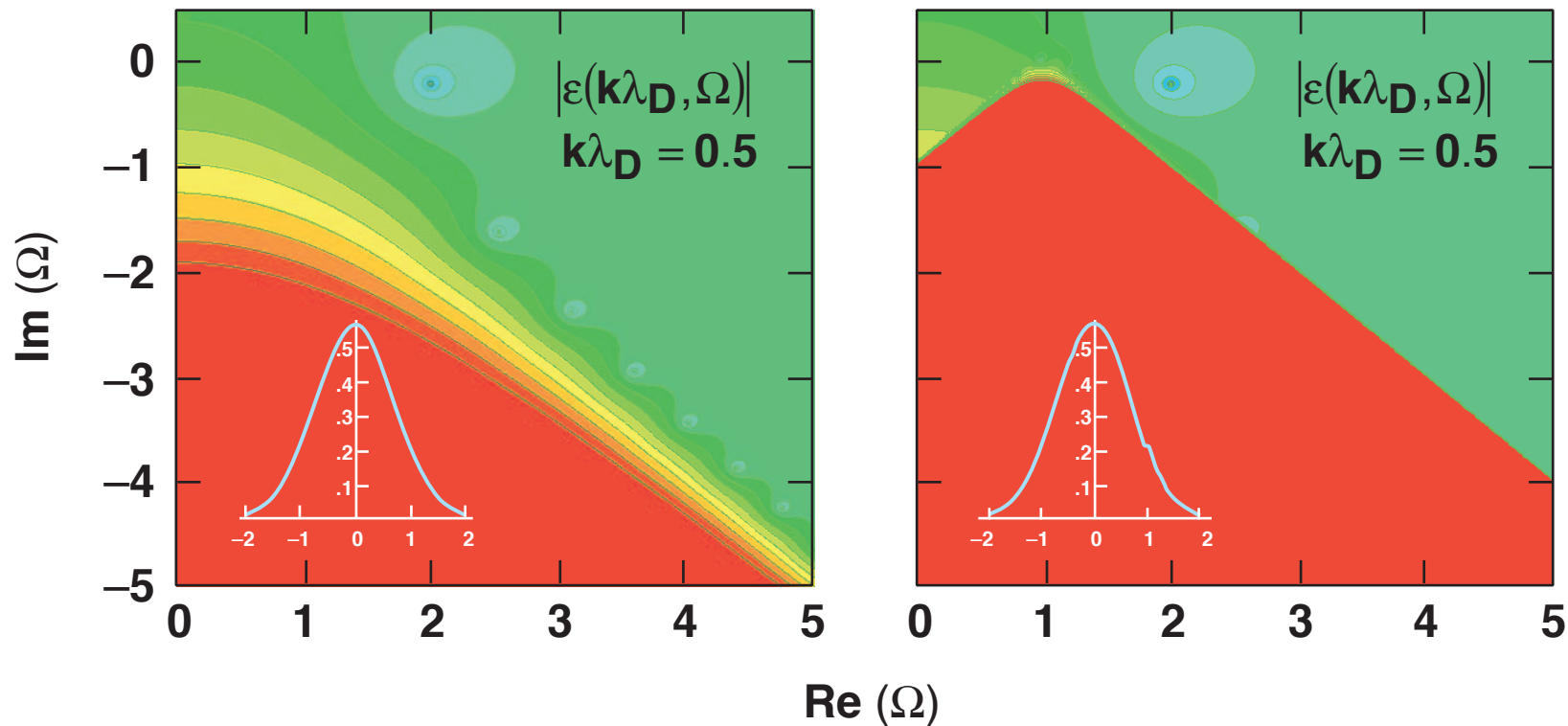


# On the Role of Electron-Acoustic Waves in Two-Plasmon Decay and Stimulated Raman Scattering



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## Summary

# A model based on electron-acoustic waves can account for otherwise enigmatic features of both TPD and SRS



- Why does the level of TPD activity depend on overlapped rather than single-beam intensities?
- Why does TPD respect the “Landau limit” on plasmon wave vector, while SRS does not?
- These observations imply the existence of plasma modes not described by the Bohm–Gross or Maxwellian Landau dispersion relations; electron acoustic waves provide this “missing link.”

