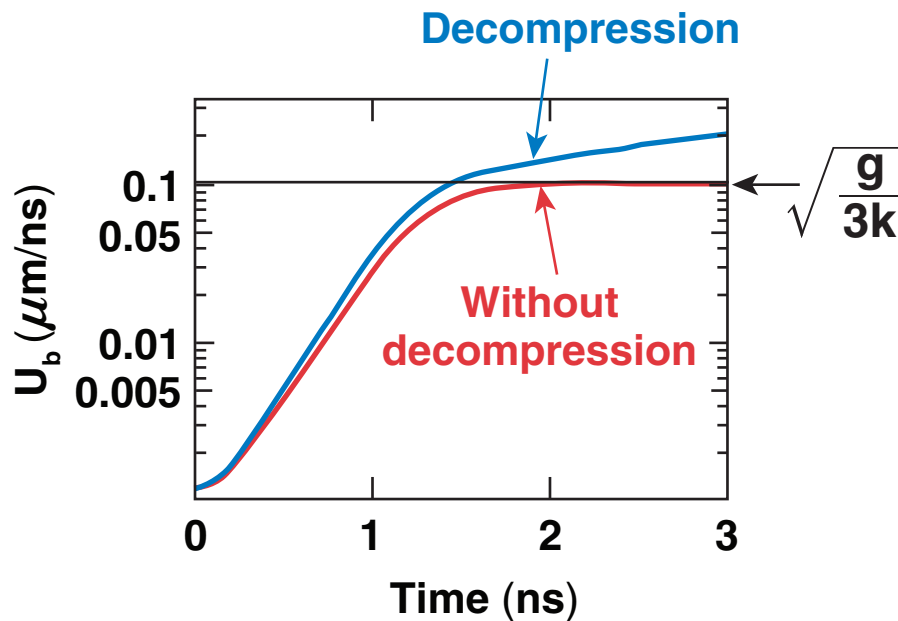
# The results of the Layzer-type model with time-dependent density have been validated with a 2-D simulation

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- Temporal density variation is important in ICF implosion.
- Layzer's model is extended to include the density variation in planar and spherical geometry.
- A 2-D Eulerian code has been developed to test the results of the model.
- Decompression increases asymptotic bubble velocity.
- The saturated bubble curvature is independent of the Atwood number.

# Density variation can be easily included in Layzer's model\*



$$\mathbf{U} = \nabla \Phi$$

$$\nabla^2 \Phi = -\frac{\dot{\rho}}{\rho}$$

$$\Phi = a(t) \cos(kx) e^{-k(y-\eta_0)} - \frac{\dot{\rho}}{\rho} \frac{y^2}{2}$$

$$\eta = \eta_0 + \eta_2 x^2$$

$$\eta_0 \xrightarrow{t \rightarrow \infty} \sqrt{\frac{g}{3k}} \frac{\int \rho(t') dt'}{\rho(t)}$$

