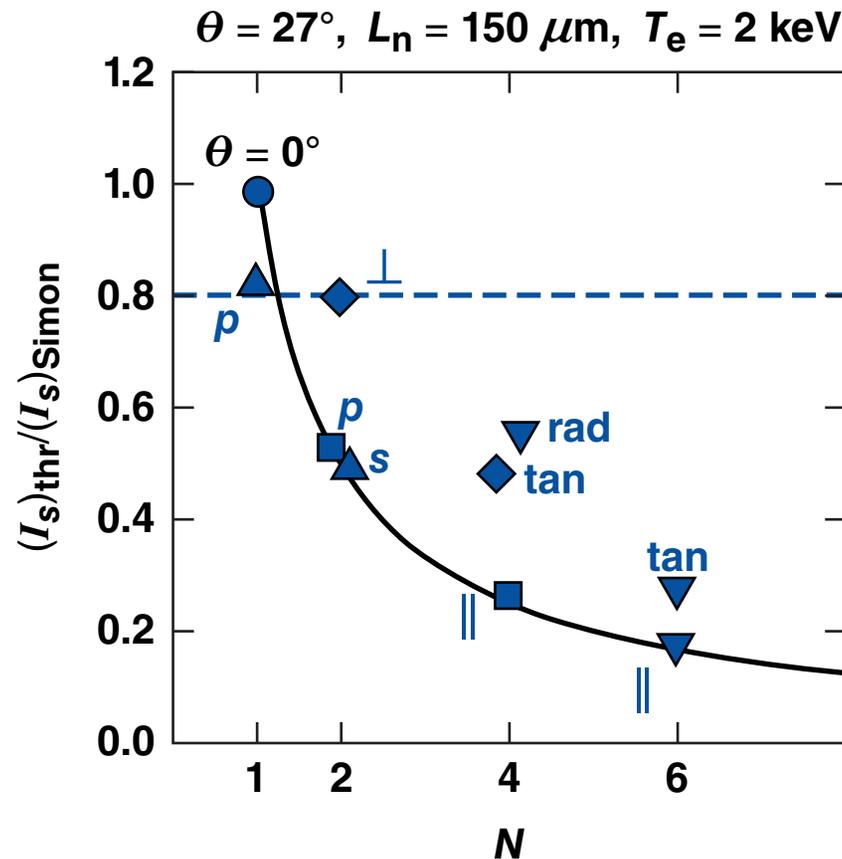


Linear Growth and Nonlinear Saturation of Two-Plasmon Decay Driven by Multiple Laser Beams



J. Zhang
University of Rochester
Laboratory for Laser Energetics

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- Our simulations recover this result, but indicate that small- k modes can share plasma waves and therefore give a lower absolute threshold for multiple beams
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*J. Zhang *et al.*, Bull. Am. Phys. Soc. **57**, 299 (2012).

C. Stoeckl *et al.*, Phys. Rev. Lett. **90, 235002 (2003);
D.T. Michel *et al.*, Phys. Rev. Lett. **109**, 155007 (2012).

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Collaborators



J. F. Myatt, R. W. Short, and A. V. Maximov

**University of Rochester
Laboratory for Laser Energetics**

H. X. Vu

University of California, San Diego, CA

D. F. DuBois and D. A. Russell

Lodestar Research Corporation, Boulder, CO

The ZAK3D model is a time-enveloped fluid moment model that describes the coupling between Langmuir and ion-acoustic fluctuations

Zakharov equation[†]

$$\nabla \cdot \left[2i\omega_{p0} (\partial_t + \overbrace{\mathbf{v}_e \cdot \nabla}^{\text{Collisional plus Landau damping}}) + 3v_e^2 \nabla^2 - \omega_{p0}^2 (\delta n + \overbrace{\delta N}^{\text{Density gradient}}) / n_0 \right] \mathbf{E}$$

$$= \underbrace{(e/4m_e) \nabla \cdot \left[\nabla \sum_{m=1}^N (\mathbf{E}_{0,m} \cdot \mathbf{E}^*) - \sum_{m=1}^N \mathbf{E}_{0,m} \nabla \cdot \mathbf{E}^* \right]}_{\text{Laser source}} e^{-i\Delta\omega t} + \underbrace{\mathbf{S}_E}_{\text{Noise source}}$$

$$\left[\partial_t^2 + \underbrace{2\mathbf{v}_i \cdot \nabla}_{\text{Landau damping for ion}} \partial_t - c_s^2 \nabla^2 \right] \delta n = \underbrace{\frac{1}{16\pi m_i} \left(\nabla^2 |\mathbf{E}|^2 + \frac{1}{4} \nabla^2 \sum_{m=1}^N |\mathbf{E}_{0,m}|^2 \right)}_{\text{Ponderomotive force}},$$

where the laser field $\mathbf{E}_L = \sum_m^N \mathbf{E}_{0,m} \exp(-i\omega_0 t) + \text{c.c.}$
 $\Delta\omega = \omega_0 - 2\omega_{pe}$

[†]D. F. DuBois, D. A. Russell, and H. A. Rose, Phys. Rev. Lett. **74**, 3983 (1995);
 D. A. Russel and D. F. DuBois, Phys. Rev. Lett. **86**, 428 (2001).