# Outline

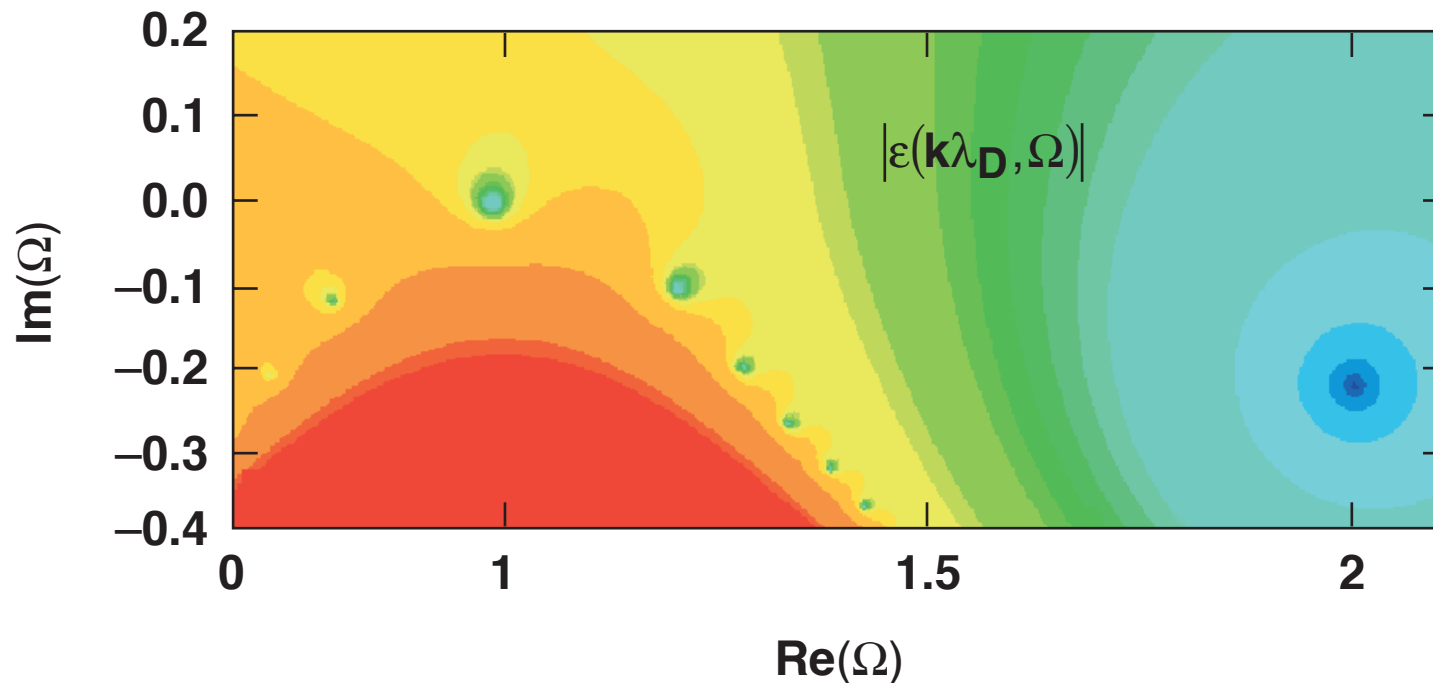
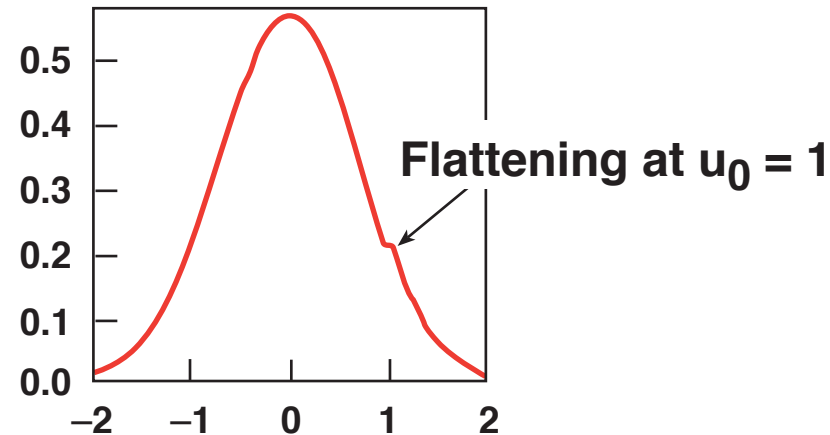
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- **Review of electron-acoustic (EA) waves and their relation to locally-flattened distribution functions.**
- **Role of local flattening in SRS compared to SEAS.**
- **Role of local flattening and EA waves in TPD.**
- **Summary and conclusions.**

