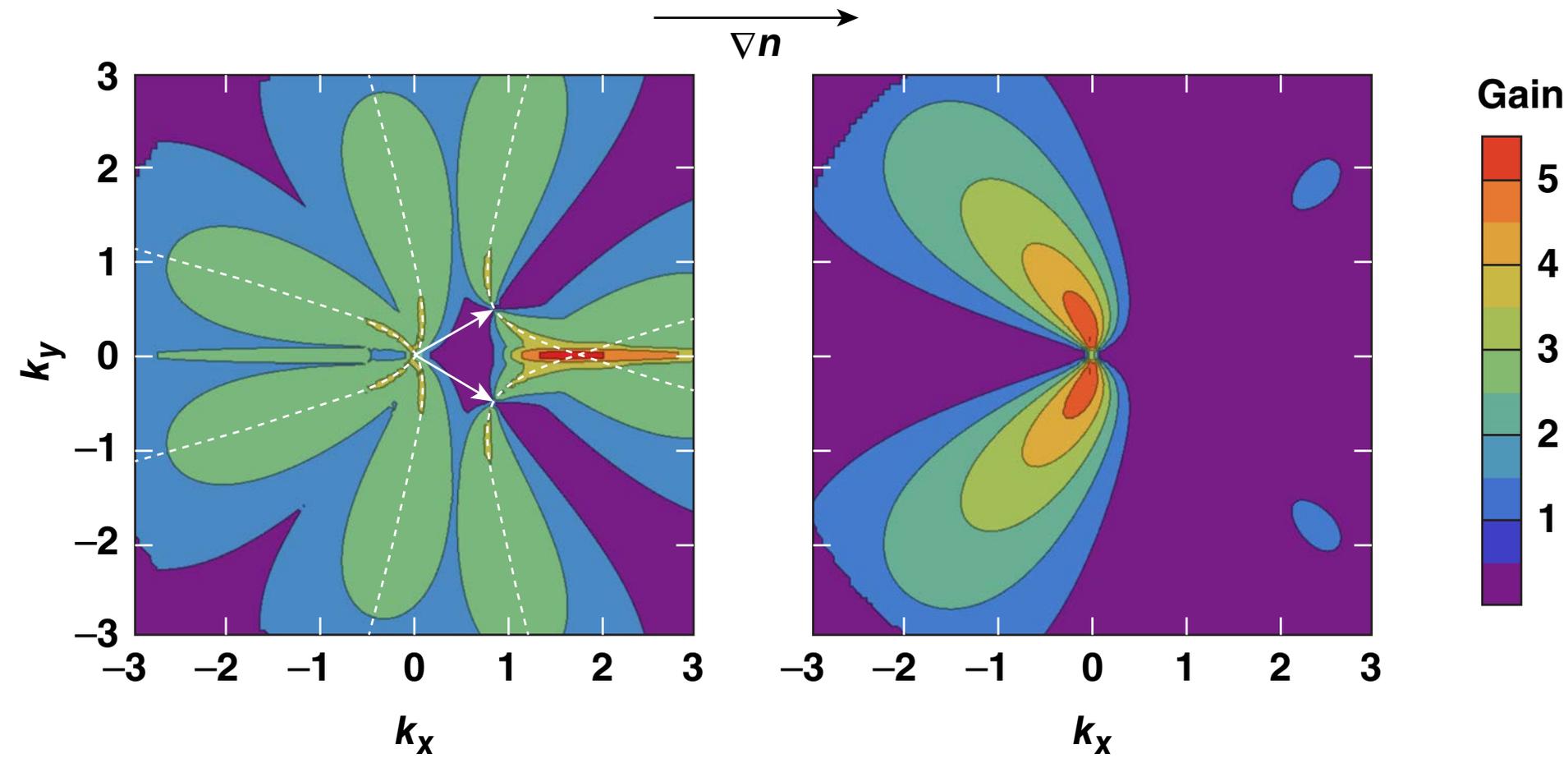


Absolute Two-Plasmon Decay and Stimulated Raman Scattering in Direct-Drive Irradiation Geometries



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Summary

In general, both stimulated Raman scattering (SRS) and two-plasmon decay (TPD) will play a role in direct-drive laser–plasma interactions



- **Absolute TPD and SRS thresholds have different dependencies on laser and plasma parameters, but are comparable**
- **The modes with lowest thresholds tend to be either SRS or TPD; mixed polarization modes seem unimportant**
- **Larger scale lengths and temperatures favor SRS; larger incidence angles favor TPD**
- **The analysis presented here is linear; however there is evidence that the absolute SRS/TPD it describes persists well into the nonlinear regime**