The Zakharov model makes some approximations

Approximations

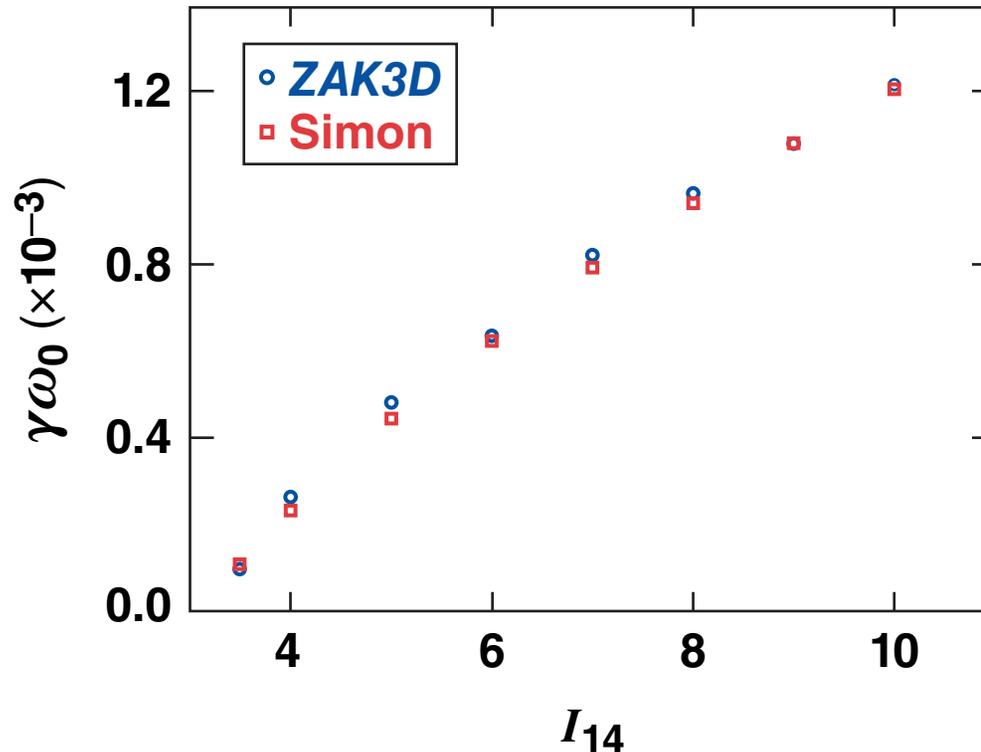
$$|\partial_t^2 \mathbf{E}| \ll |\omega_p \partial_t \mathbf{E}|;$$
$$\frac{|\mathbf{E}|^2}{4\pi n_0 T_e} \lesssim 1, \frac{\delta n_0}{n_{e0}} \lesssim 1, \text{ and } k\lambda_{De} \lesssim 1$$

Limitation

- (1) lack of kinetic effects
- (2) dissipation is included only approximately
- (3) time envelope removes higher-order harmonics

The temporal growth rate agrees very well with Simon* predictions for a single-plane electromagnetic (EM) wave

Absolute growth rate of most-unstable mode for different laser intensities



$L_n = 150 \mu\text{m}$
 $T_e = 2 \text{ keV}$

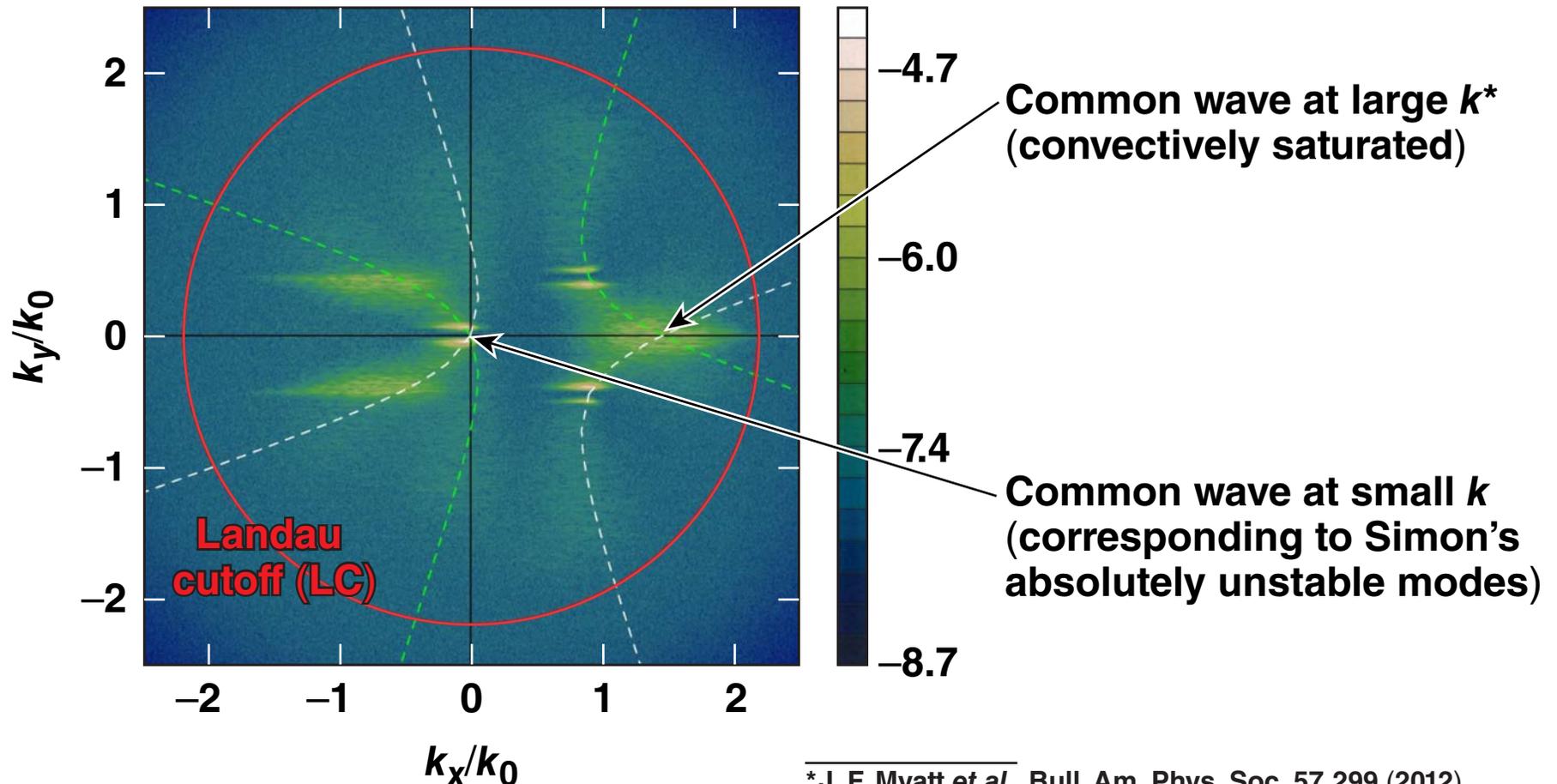
Normal laser incidence.