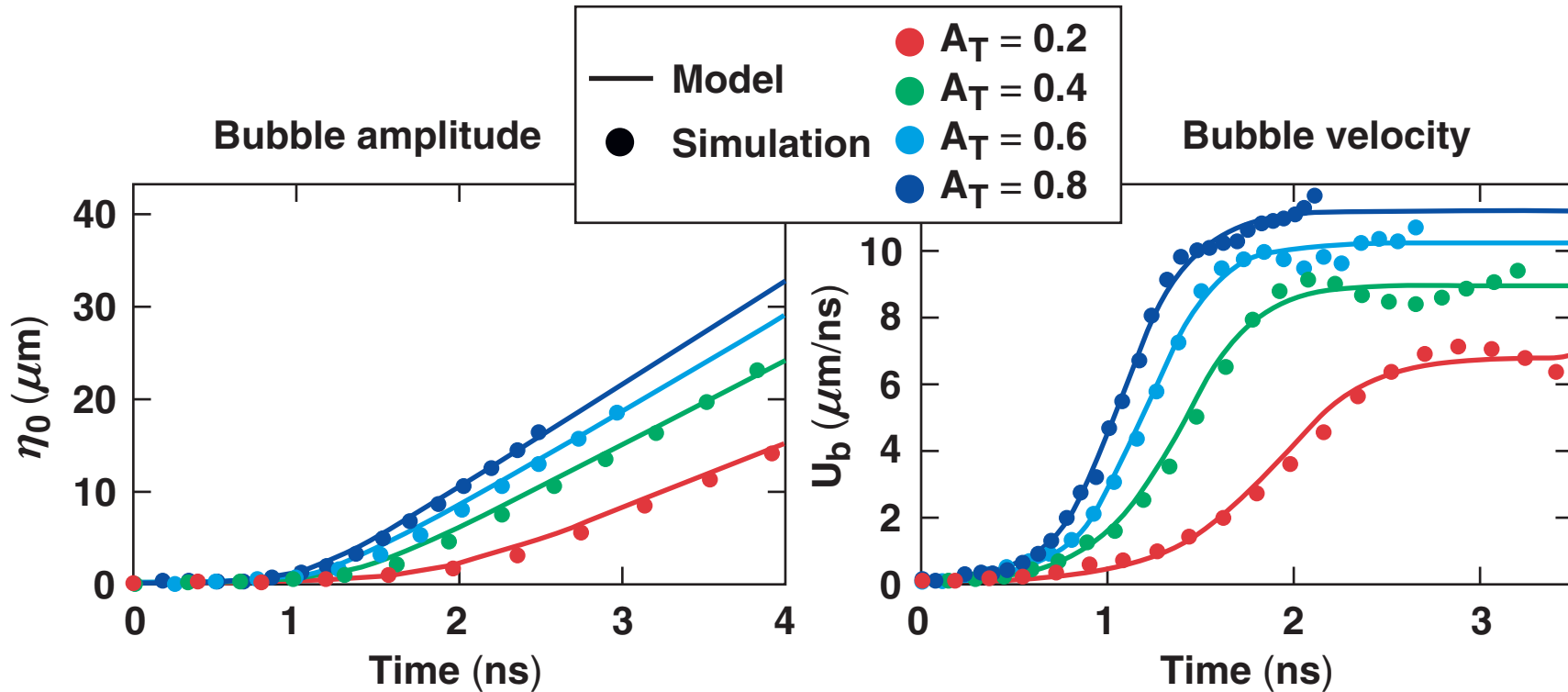
# A 2-D Eulerian code was developed to test the decompression effects

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- A two-dimensional MacCormack's method is used to solve Euler equations.
- Artificial viscosity is introduced in momentum equations and artificial heat flux in the energy equation.
- Periodic boundary conditions are applied on the left and right sides.
- Continuous boundary conditions are applied on the upper and lower borders.