# A localized flattening of the distribution function introduces a new linear family of modes

$$k\lambda_D = 0.5$$

$$\Omega \equiv \frac{\omega}{\sqrt{2} k v_T}$$

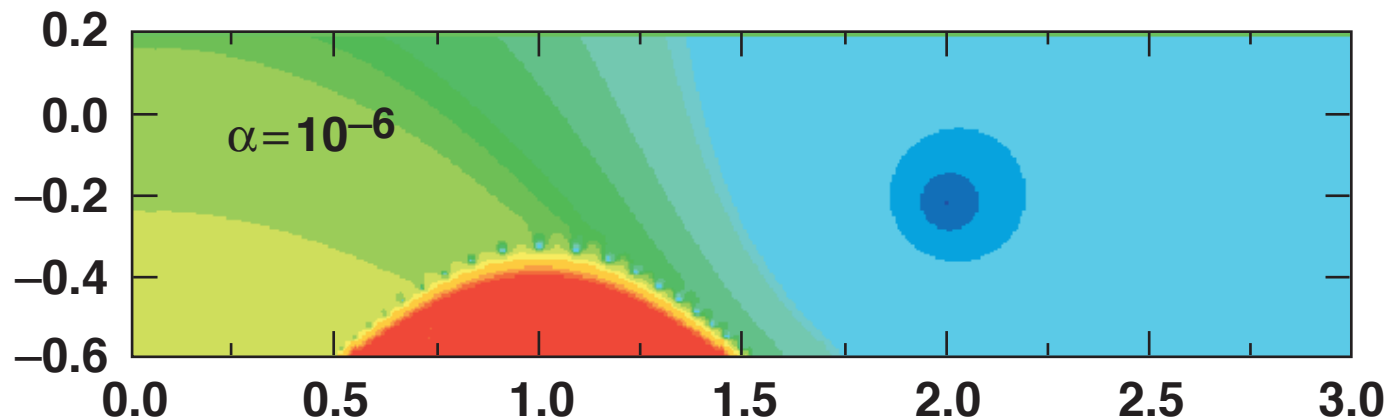


# Even minuscule deviations from a Maxwellian introduce new moderately-damped modes

- Local flattening is modeled by adding a localized term to a Maxwellian:

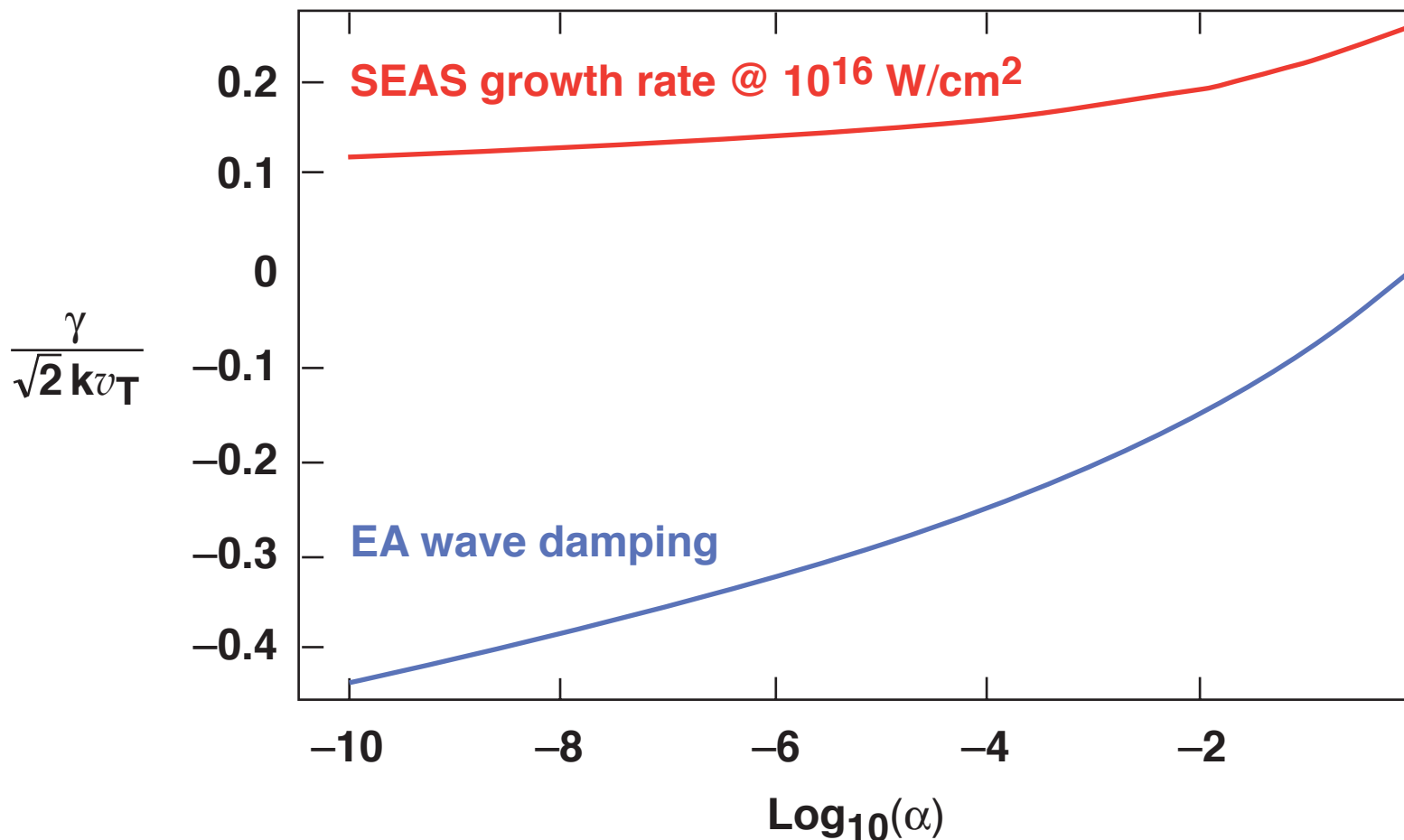
$$f(u) = \frac{1}{\sqrt{\pi}} e^{-u^2} - \alpha f'_0(u_0)(u - u_0) e^{-\frac{(u-u_0)^2}{(\Delta u)^2}}; \alpha = 1 \text{ gives } f(u_0) = 0.$$

- $\text{Re}[\varepsilon(\Omega = u_0, k\lambda_D)] = 0$  is the dispersion relation for electron-acoustic waves, for  $\alpha = 1$  these are undamped.
- Even at small values of the flattening parameter  $\alpha$ , new moderately damped linear modes appear.



# In SEAS, flattening develops from Landau damping of incoherent noise amplified by the pump

- Since the electromagnetic scattered wave has very low damping, the threshold for SEAS growth is exceeded even for small  $\alpha$ .



# The evolution of the flattening is described by diffusion in velocity space

- Temporal evolution of the distribution function:

$$\frac{\partial f}{\partial t} = \frac{\partial}{\partial \mathbf{p}_\alpha} \left( \mathbf{D}_{\alpha\beta} \frac{\partial f}{\partial \mathbf{p}_\beta} \right),$$

where  $\mathbf{D}_{\alpha\beta}(\mathbf{p}) = 2\pi e^2 \int_{\mathbf{k} \approx \mathbf{k}_{\text{res}}} (\mathbf{E}^2)_{\mathbf{k}} \frac{\mathbf{k}_\alpha \mathbf{k}_\beta}{k^2} \delta(\omega - \mathbf{k} \cdot \mathbf{v}) \frac{d^3 \mathbf{k}}{(2\pi)^3}$

and  $(\mathbf{E}^2)_{\mathbf{k}}$  is the power spectrum of linear EA waves.