Most unstable modes
have $k_{\perp} \sim 0.1 k_0$

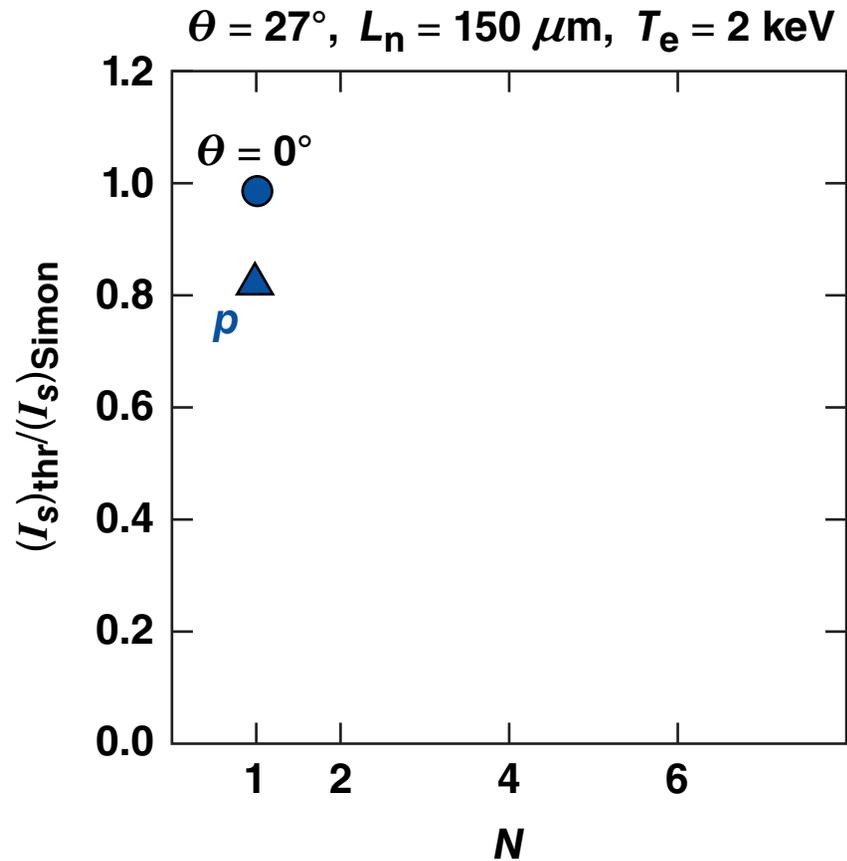
Extrapolating the growth rate to zero gives the threshold of absolute instability.

Two-plane EM waves with p -polarization show shared plasma waves in both the large- and small- k regions

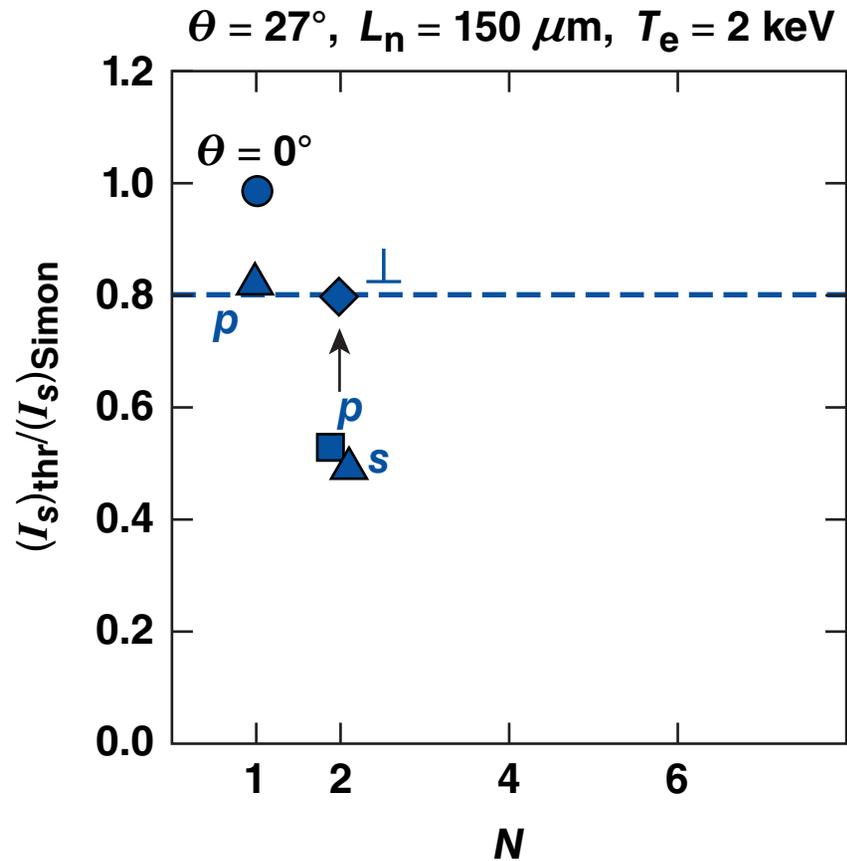
Energy spectrum of Langmuir wave (LW) during linear growth phase (early time, arbitrary units).