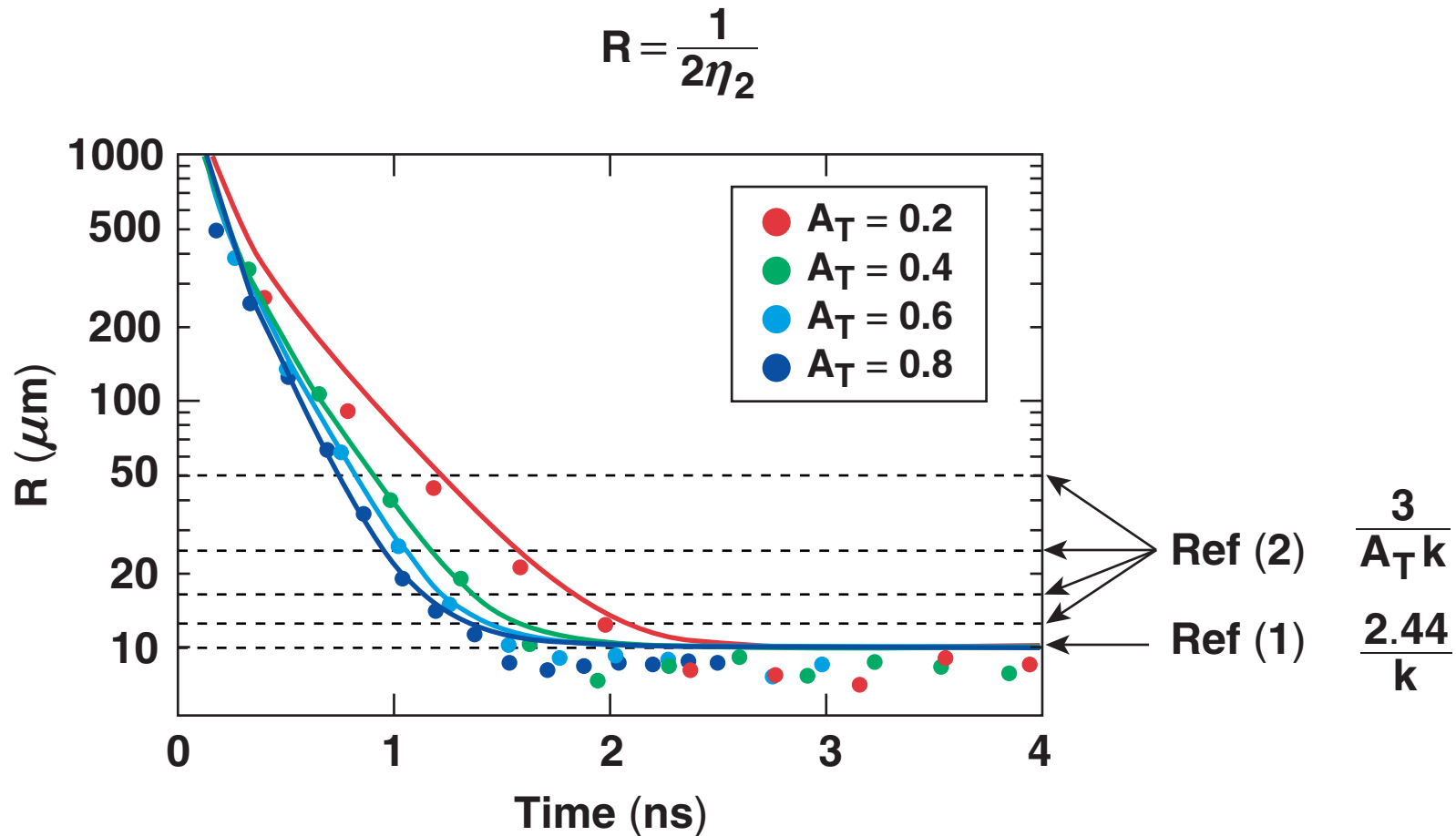
# The code was tested against a Layzer-type solution with constant density\*



$$\begin{aligned} \eta_0(0) &= 0.0 \mu\text{m} \\ \dot{\eta}_0(0) &= 0.2 \mu\text{m/ns} \\ g &= 100 \mu\text{m/ns}^2 \\ \lambda &= 25 \mu\text{m} \end{aligned}$$