The origin in k space corresponds to the plasma-wave turning point, allowing SRS and TPD to be absolute there

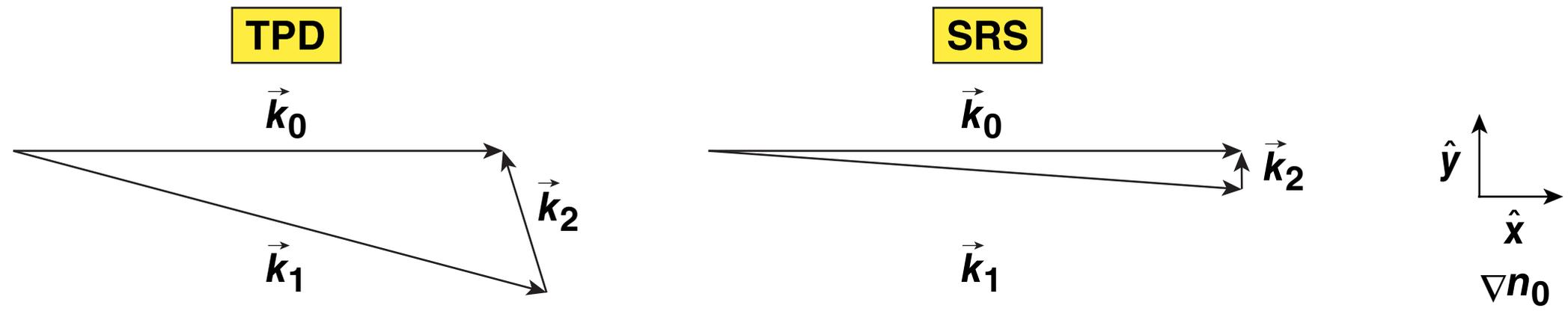


- In general, instabilities can only be convective in inhomogeneous plasmas*
- Near the turning point, however, there is a finite threshold for absolute instability**
- Enhanced multibeam convective gain near the origin in k space suggests the potential for absolute instability there
- Convective SRS occurs for $n/n_c \leq 1/4$; for absolute SRS, the electromagnetic (EM) decay wave must have $k \cong 0$ and originate at $n/n_c \cong 1/4$

*M. N. Rosenbluth, Phys. Rev. Lett. 29, 565 (1972).

**C. S. Liu, M. N. Rosenbluth, and R. B. White, Phys. Rev. Lett. 31, 697 (1973);
A. Simon *et al.*, Phys. Fluids 26, 3107 (1983).

Absolute SRS requires the component of k perpendicular to the density gradient to vanish



- The y components of the plasma-wave group velocity $v_g = 3v_T^2 k / \omega$ are equal and opposite, so TPD is absolute in the y direction
- For SRS, $v_{g1y} = 3v_T^2 k_{1y} / \omega$ and $v_{g2y} = c^2 k_{2y} / \omega$, so SRS will be convective in y unless $k_{2y} \cong 0$

For a single beam, the absolute TPD threshold* is lower than the Rosenbluth convective threshold

- The Simon threshold (adjusted for s-polarized oblique incidence) is $\eta \equiv \frac{I_{14} L_{\mu}}{233 T_{\text{keV}} \cos\theta} > 1$
- The Rosenbluth convective gain is $G_R = \frac{2\pi\gamma_0^2}{\kappa' V_1 V_2} = \frac{I_{14} L_{\mu}}{53.6 T_{\text{keV}} \cos\theta} \cong 4.35 \eta$
- The nominal convective threshold is $G_R > 2\pi$ or $\eta > \frac{2\pi}{4.35} \cong 1.44$
- Therefore, the TPD absolute instability threshold lies below the convective instability threshold; this, in general, remains true for multiple beams
- The threshold for absolute SRS is comparable**

*A. Simon *et al.*, Phys. Fluids 26, 3107 (1983).

