

The Effects of Beam Intensity Structure on Two-Plasmon Decay in Direct-Drive Laser Fusion Targets



R. W. Short

**University of Rochester
Laboratory for Laser Energetics**

**42nd Annual Meeting of the American Physical Society
Division of Plasma Physics
Québec City, Canada
23–27 October 2000**

The Effects of Beam-Intensity Structure on Two-Plasmon Decay in Direct-Drive Laser Fusion Targets

R. W. Short

Laboratory for Laser Energetics, U. of Rochester

Two-plasmon decay involves the conversion of an incident electromagnetic wave into two Langmuir waves at the quarter-critical density. Because of its comparatively low threshold and potential for hot-electron production, the theory of this instability has been extensively studied. Its linear behavior for idealized one-dimensional pump and plasma structures is well known. Two-plasmon decay is essentially a two-dimensional instability, however, since at least one of the product plasma waves must propagate at a finite angle to the pump. Thus, the short-scale-length azimuthal intensity variations produced by beam-smoothing techniques such as SSD can be expected to affect the growth and saturation of the instability. The size threshold for two-plasmon decay to be transversely localized as an absolute instability in a hot spot is calculated and compared with the intensity structures expected at quarter-critical density. This work was supported by the U.S. Department of Energy Office of Inertial Confinement Fusion under Cooperative Agreement No. DE-FC03-92SF19460.

Summary

Hot-spot effectiveness in driving two-plasmon decay is reduced relative to SBS and SRS because of the two-dimensional nature of the instability



- **SBS and SRS have maximum growth rates for backscatter; in two-plasmon decay the fastest-growing plasma waves have perpendicular components comparable to their parallel components.**
- **Hot spots in smoothed beams are aligned with the pump direction, so they should be less effective in driving TPD than SRS or SBS.**
- **TPD is near threshold for direct-drive conditions, but the threshold is exceeded in hot spots.**
- **The two-plasmon decay waves tend to propagate out of hot spots laterally, but absolute growth can still occur.**
- **Shorter amplification range may reduce hot-electron production by nonlinearly saturated waves.**

Outline

- **Calculation of intensity distribution in spherically symmetric coronas**
- **Calculation of transverse absolute instability thresholds for two-plasmon decay (TPD)**
- **Comparison with hot-spot radii and intensities**
- **Summary and conclusions**

The intensity pattern in a spherically symmetric plasma corona may be calculated using spherical harmonics

- Neglecting polarization, the field amplitude satisfies the scalar wave equation:

$$\nabla^2 \mathbf{E} + \frac{\omega^2}{c^2} \varepsilon(\mathbf{r}) \mathbf{E} = 0$$

- Absorption can be included by using a complex dielectric function:

$$\varepsilon(\mathbf{r}) = 1 - \frac{\omega_{pe}^2(\mathbf{r})}{\omega[\omega + i\nu_{ei}(\mathbf{r})]}$$

- $\mathbf{E}(\mathbf{r}, \theta, \phi)$ is expanded in spherical harmonics:

$$\mathbf{E}(\mathbf{r}, \theta, \phi) = \sum_{\ell, m} \mathbf{a}_{\ell, m} \frac{1}{r} \mathbf{g}_{\ell}(\mathbf{r}) Y_{\ell, m}(\theta, \phi)$$

The solution to the radial wave equation can be represented by an asymptotic approximation

- The radial wave functions satisfy

$$\frac{d^2g}{ds^2} + \left[\varepsilon(s) - \frac{\ell(\ell+1)}{s^2} \right] g = 0, \quad s = \frac{\omega_0}{c} r$$