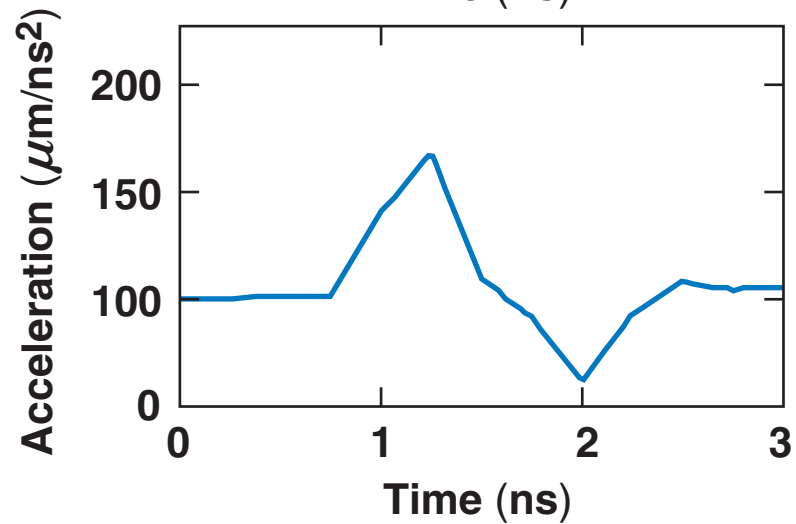
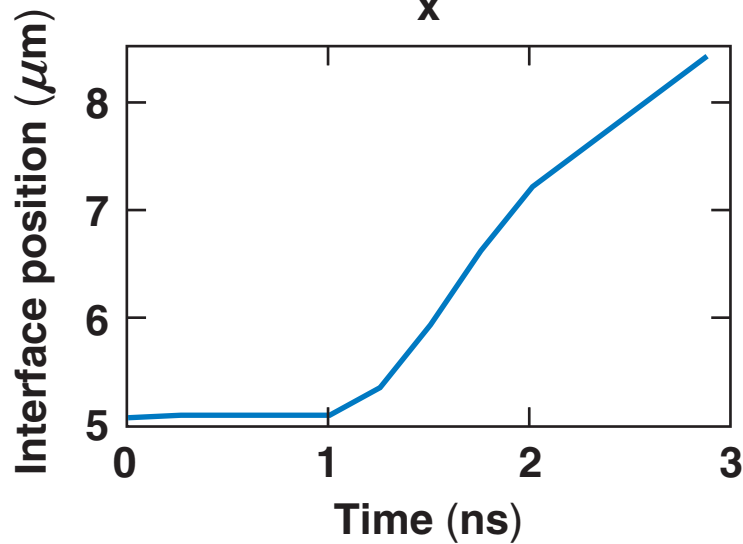
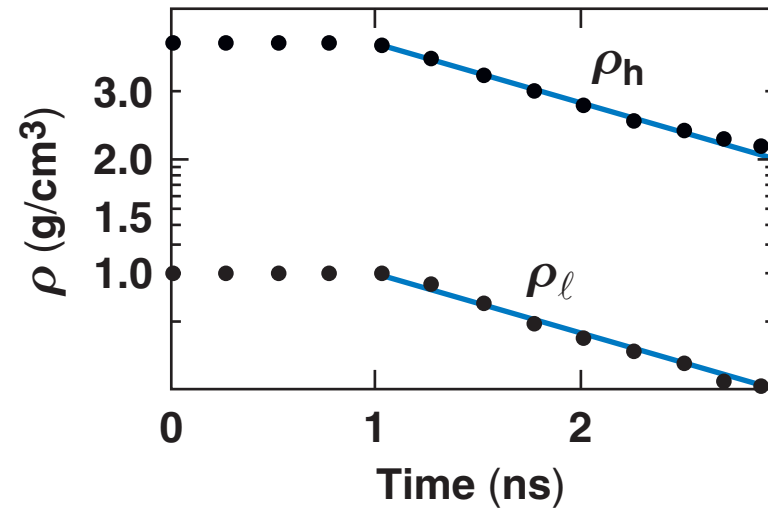
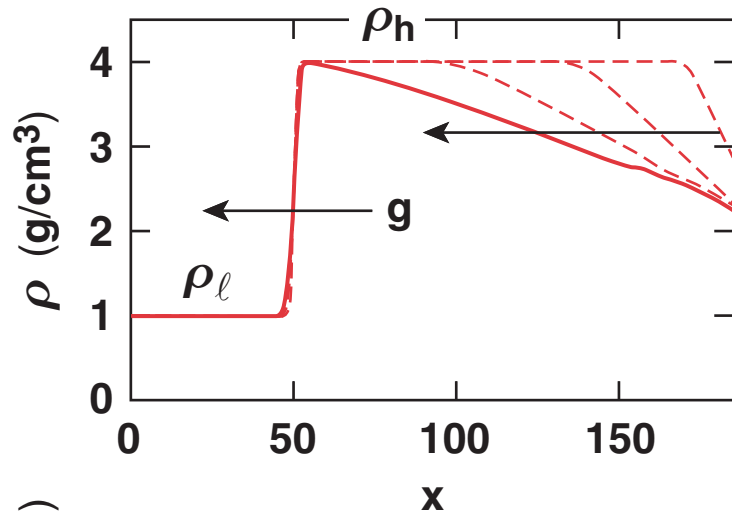
$$A_T = \frac{\rho_h - \rho_\ell}{\rho_h + \rho_\ell} \quad U_b \rightarrow \sqrt{\frac{2A_T}{1 + A_T} \frac{g}{3k}}$$