**C. S. Liu, M. N. Rosenbluth, and R. B. White, Phys. Fluids 17, 1211 (1974).

Fourier analysis of the time-independent TPD equations results in a set of first-order linear differential equations



- Absolute TPD and SRS occur near quarter-critical, so the local density profile may be approximated by a linear gradient
- Fourier transforming in space, the wave equations become first-order linear equations for the longitudinal and transverse components of the small- k decay wave
- The larger- k decay wave may be taken to be longitudinal
- For N beams there are therefore $3N + 1$ linear differential equations that are integrated from $k_x \rightarrow -\infty$ to $k_x \rightarrow +\infty$ to obtain the spatial gain
- Divergence of the gain indicates an onset of absolute instability; optimizing over ω gives the threshold and frequency

Fourier analysis of the time-independent TPD equations results in a set of first-order linear differential equations

- For a single beam, take the decay triangle in the x–y plane and normalize $\vec{k} \rightarrow c\vec{k}/\omega_0$, $\Delta \rightarrow \omega/\omega_0 - 1/2$, $L \rightarrow \omega_0 L/c$

$$\frac{\partial u_L}{\partial k_x} = iL \left(\frac{k_d}{k} - \frac{k}{k_d} \right) (k \cdot v_0) e^{-4iL \left\{ 2\Delta k_x - 3 \frac{v_T^2}{c^2} \left(\frac{1}{3} k_x^3 + k_y^2 k_x \right) + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_d$$

$$\frac{\partial u_T}{\partial k_x} = iL \frac{k_d}{k} [(k_x \hat{y} - k_y \hat{x}) \cdot v_0] e^{-4iL \left\{ 2\Delta k_x - \left[\frac{1}{3} k_x^3 + \left(\frac{ck_y}{\omega_0} \right)^2 k_y^2 k_x \right] + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_d$$

$$\frac{\partial u_z}{\partial k_x} = iL k_d v_{0z} e^{-4iL \left\{ 2\Delta k_x - \left(\frac{1}{3} k_x^3 + k_y^2 k_x \right) + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_d$$

$$\frac{\partial u_d}{\partial k_x} = iL \left(\frac{k_d}{k} - \frac{k}{k_d} \right) \left(\frac{ck}{\omega_0} \cdot \frac{v_0}{c} \right) (k \cdot v_0) e^{4iL \left\{ 2\Delta k_x - 3 \frac{v_T^2}{c^2} \left(\frac{1}{3} k_x^3 + k_y^2 k_x \right) + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_L$$

$$+ iL \frac{k_d}{k} [(k_x \hat{y} - k_y \hat{x}) \cdot v_0] e^{4iL \left\{ 2\Delta k_x - \left[\frac{1}{3} k_x^3 + \left(\frac{cky}{\omega_0} \right)^2 k_y^2 k_x \right] + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_T$$

$$+ iL k_d v_{0z} e^{4iL \left\{ 2\Delta k_x - \left(\frac{1}{3} k_x^3 + k_y^2 k_x \right) + 3 \frac{v_T^2}{c^2} \left[\frac{1}{3} (k_x - k_{0x})^3 + (k_y - k_{0y})^2 k_x \right] \right\}} u_z$$

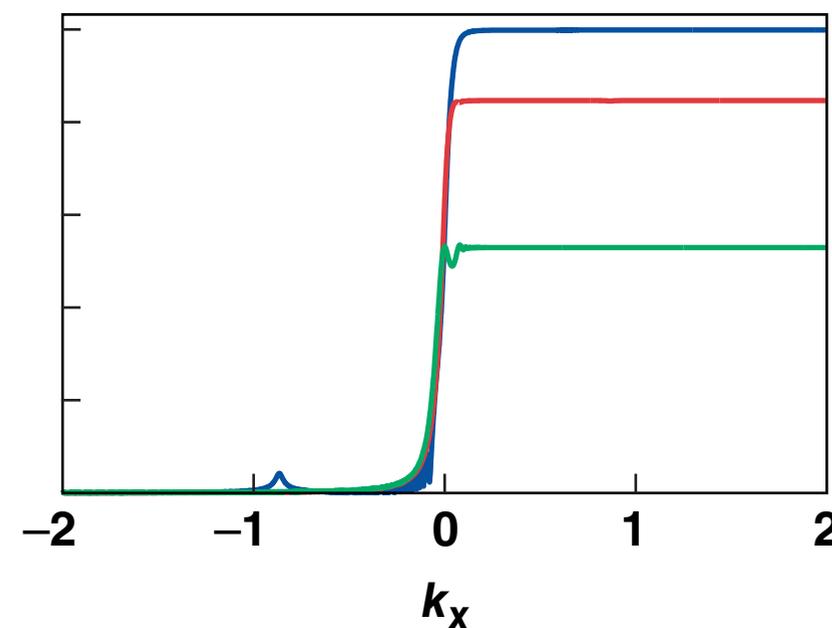
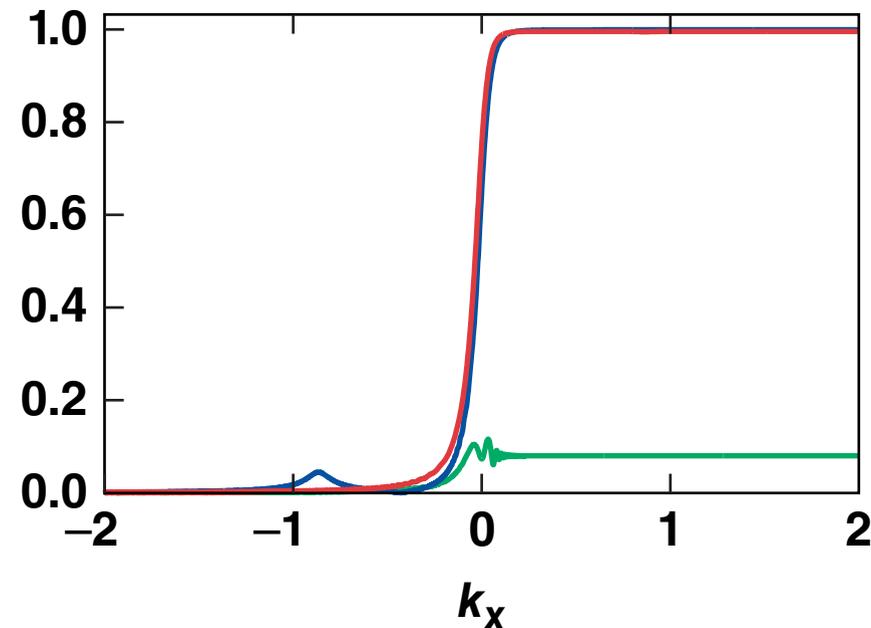
For smaller k_{\perp} , TPD decay waves become more transverse

