

Extracting “dark matter” volume density information at NIF



P-23 Advanced Imaging Team, LANL

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D. Casey, D. Fittinghoff, G. Grim**

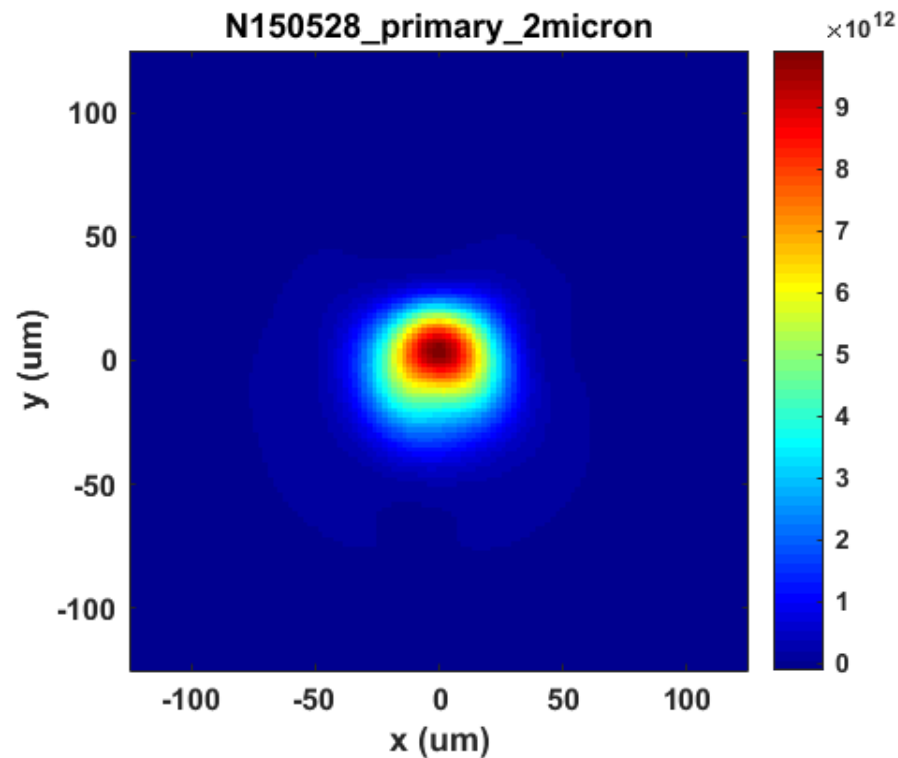


CEA-NNSA Joint Diagnostic Meeting
June 29-30, 2016

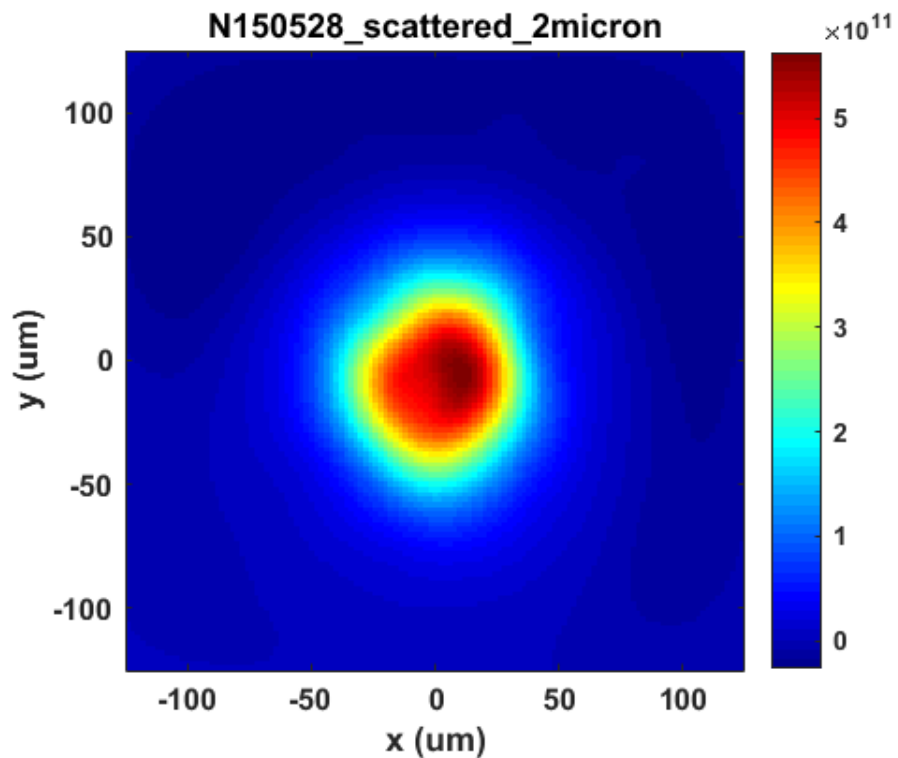
Outline

- **Cold fuel density reconstruction from primary and scattered neutron images**
 - Single scatter model
 - Experimental data reconstruction
 - 3D reconstruction
- **Gamma images analysis and reconstruction**
 - Noise analysis
 - Experimental data reconstruction
 - Statistical tests