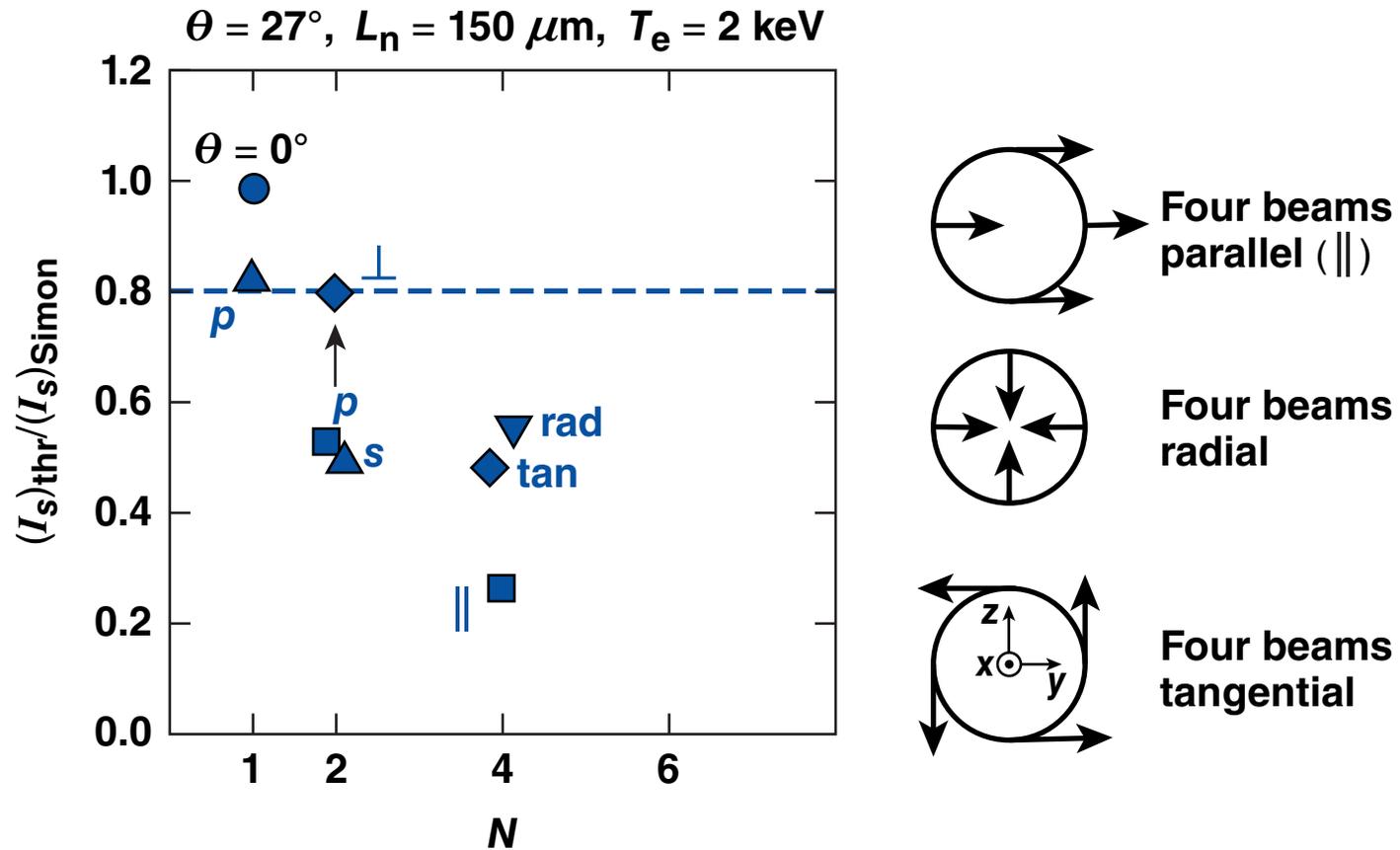
The absolute thresholds for different numbers of beams and beam configurations have been computed