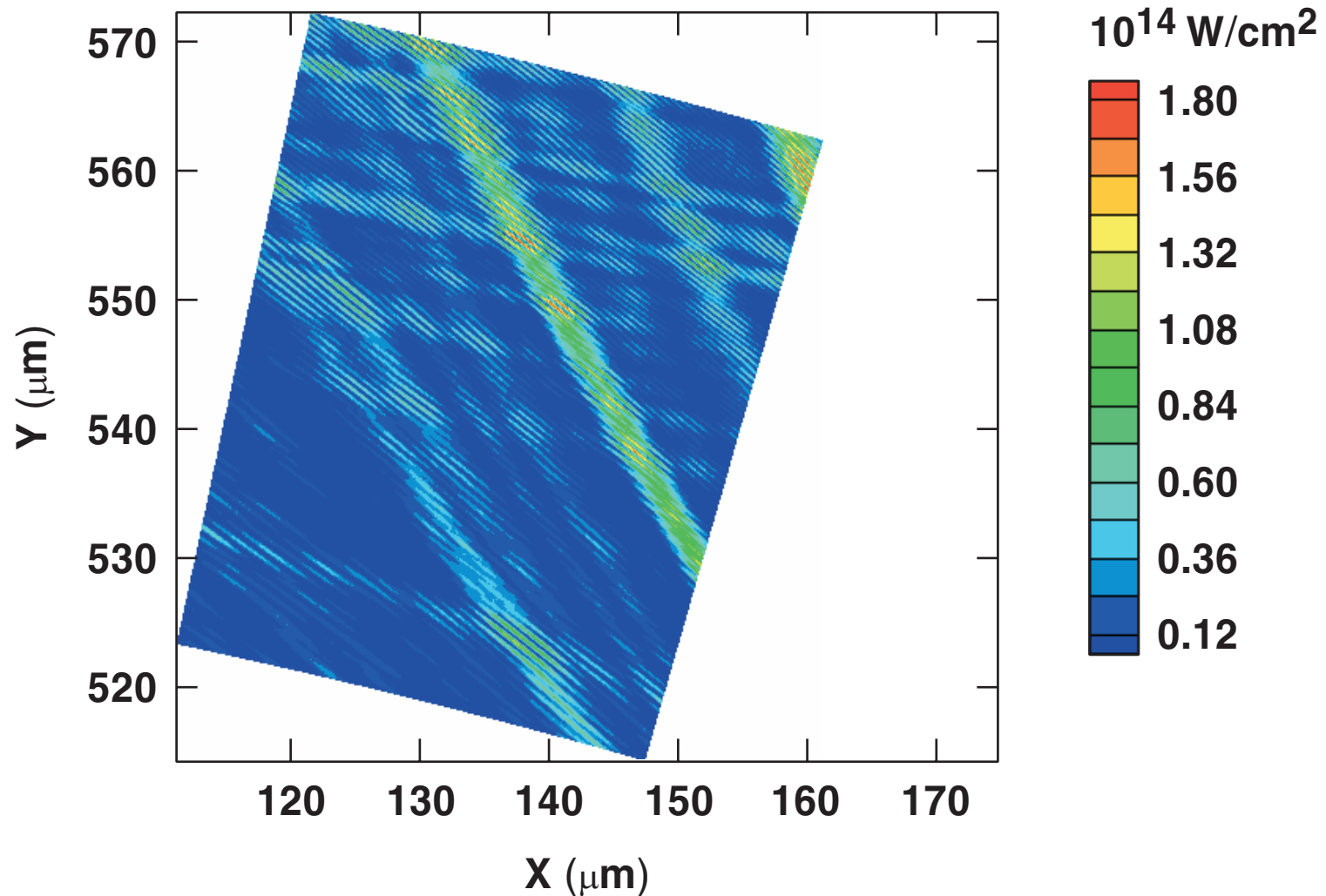
- The approximate solution can be written:

$$g_\ell(s) = 2\sqrt{\pi} \left(\frac{3}{2} S_0 \right)^{1/6} [Q(s)]^{-1/4} \text{Ai} \left[\left(\frac{3}{2} S_0 \right)^{2/3} \right], \quad Q(s) = \varepsilon(s) - \frac{\ell(\ell+1)}{s^2}, \text{ and}$$