NIS: Primary and down-scattered images



Energy range > 13 MeV



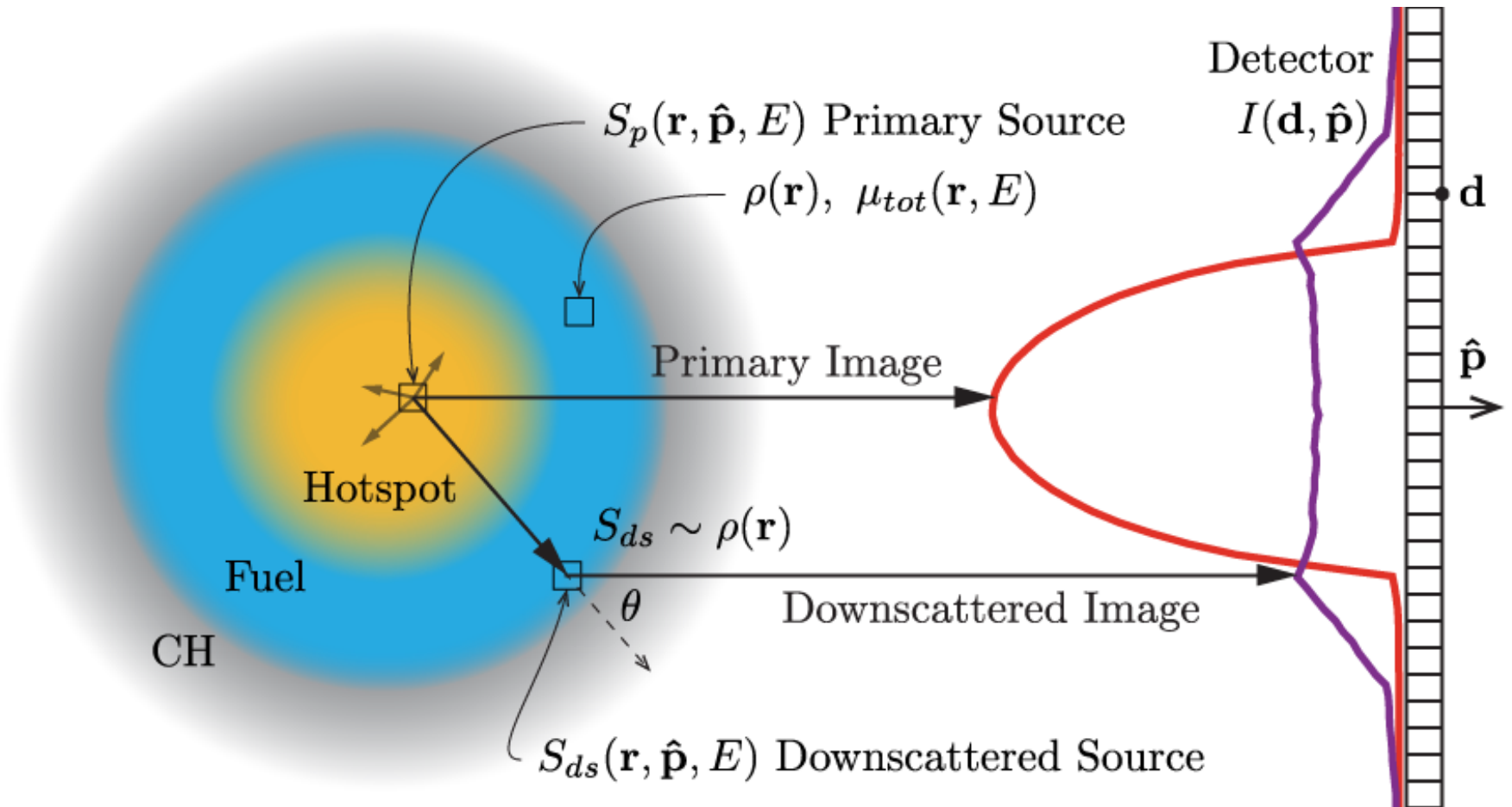
Energy range [6..12] MeV

Can we extract cold-fuel volume density from those images?

THEORY/ALGORITHM

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Down-Scattered Image Formation



$$I_{ds}(\mathbf{d}, \hat{\mathbf{p}}) = \Delta a / L^2 \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \rho(\mathbf{d} + \xi \hat{\mathbf{p}}) \Phi(\mathbf{d} + \xi \hat{\mathbf{p}}, \hat{\mathbf{p}}) \tau_{ds} d\xi$$

$$\Phi(\mathbf{r}, \hat{\mathbf{p}}) = N A / m a \int_0^{\infty} \int_{\Omega} \int_{\Omega} S_p(\mathbf{r}', E) \int_0^{\infty} D(E') A(\mathbf{r}, \hat{\mathbf{p}}, E') d\sigma_{sc}(E, \theta, E') / d\Omega$$

$$A(\mathbf{r}, \hat{\mathbf{p}}, E) = \int_{\Omega} \int_{\Omega} A(\mathbf{r}, \hat{\mathbf{p}}, E) / |\mathbf{r} - \mathbf{r}'|^2 dE' d\Omega' r' dE$$