# The saturated bubble curvature is independent of Atwood numbers<sup>1</sup>



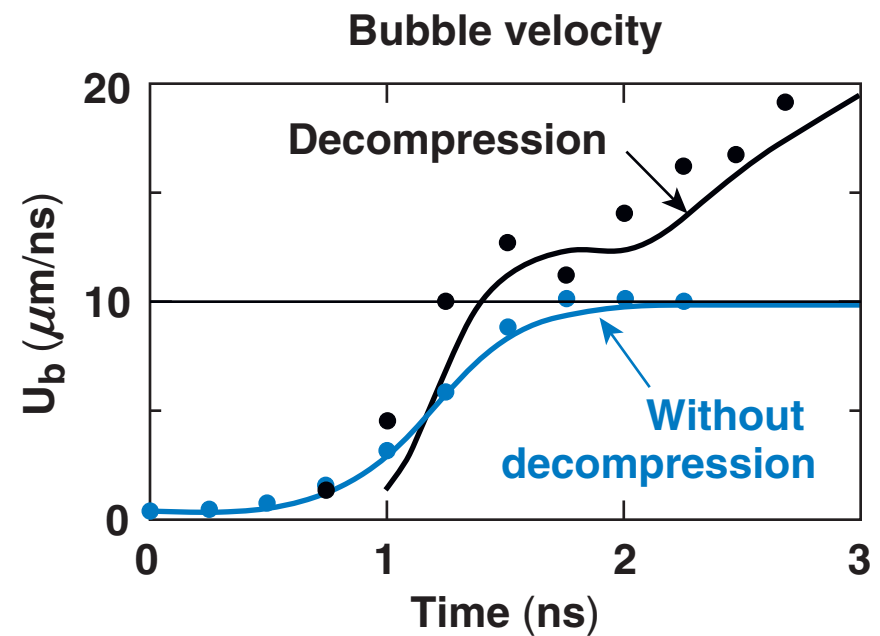
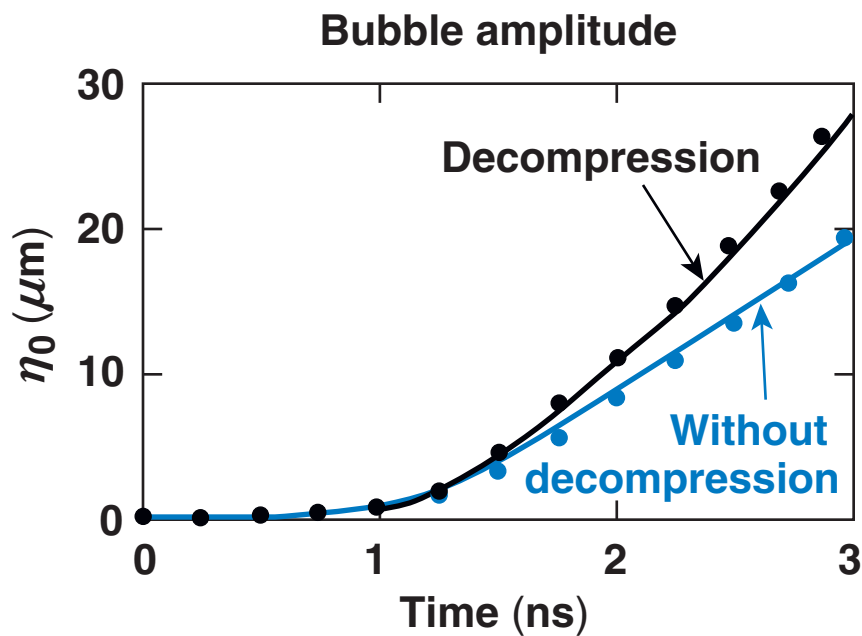
<sup>1</sup> V.N. Goncharov, Phys. Rev. Lett. **88**, 4502 (2002).  
<sup>2</sup> S. I. Abarzhi *et al.*, Phys. Lett. A **317**, 470 (2003).