- The optimal SRS mode has $k \cong 0$ and is almost entirely electromagnetic
- The optimal TPD mode is almost entirely electrostatic (ES); for smaller k_{\perp} , the EM component and the threshold increase

$k_{\perp} = 0.06$
Threshold $I_{14} = 1.54$

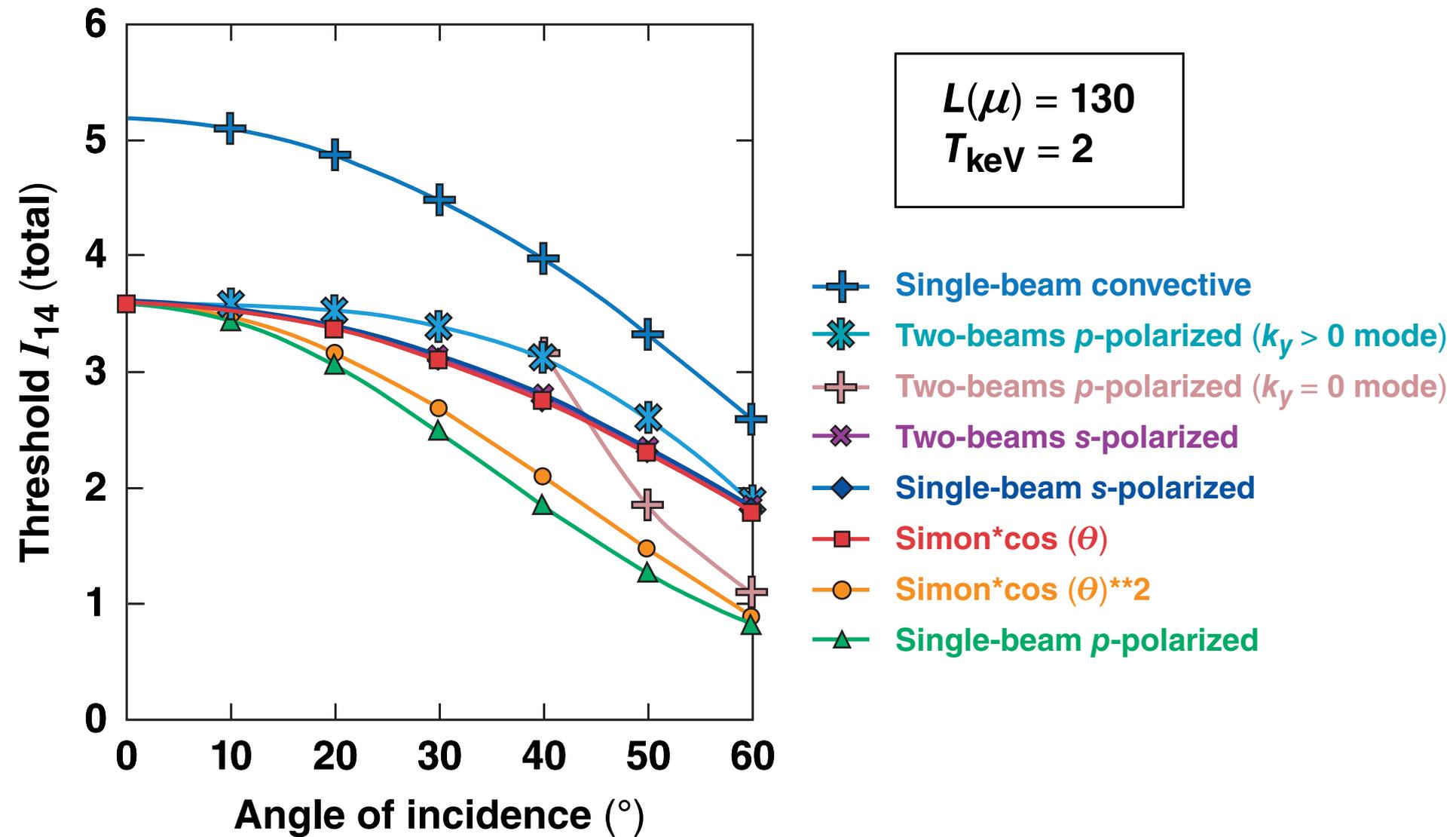
$k_{\perp} = 0.02$
Threshold $I_{14} = 1.85$