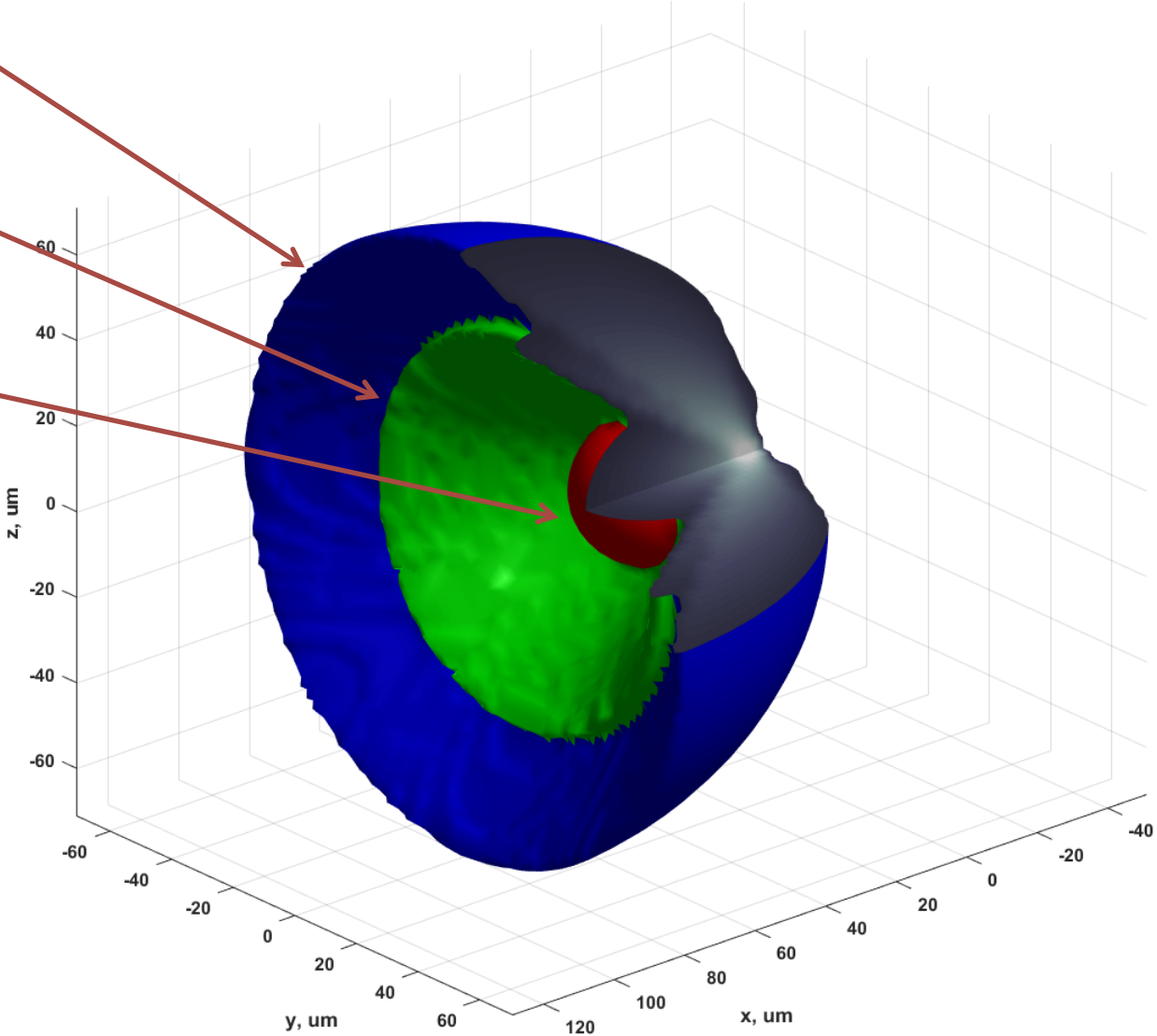
Down-scattered image projection kernel $\phi(\mathbf{r}, \mathbf{p})$ for a point primary source