- An initial slight flattening near the resonance for scattering results in growth of waves satisfying the matching condition, an enhanced diffusion coefficient, and further localized flattening.
- For small  $\alpha$ , energy is transferred from the waves to  $f(\mathbf{u})$  at the Landau damping rate, and the flattening time is

$$\tau_{\text{fl}} \sim (\Delta \mathbf{u})^3 / \nu_{\text{L}};$$

collisional diffusion tends to restore the Maxwellian on a timescale

$$\sim (\Delta \mathbf{u})^2 / \nu_{\text{coll}}.$$

# In the case of SRS, local flattening arises from damping of the amplified Landau mode

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- **SRS is often observed from plasma waves with large  $k\lambda_D$ . In a Maxwellian plasma, Landau damping would greatly reduce the growth of such modes.**
- **As in the SEAS case, incoherent noise with frequencies and wave vectors near the matching condition is amplified and results in local flattening and increased growth.**
- **Noise levels are larger near the Landau resonance, so SRS starts from a larger seed than SEAS; consequently, SRS levels are much larger.**



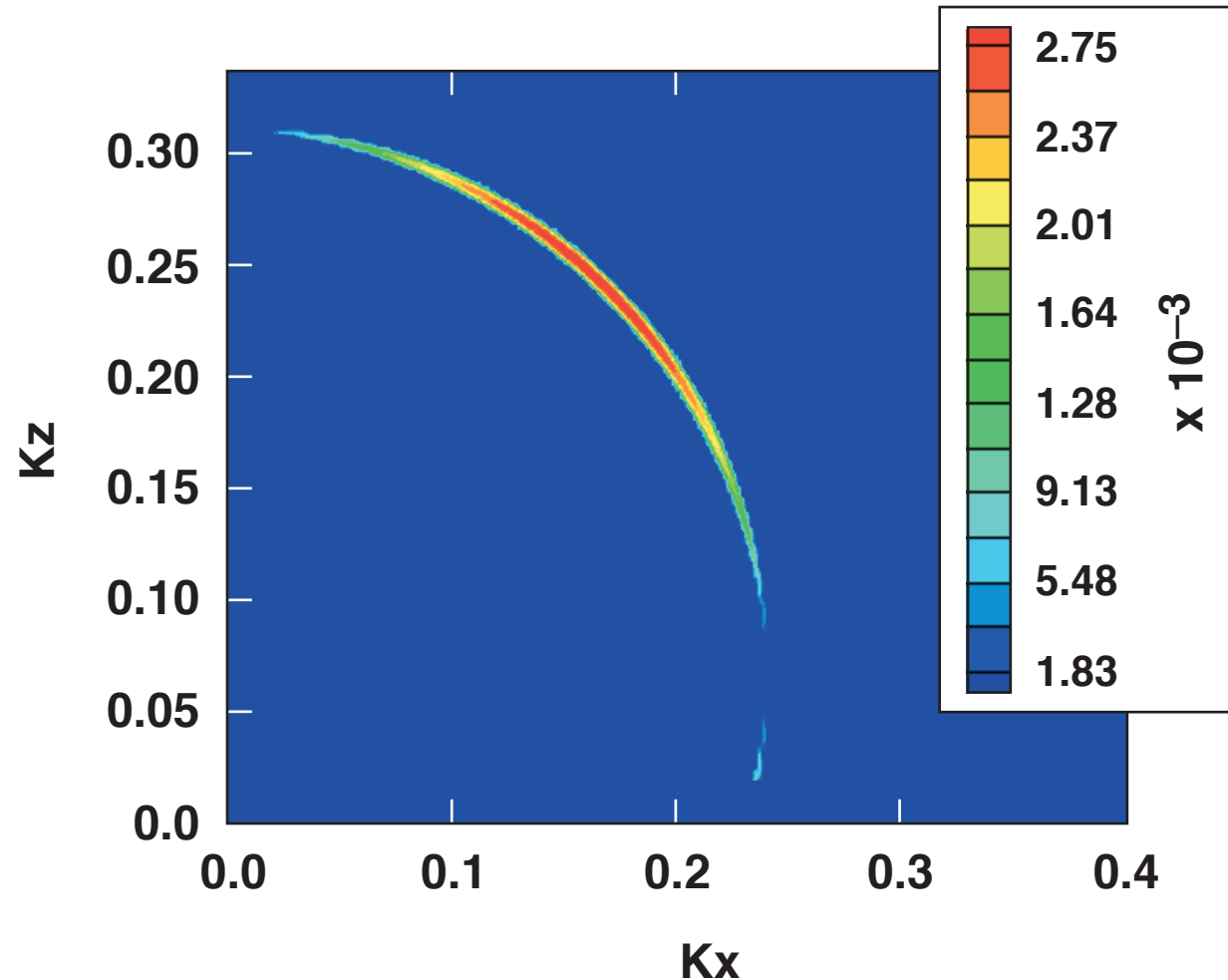
# At moderate intensities, the range of plasmon wave vectors driven by TPD is narrow