$L(\mu) = 300$
 $T_{\text{keV}} = 2.0$

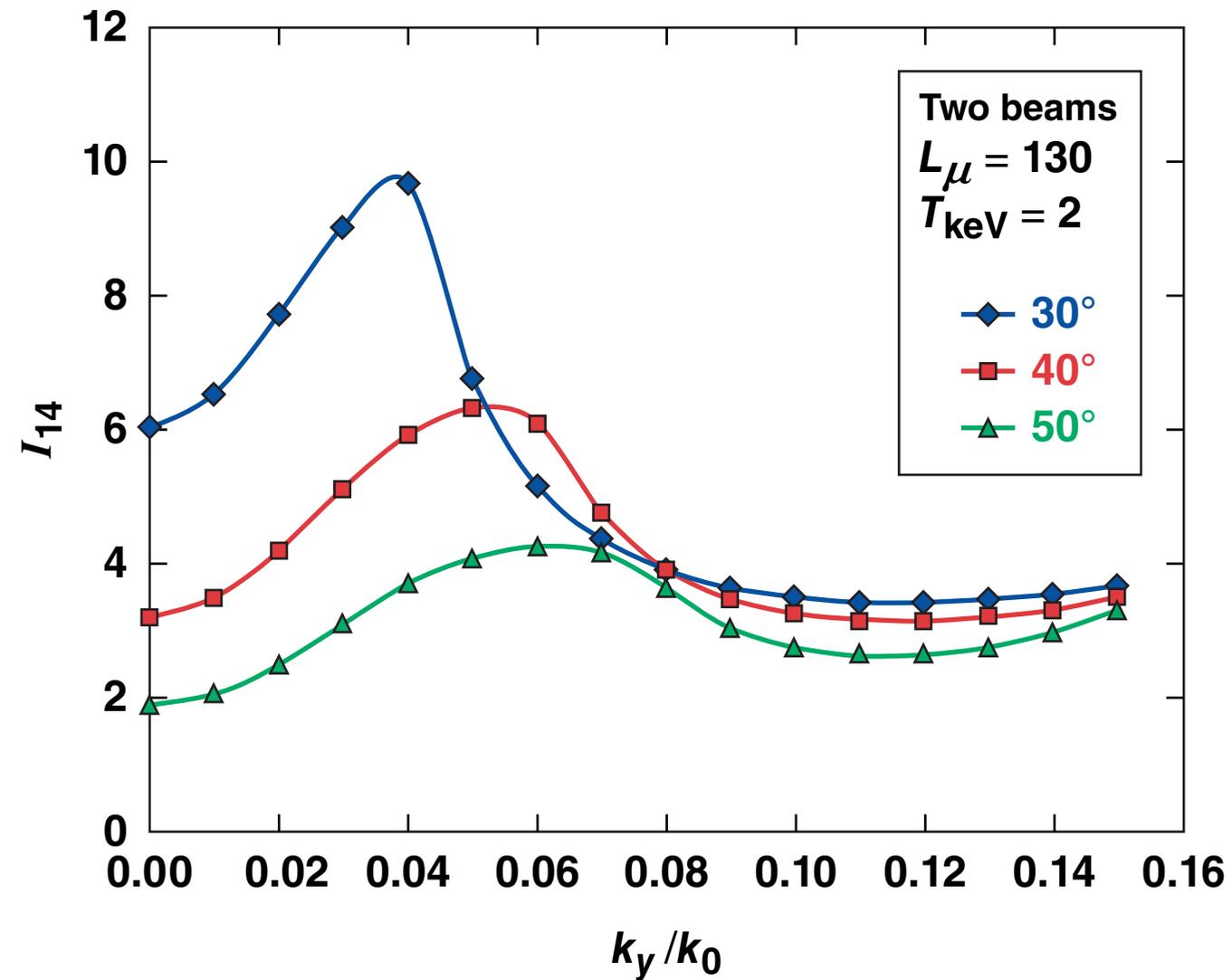


— Large k wave
— Small k wave, ES component
— Small k wave, EM component

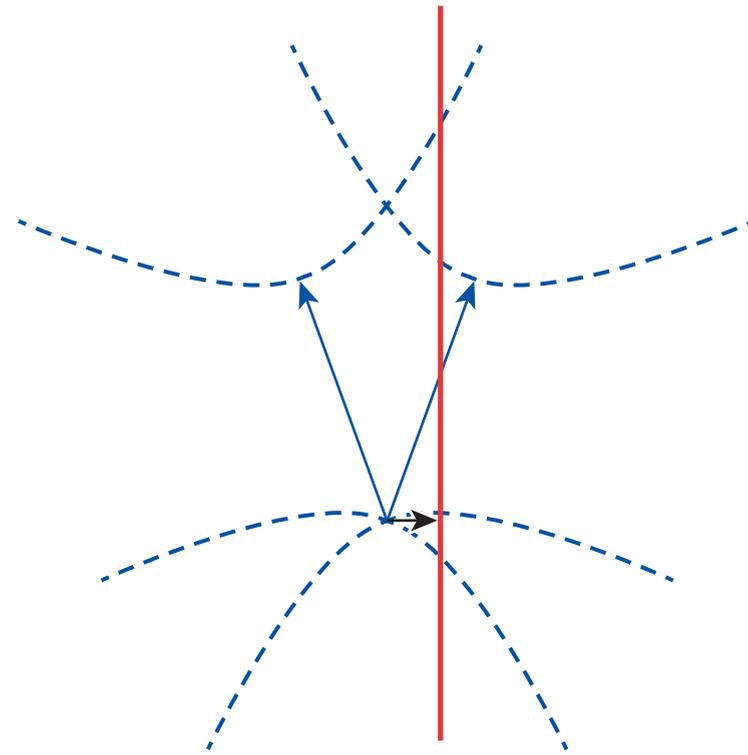