Down-scattered neutrons: 6.0 .. 12.0 MeV

$T(n,elastic)$

$D(n,elastic)$

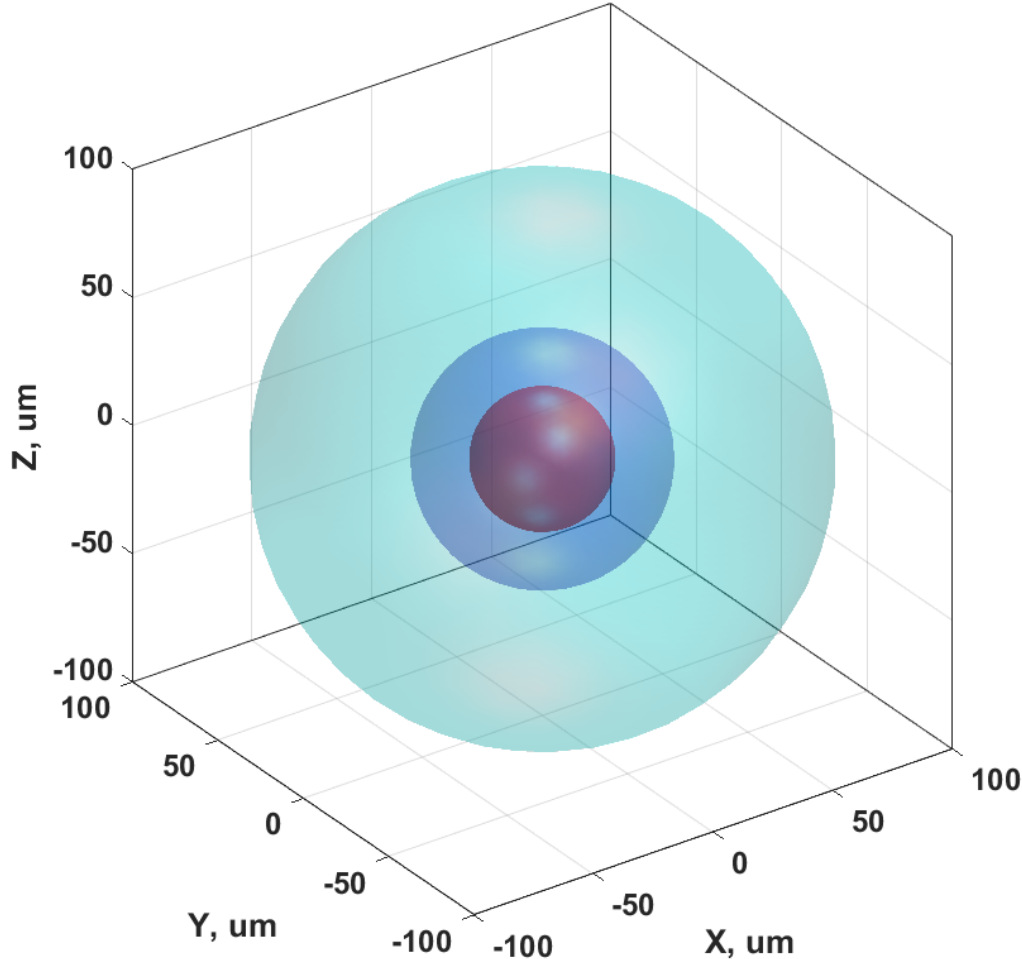
$D(n,2n)$



MCNP SIMULATION

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MCNP Simulation



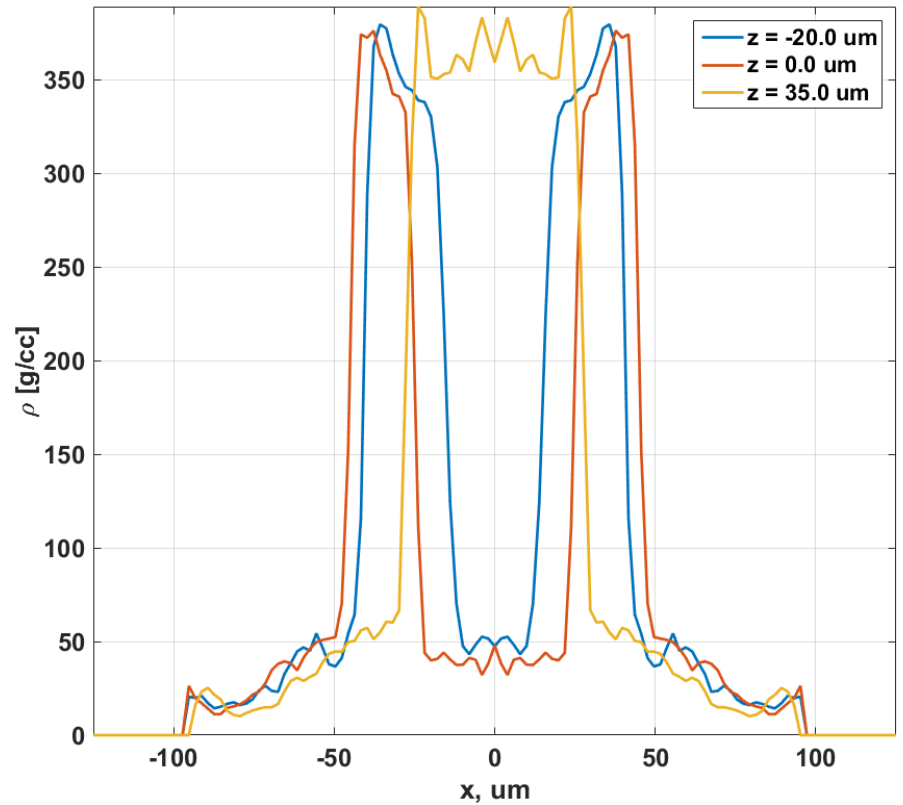
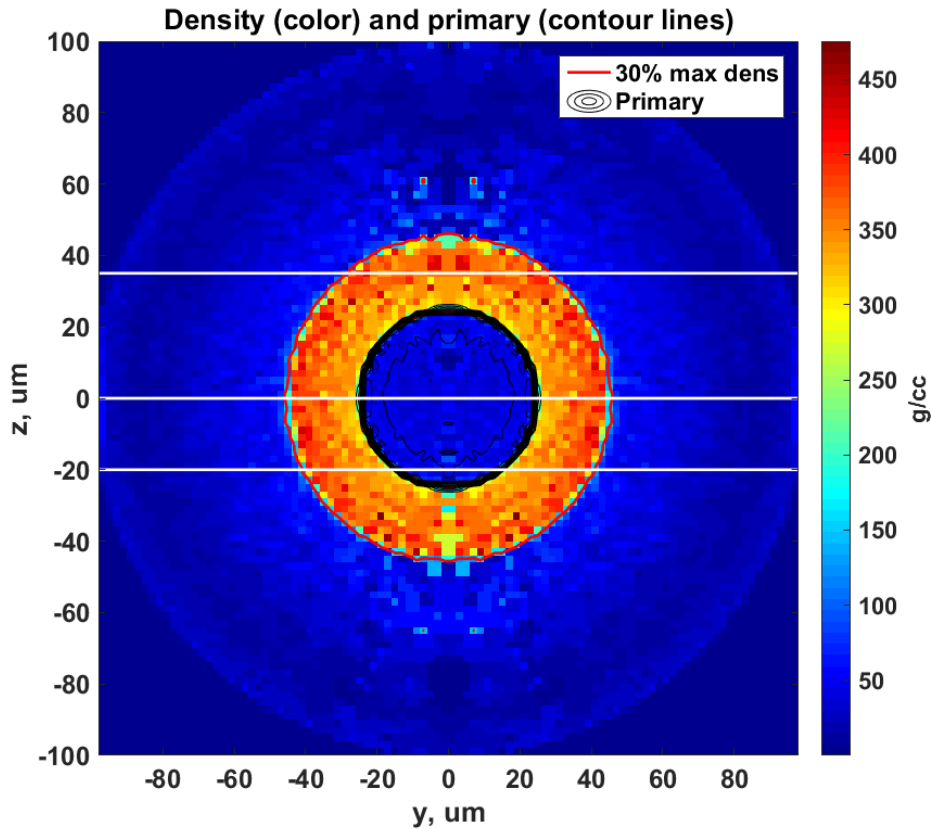
“Hot spot” (magenta):
radius = 25 μm ,
material 50%D + 50%T,
density 25 g/cc,
emission = $1 \cdot \text{TotalYield} / \text{Volume} / 4\pi$

DT shell (blue):
thickness = 20 μm ,
material 50%D + 50%T,
density 350 g/cc,
emission = 0

CH shell (cyan):
thickness = 55 μm ,
material 50%C + 50%H ,
density tapering from 150g/cc at 45
 μm to 30g/cc at 100 μm ,
emission = 0