- Growth rate  $\gamma/\omega_p$  for single pump at  $5 \times 10^{14} \text{ W/cm}^2$

$$n/n_c = 0.21$$

$$T_e = 2.5 \text{ keV}$$

$$k_0 \lambda_D \cong 0.12$$



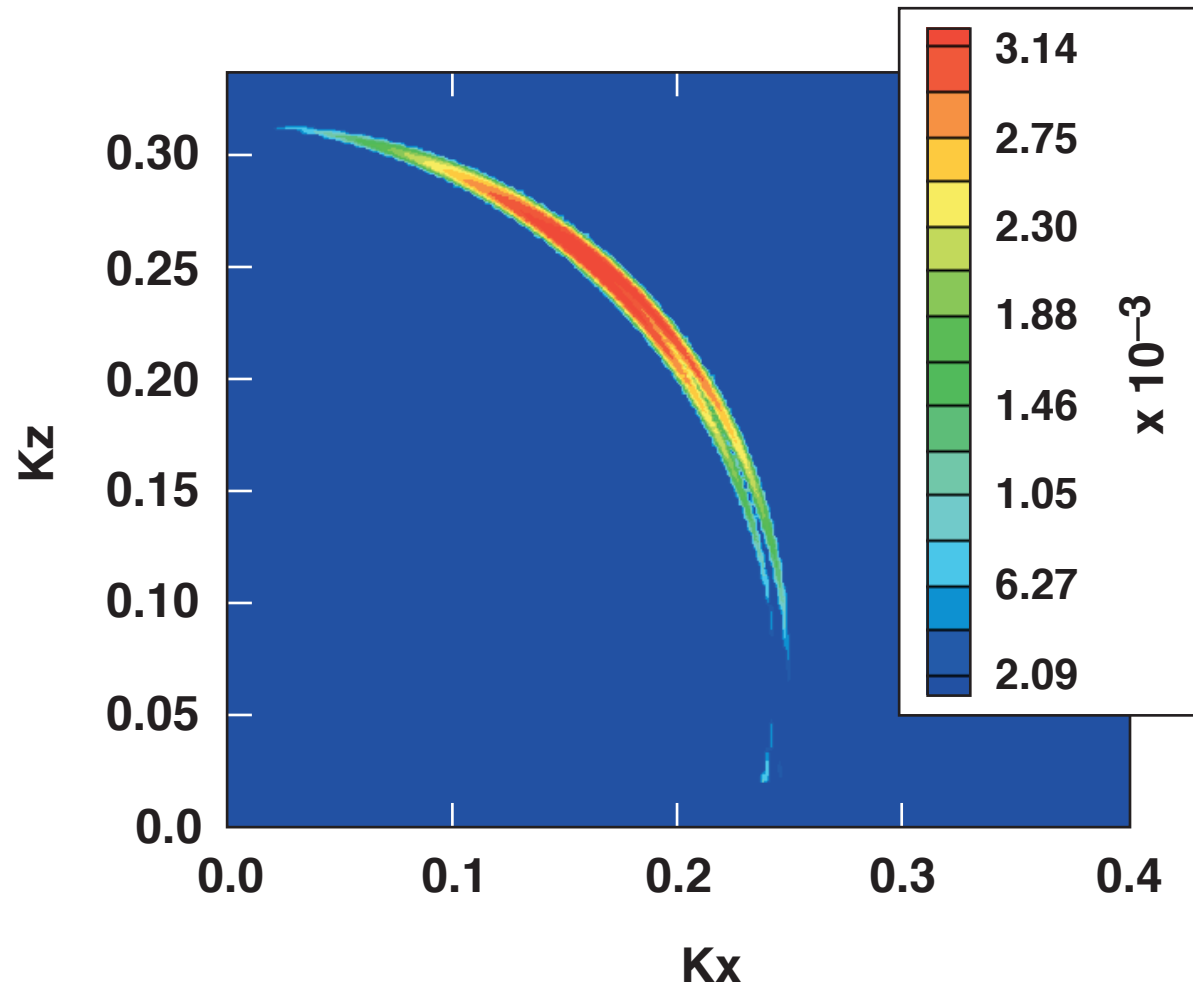
# Even at only $5^\circ$ separation there is little enhancement of the single-beam growth rate