The absolute threshold for TPD depends on angle of incidence and polarization



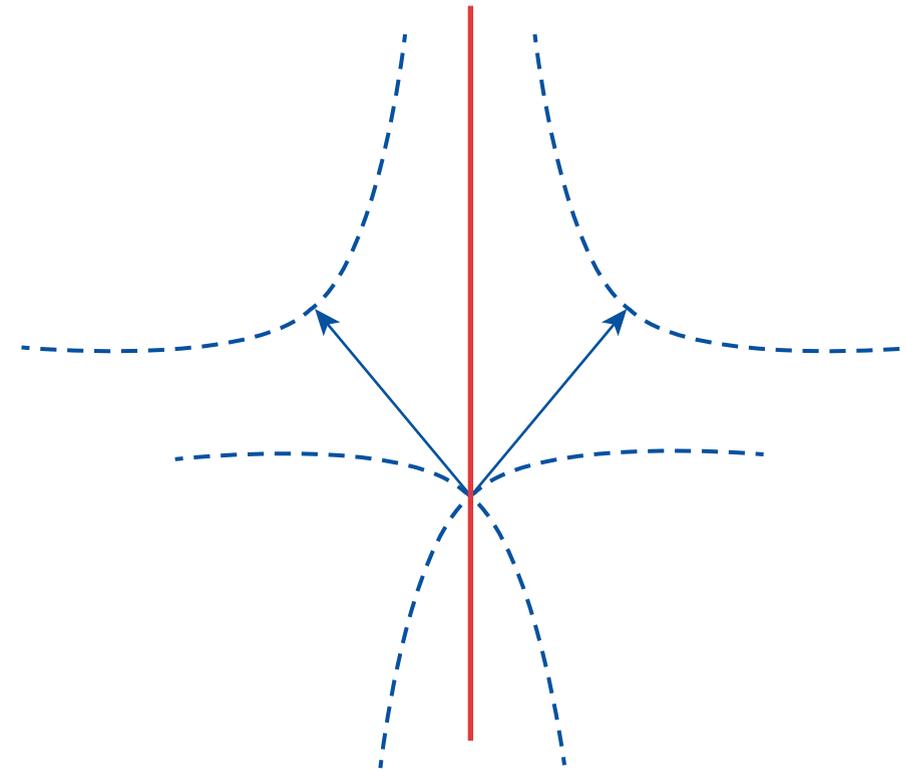
For two p -polarized beams, an on-axis TPD mode ($k_y = 0$) has the lowest threshold at larger incidence angles