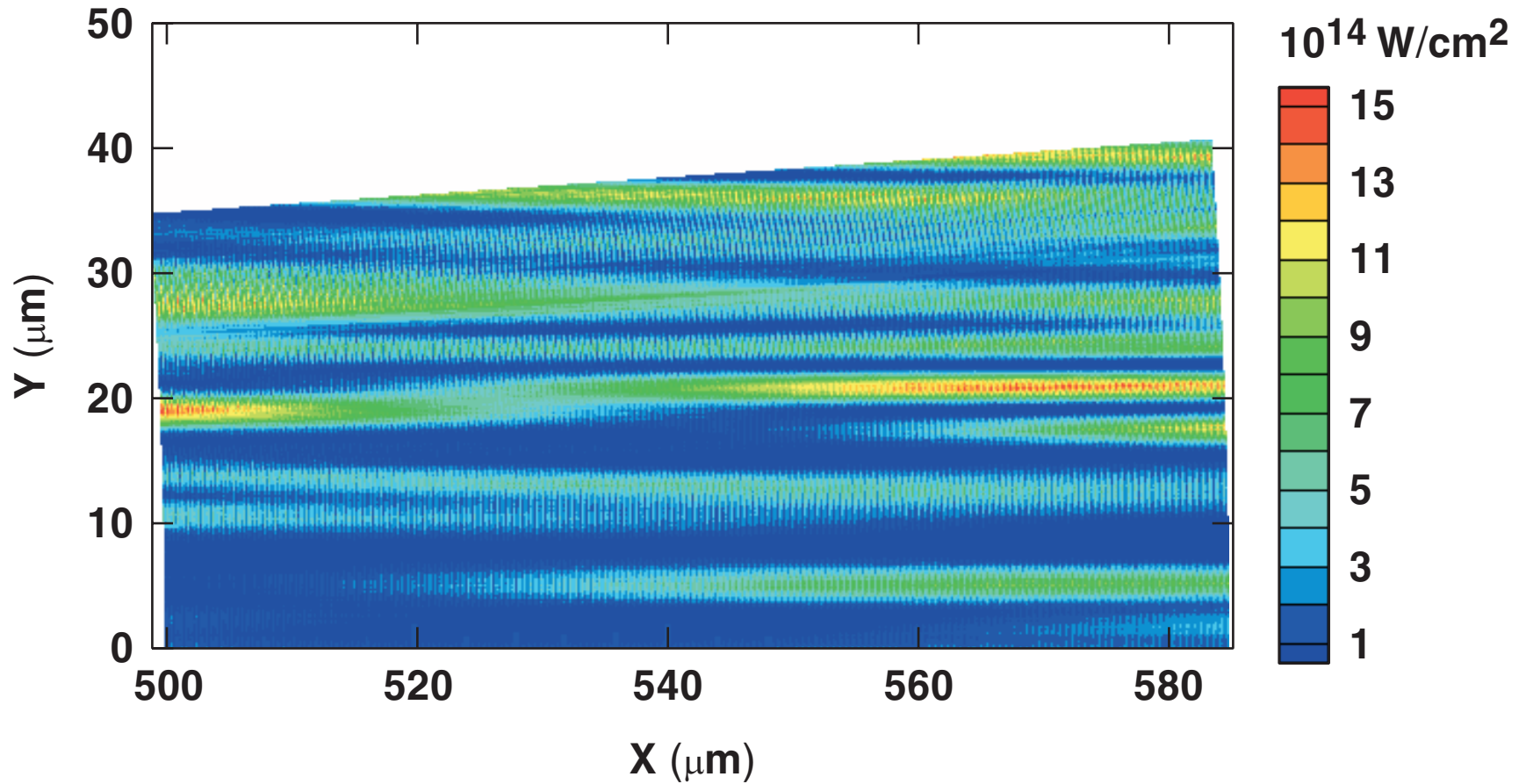
$$S_0 = \int_{s_t}^s Q^{1/2}(s) ds$$

- This solution is valid for all radii (both over- and underdense plasma), and for scale lengths longer than a few microns is virtually identical to the exact numerical solution.

Hot spots are less intense where caustic meets quarter-critical density



Quarter-critical hot spots reach $\sim 15\times$ nominal intensity



Growth rates and instability thresholds for TPD are obtained from the dispersion relation