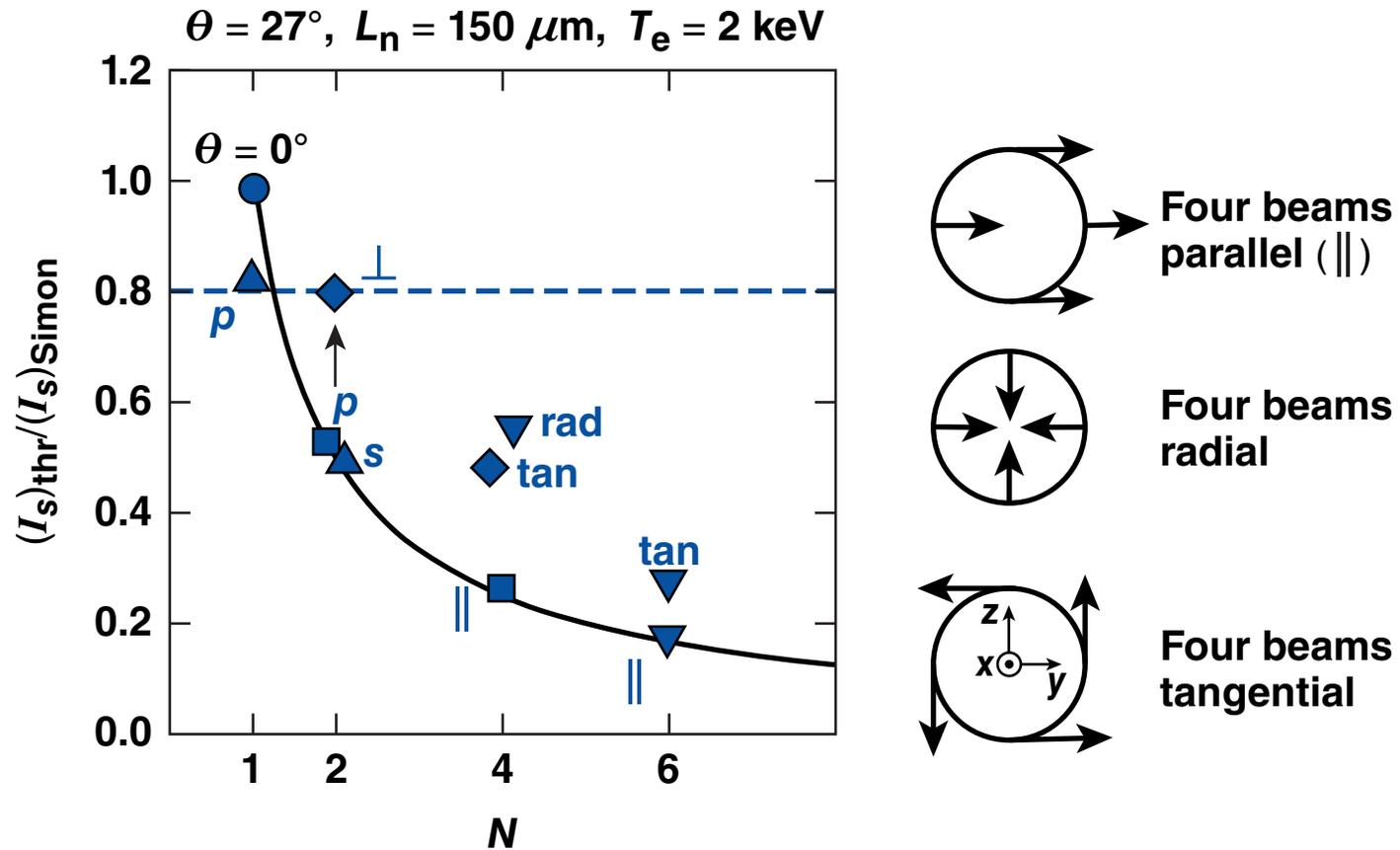
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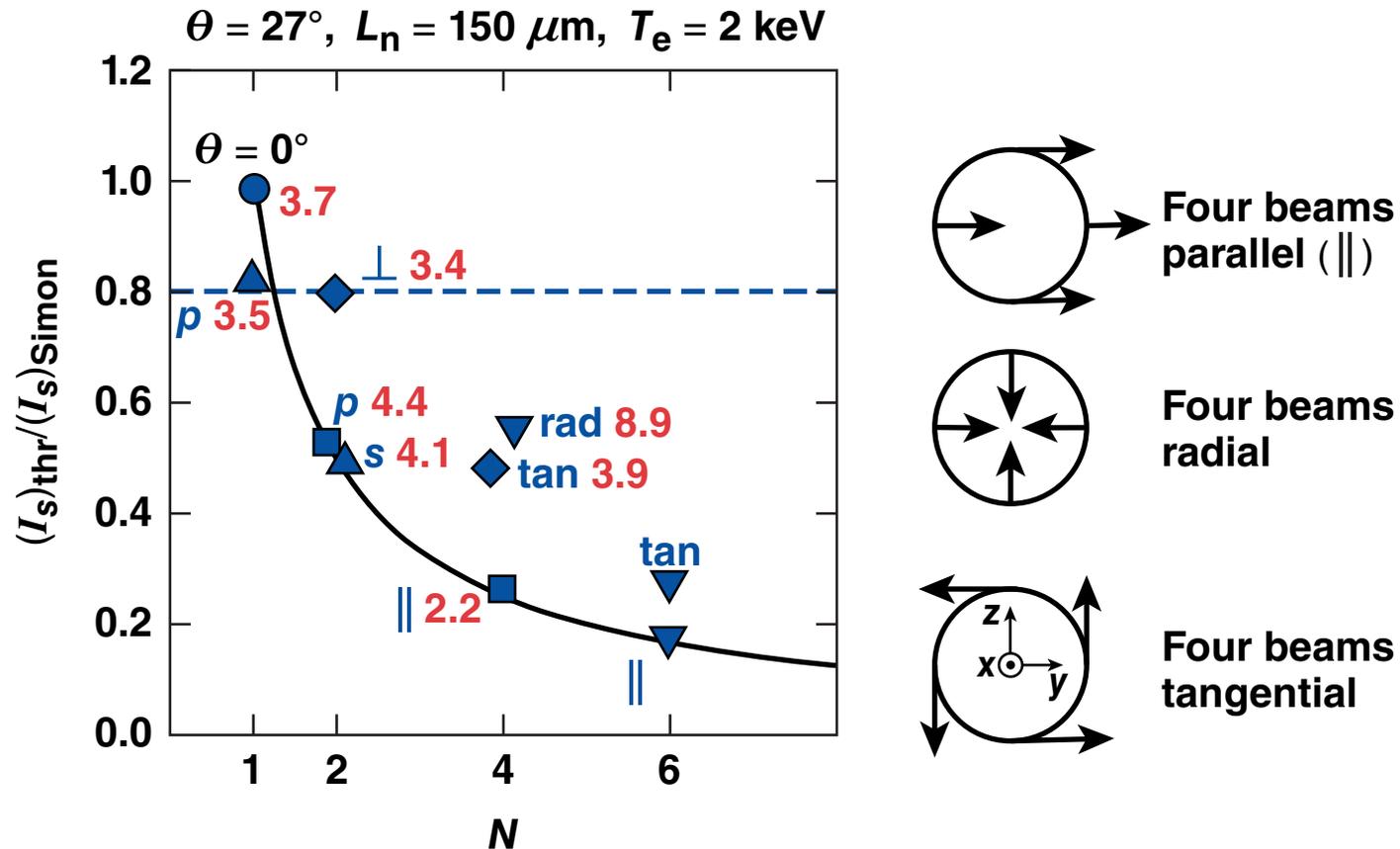