# Decompression is imposed by launching a rarefaction wave



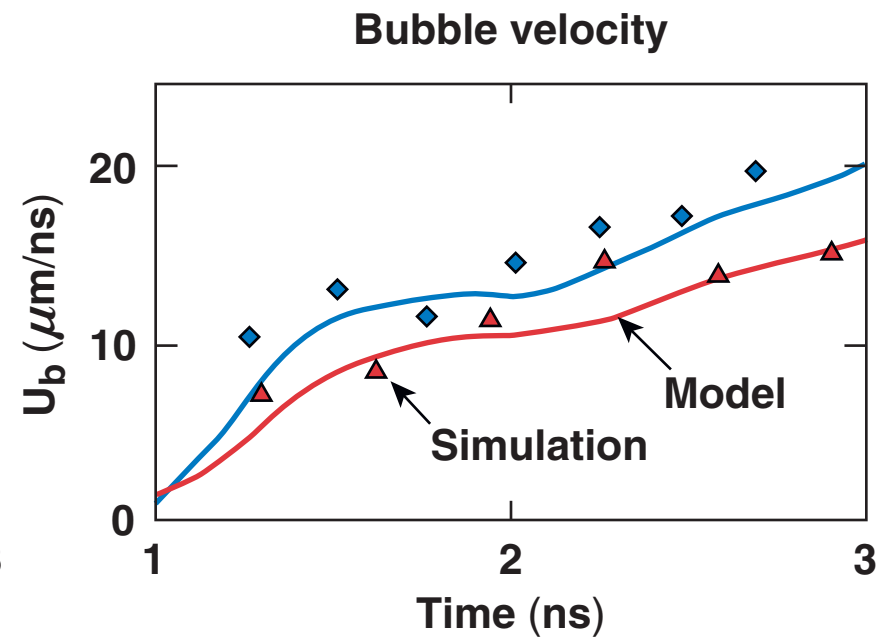
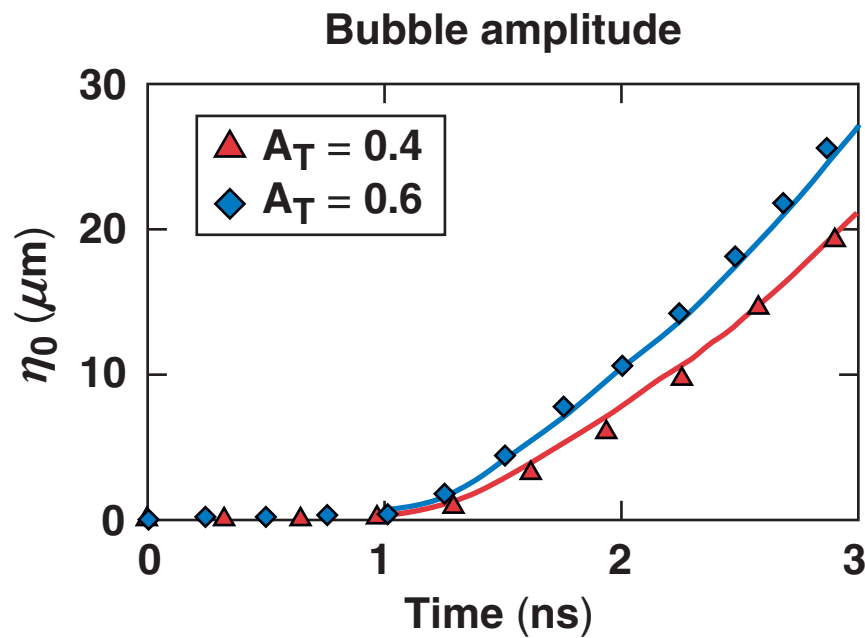
# Decompression increases the asymptotic bubble velocity