- Growth rate  $\gamma/\omega_p$  for two pumps, each  $5 \times 10^{14} \text{ W/cm}^2$ , separated by  $5^\circ$ .

$$n/n_c = 0.21$$

$$T_e = 2.5 \text{ keV}$$

$$k_0 \lambda_D \cong 0.12$$



# TPD is found to depend on overlapped beam intensities, and to be limited by the “Landau cutoff”



- **The problem: if a pump  $(k_0, \omega_0)$  is resonantly coupled to a “signal” wave  $(k_1, \omega_1)$  by an “idler” wave  $(k_0 - k_1, \omega_0 - \omega_1)$ , then the idler wave  $(k_0 - k_1, \omega_0 - \omega_1)$  required to link a second pump  $(k'_0, \omega_0)$  to the signal  $(k_1, \omega_1)$  is not, in general, a normal mode of the plasma.**
- **But it can become one: the driven (ponderomotive) response at  $(k'_0 - k_1, \omega_0 - \omega_1)$  is subject to Landau damping, and hence locally flattens the distribution function of at the phase velocity**

$$\frac{(\omega_0 - \omega_1)}{(k'_0 - k_1)}$$

- **Local flattening introduces new, lightly-damped modes; these are (almost) electron acoustic modes. They provide the missing link.**

# Multiple-pump modes in LDF's can be studied by solving the kinetic dispersion relation



- The kinetic dispersion relation for two-pump TPD is

$$\frac{\varepsilon(\mathbf{k}, \omega)}{1 - \varepsilon(\mathbf{k}, \omega)} = \frac{1 - \varepsilon(\mathbf{k}_0 - \mathbf{k}, \omega_0 - \omega)}{\varepsilon(\mathbf{k}_0 - \mathbf{k}, \omega_0 - \omega)} \left\{ \frac{(\mathbf{k} \cdot \mathbf{v}_0)^2 [(\mathbf{k}_0 - \mathbf{k})^2 - k^2]^2}{4\omega_p^2 k^2 (\mathbf{k}_0 - \mathbf{k})^2} \right\} + \frac{1 - \varepsilon(\mathbf{k}'_0 - \mathbf{k}, \omega_0 - \omega)}{\varepsilon(\mathbf{k}'_0 - \mathbf{k}, \omega_0 - \omega)} \left\{ \frac{(\mathbf{k} \cdot \mathbf{v}'_0)^2 [(\mathbf{k}'_0 - \mathbf{k})^2 - k^2]^2}{4\omega_p^2 k^2 (\mathbf{k}'_0 - \mathbf{k})^2} \right\}.$$

- The local flattening makes  $\varepsilon(\mathbf{k}'_0 - \mathbf{k}, \omega_0 - \omega)$  resonant, so the second term contributes as much as the first.

# How does TPD differ from anomalous (large $k\lambda_D$ ) SRS?

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- In both cases the Landau damping of the beat of two lightly-damped modes (pump and signal) generates local flattening and a new, lightly damped mode (idler) that did not exist in the original Maxwellian.
- In the SRS case, both pump and signal are EM waves, essentially undamped for all  $k$ , so the idler can have large  $k\lambda_D$ .
- In the TPD case, the signal is a plasma wave and must have  $k_1\lambda_D < 0.25$  to be lightly damped. Since  $k_0\lambda_D \ll k_1\lambda_D$  at the Landau cutoff, we must also have  $k_2\lambda_D \lesssim 0.25$ .
- So TPD is limited by the Landau cutoff, while SRS is not.

## Summary/Conclusions

# A model based on electron-acoustic waves can account for otherwise enigmatic features of both TPD and SRS



- Why does the level of TPD activity depend on overlapped rather than single-beam intensities?
- Why does TPD respect the “Landau limit” on plasmon wave vector, while SRS does not?
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