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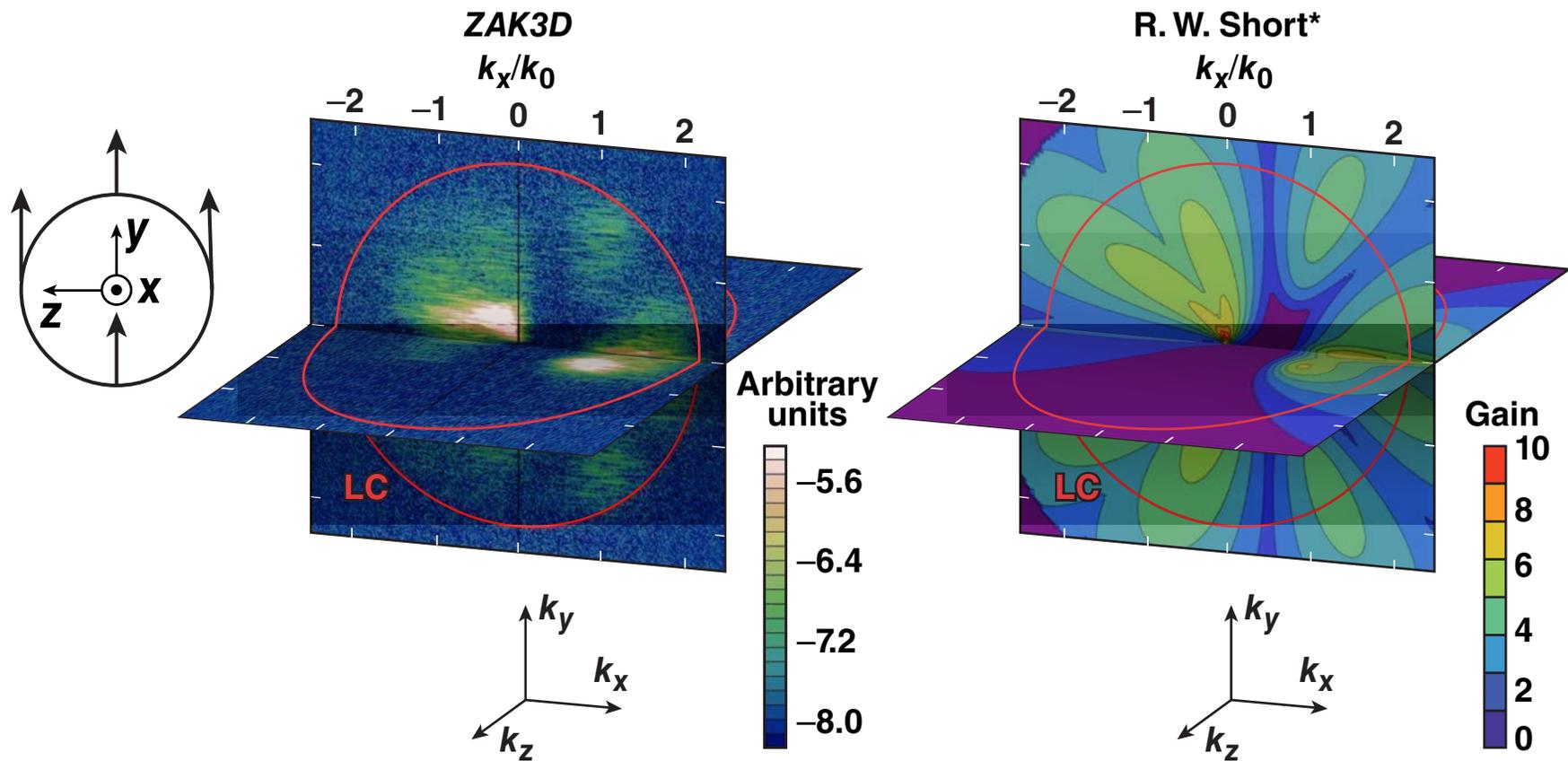