$$A_T = 0.4, \lambda = 25 \mu\text{m}$$

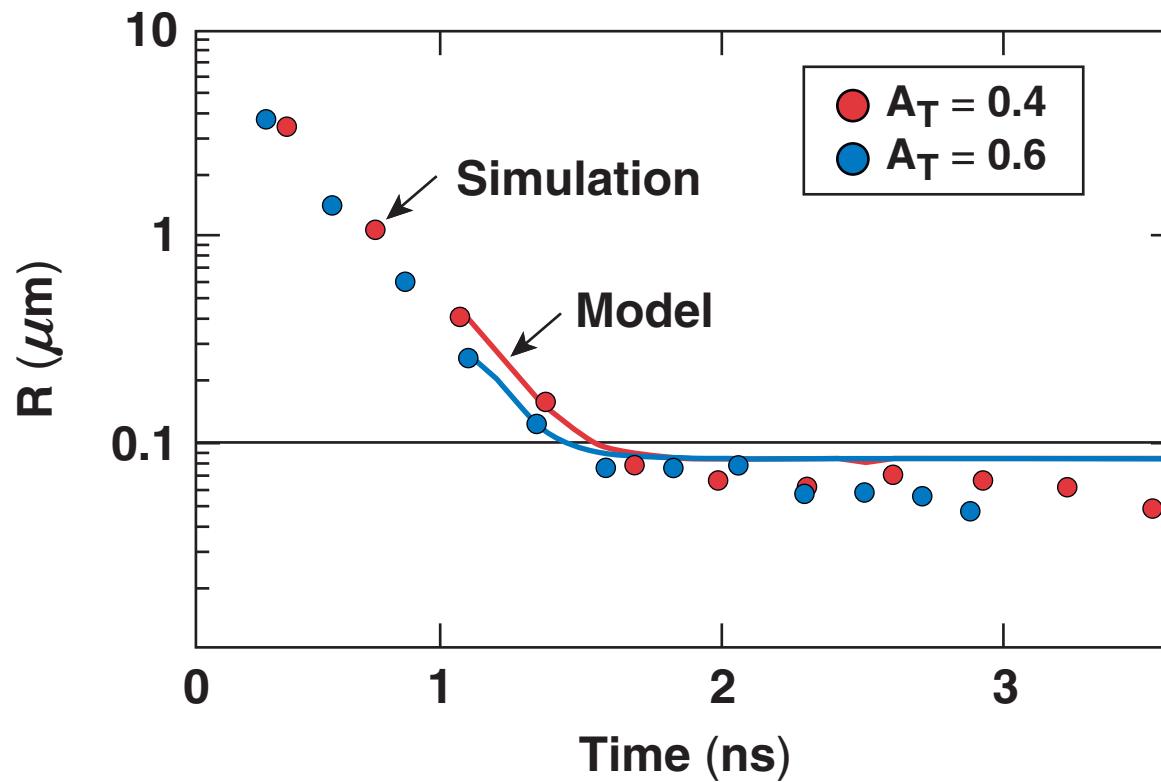




# The Layzer-type model with decompression is in good agreement with simulations for different Atwood numbers



# The saturated bubble curvature is independent of the Atwood number for time-dependent density



# **The results of the Layzer-type model with time-dependent density have been validated with a 2-D simulation**



- **Temporal density variation is important in ICF implosion.**
- **Layzer's model is extended to include the density variation in planar and spherical geometry.**
- **A 2-D Eulerian code has been developed to test the results of the model.**
- **Decompression increases asymptotic bubble velocity.**
- **The saturated bubble curvature is independent of the Atwood number.**