At larger angles, the on-axis mode is closer to the hyperbolas than the off-axis modes



$\theta = 20^\circ$



$\theta = 40^\circ$

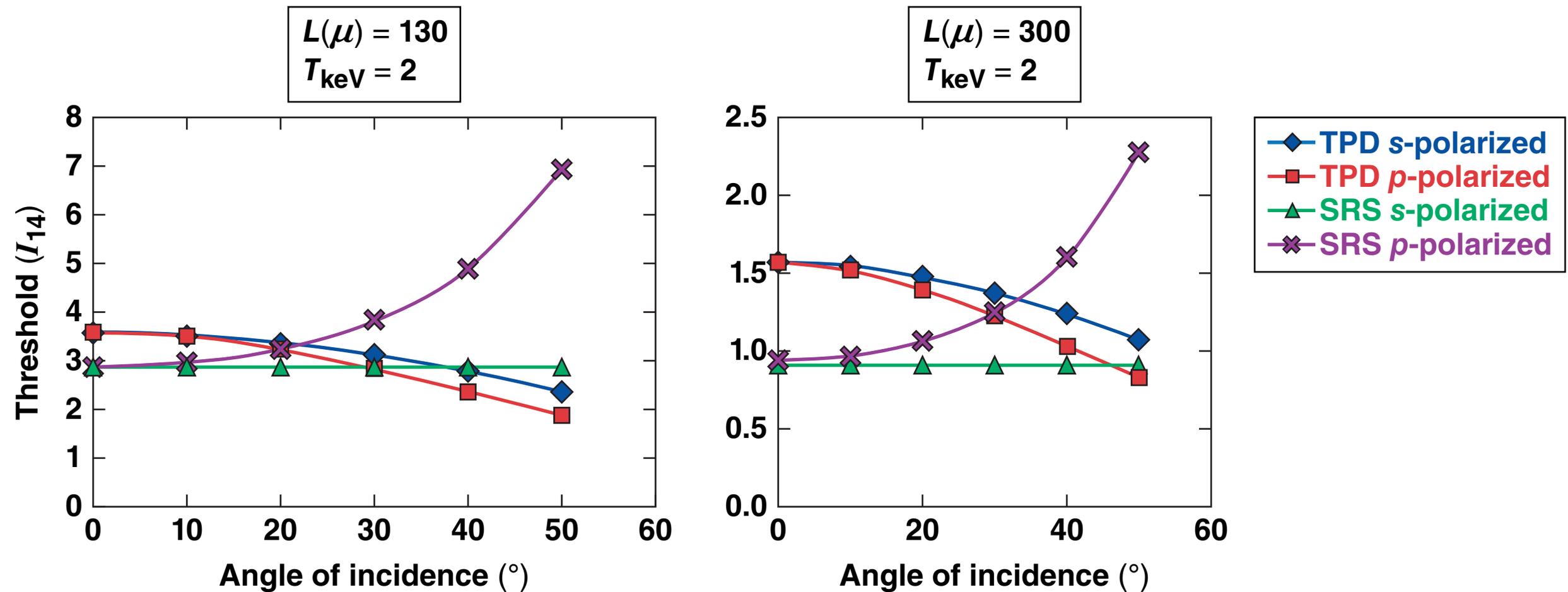
Light from absolute SRS will be emitted along the density gradient

- The much-higher group velocity of the EM wave means the instability must be absolute in the direction perpendicular to the density gradient, i.e., $k_y \sim k_z \sim 0$ and the wave is purely transverse
- Phase matching, and therefore threshold, will be insensitive to temperature
- The spectrum of the emitted light will have the same dependence on temperature as for TPD
- For s-polarization the threshold will be independent of pump incidence angle; for p-polarization the coupling is reduced for oblique incidence and the threshold increases with angle
- Analysis of the k -space equations for a normally incident beam gives