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The absolute threshold is lower than the convective threshold in most cases; the regime of linear convective growth is very restricted.

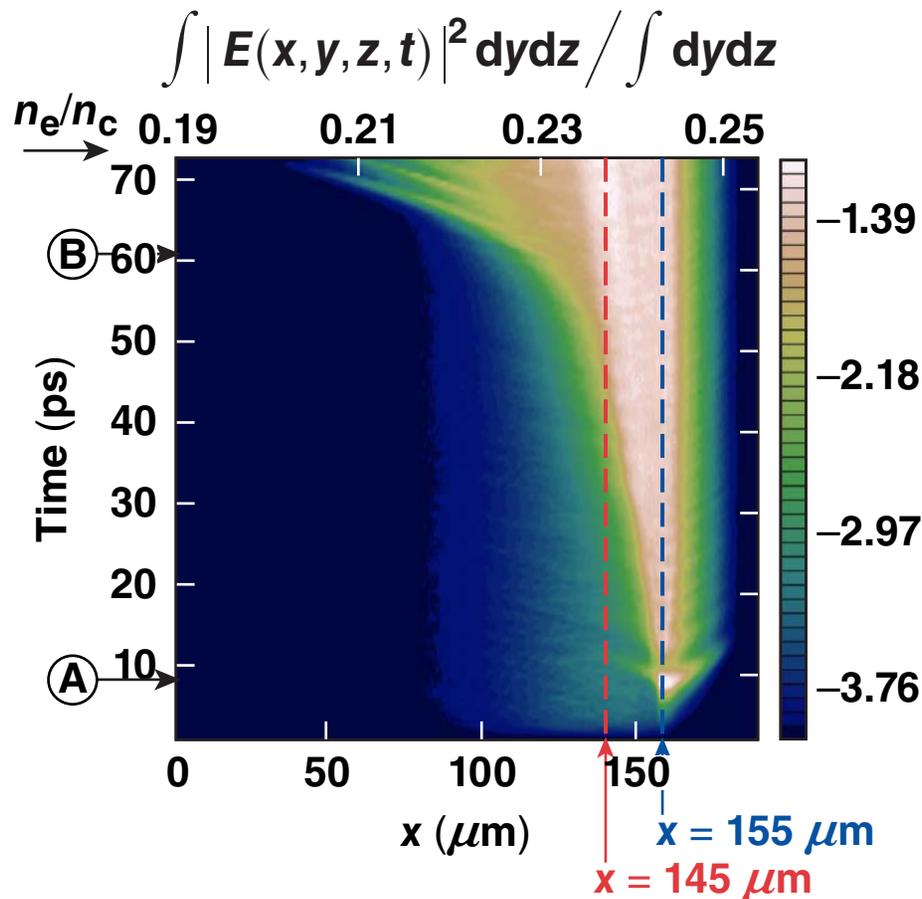
Comparison between ZAK3D and convective gain for four beams with parallel polarization shows consistency for large k



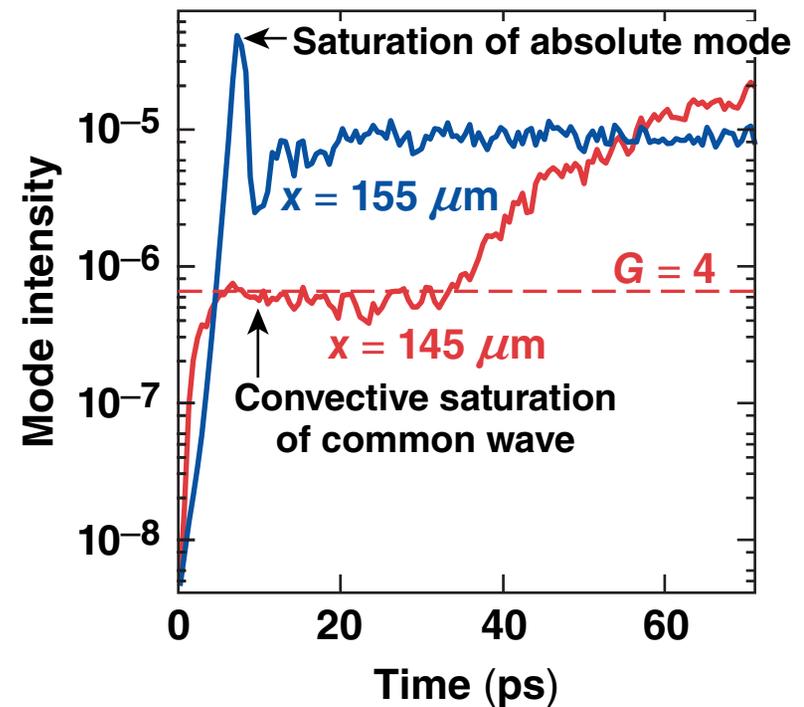
The presence of absolute instability requires a treatment of nonlinear saturation.