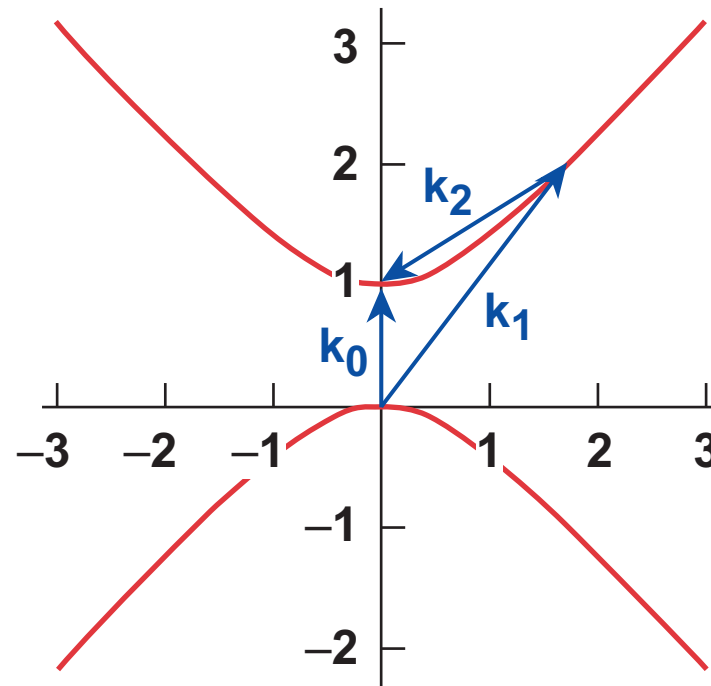
- The dispersion relation for TPD can be written $D(\omega, \mathbf{k}) = 0$, where

$$D(\omega, \mathbf{k}) \equiv (\omega^2 - \omega_{e, \mathbf{k}}^2) \left[(\omega - \omega_0)^2 - \omega_{e, \mathbf{k} - \mathbf{k}_0}^2 \right] - \left\{ \frac{\mathbf{k} \cdot \mathbf{v}_{\text{osc}} \omega_{pe} \left[(\mathbf{k} - \mathbf{k}_0)^2 - k^2 \right]}{2k |\mathbf{k} - \mathbf{k}_0|} \right\}^2 .$$

- If $k_{\perp \text{max}}$ is the perpendicular wave number giving the maximum growth rate, the propagation velocity of the fastest-growing amplitude is

$$\mathbf{V} = \left. \frac{\partial \omega_r}{\partial \mathbf{k}_{\perp}} \right|_{\mathbf{k}_{\perp \text{max}}} = \left. \frac{\partial D(\mathbf{k}, \omega) / \partial \mathbf{k}_{\perp}}{\partial D(\mathbf{k}, \omega) / \partial \omega} \right|_{\mathbf{k}_{\perp \text{max}}}$$

Fastest growth rates occur for comparable perpendicular and parallel wave vectors



- Growth rates are limited by inhomogeneity for small wave vectors and by Landau damping for large wave vectors.
- For NIF, lowest threshold $\sim 10^{14}$ W/cm²; marginal, but exceeded in hot spots.

The threshold for transverse absolute instability can be obtained from the homogeneous dispersion relation

- Assuming the density is uniform perpendicular to the pump, the condition for absolute instability is found by imposing boundary conditions of zero incoming waves at $y = 0, L$.

- The result is

$$\frac{(k - k_0)^2 - k^2}{k|k - k_0|} \frac{v_0}{\sqrt{v_{\perp 1} v_{\perp 2}}} kL > \pi$$

- This can be approximated by $I_{14}^{1/2} > 0.68 \frac{T_{\text{keV}}}{L_{\perp \mu}}$
- Easily satisfied in hot spots.

Bandwidth increases threshold for absolute TPD and/or reduces time available for growth

- Hot spots are caused by interference between different parts of the laser beam; bandwidth causes spots to move or flicker.
- Maximum velocity due to bandwidth is $\frac{V}{c} \sim F \frac{\Delta\lambda}{\lambda} \sim 1.2 \times 10^{-3} F \Delta\nu$ (THz).
- At this relative velocity, the instability is no longer absolute at typical hot-spot intensities; but most hot spots won't move this fast.
- Some hot spots don't move at all; some may vary in intensity without moving.
- Effect of bandwidth on TPD requires convolution of hot-spot temporal and spatial variation with absolute TPD threshold conditions.

Summary/Conclusions

Hot-spot effectiveness in driving two-plasmon decay is reduced relative to SBS and SRS because of the two-dimensional nature of the instability



- **SBS and SRS have maximum growth rates for backscatter; in two-plasmon decay the fastest-growing plasma waves have perpendicular components comparable to their parallel components.**
- **Small-radius hot spots in smoothed beams are aligned along the pump, so they would be expected to be less effective in driving TPD.**
- **TPD is near threshold for direct-drive conditions, but the threshold is exceeded in hot spots.**
- **The two-plasmon decay waves tend to propagate out of hot spots laterally, but absolute growth can still occur.**
- **Shorter amplification range may reduce hot-electron production by nonlinearly saturated waves.**