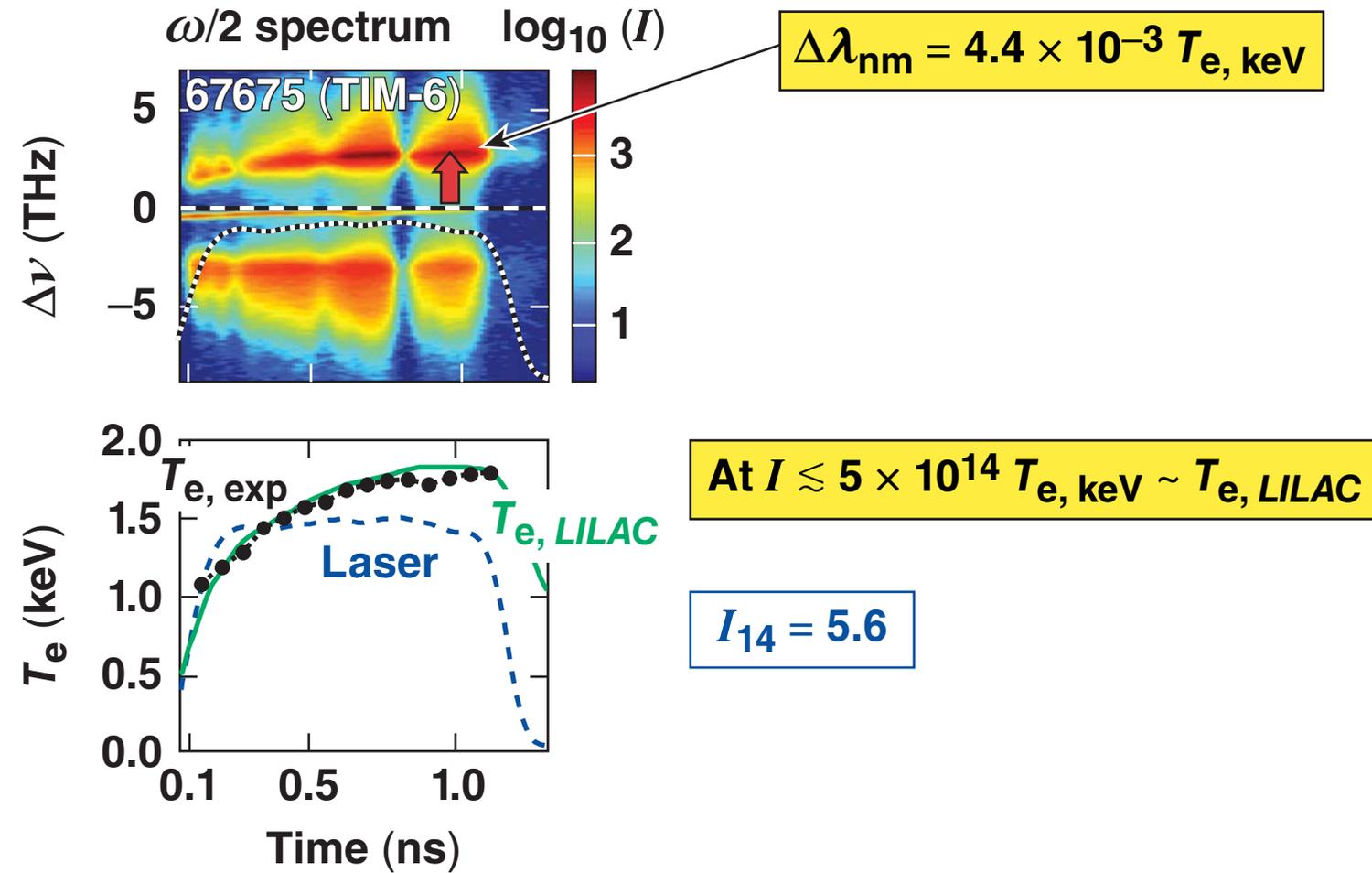
a threshold of $I_{14} > \frac{1995}{L_{\mu}^{4/3}}$, close to the Liu, Rosenbluth, and White result

For oblique incidence, TPD and SRS behave differently as a function of incidence angle

- Increasing temperatures and scale lengths favor SRS; increasing incidence angles favor TPD



The spectral signature of the absolute instability near $n_c/4$ is a sharp red-shifted feature that can be used for T_e measurements



- Although the absolute instability is obtained from linear analysis, it can remain the most-intense TPD mode in the nonlinear regime, persisting throughout the pulse

Summary/Conclusions

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