In the nonlinear stage, a state of nonlinear Langmuir wave turbulence propagates to lower densities

- TPD driven by two beams with in-plane polarization (*p*-polarized) is simulated in the nonlinear stage $I_{14} = 1.2$, $L_n = 330 \mu\text{m}$, and $\theta = 27^\circ$

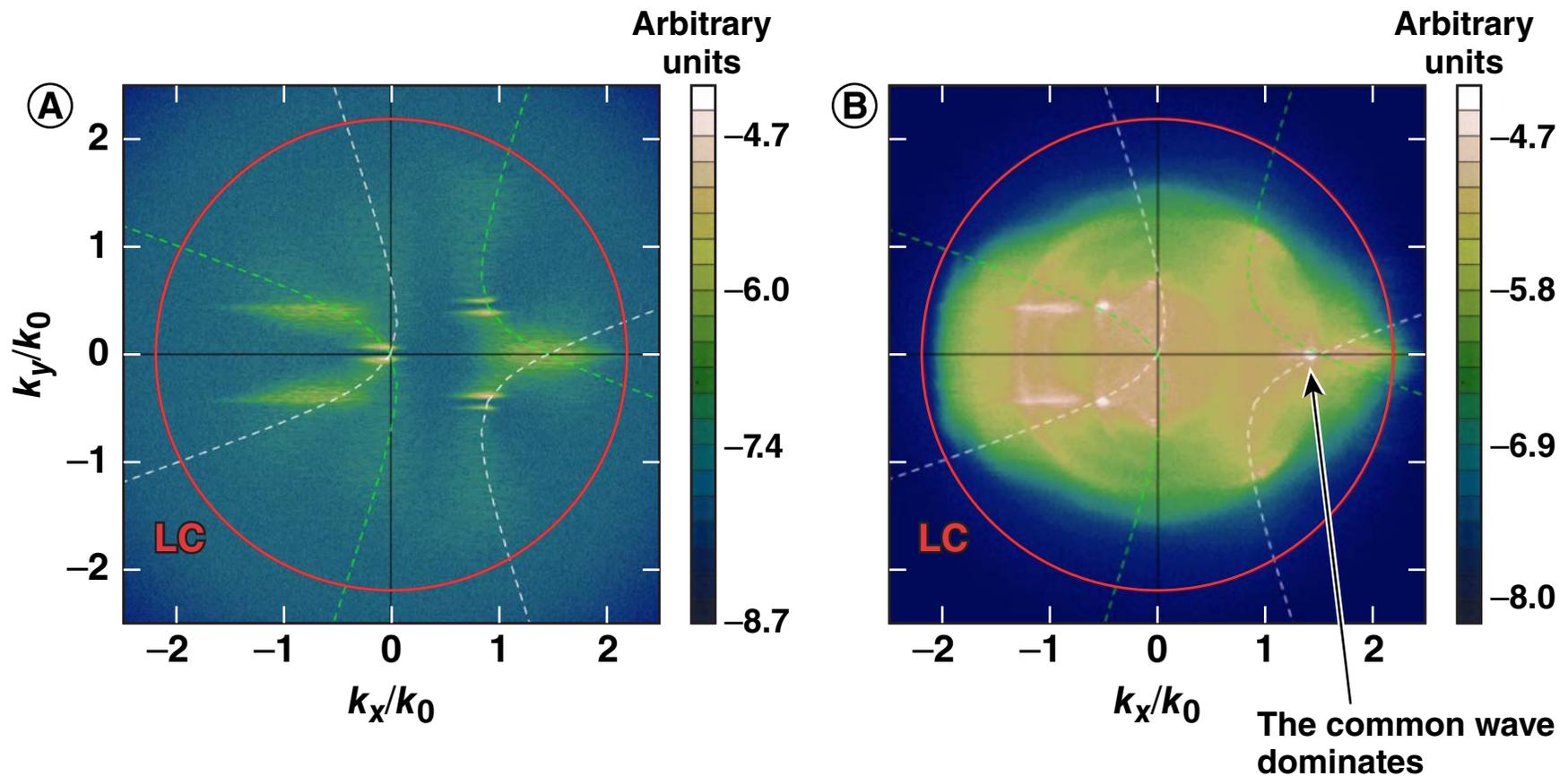


Lineout of energy spectrum at different times



Density perturbations generated by the strong Langmuir turbulence restore growth to the convectively saturated modes; these dominate at late times

- Two beams, p -polarized, $I_{14} = 1.2$, $L_n = 330 \mu\text{m}$, and $\theta = 27^\circ$



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The Langmuir wave equation is formally equivalent to the fluid equations used by Liu[†] and Simon[‡]

Fourier transforming the Langmuir wave (LW) equation in time and space, after simple derivation it leads to these $N + 1$ equations

$$\left\{ \begin{array}{l} [2\omega_{pe0} (\omega - \Delta\omega/2) - 3k^2 V_{te}^2] u + \frac{i\omega_{pe0}^2}{L} \left(\frac{\partial u}{\partial k_x} - \frac{k_x}{k^2} u \right) \\ = \sum_{m=1}^N \frac{\omega_{pe0}}{4} \left(\frac{k^2}{k_{d,m}^2} - 1 \right) (\vec{k} \cdot V_{0,m}) u_{d,m}^* \\ [2\omega_{pe0} (\omega_d + \Delta\omega/2) + 3k_{d,m}^2 V_{te}^2] u_{d,m}^* - \frac{i\omega_{pe0}^2}{L} \left(\frac{\partial u_{d,m}^*}{\partial k_x} - \frac{k_{xd,m}}{k_{d,m}^2} u_{d,m}^* \right) \\ = \frac{\omega_{pe0}}{4} \left(\frac{k_{d,m}^2}{k^2} - 1 \right) (\vec{k} \cdot V_{0,m}^*) u \end{array} \right.$$

where $\omega_{d,m} = \omega - \omega_{0,m}$, $k_{d,m} = k - k_{0,m}$, $u_{d,m} = u - u_{0,m}$
 V_0 is the electron oscillation velocity in laser field

[†]C. S. Liu and M. N. Rosenbluth, Phys. Fluids 19, 967 (1976).
[‡]A. Simon et al., Phys. of Fluids 26, 3107 (1983).