Total mass of DT = 112 μg

Density reconstruction

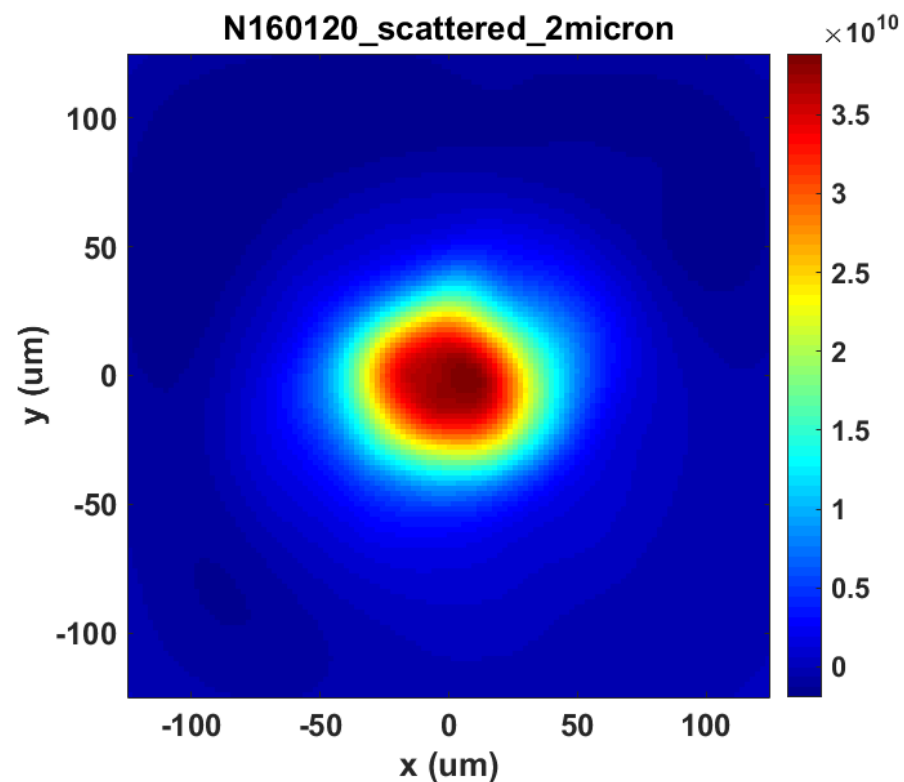
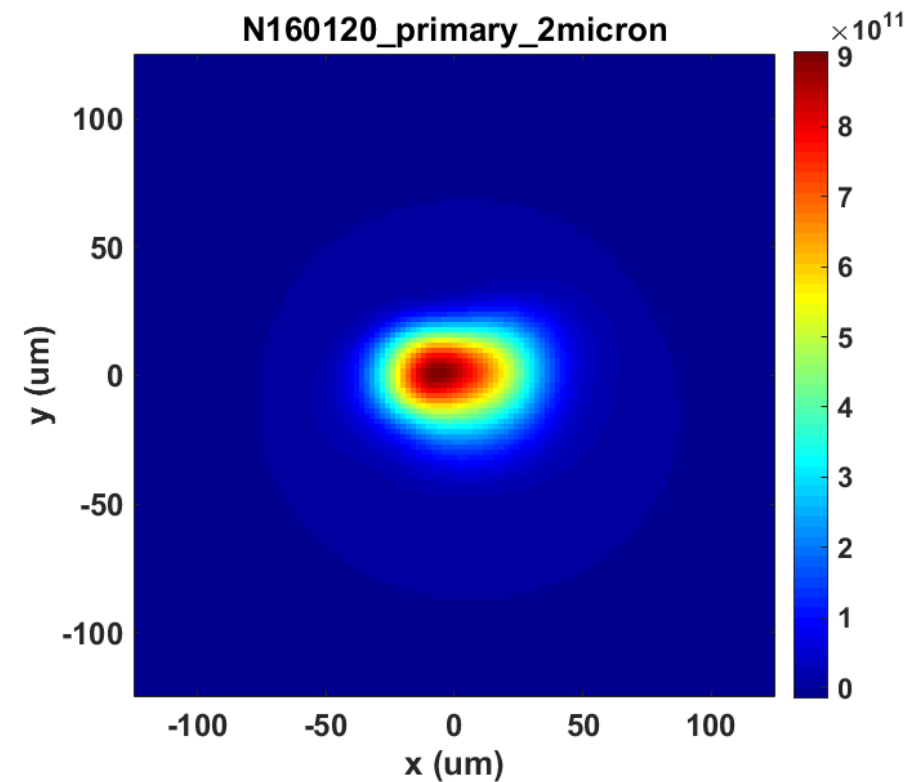


Total reconstructed mass of DT (inside 30% level) = 114 μg (exact value 112 μg)

EXPERIMENTAL DATA RECONSTRUCTION

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N160120



	P_0 (μm)	P_2/P_0 (%)	P_3/P_0 (%)	P_4/P_0 (%)
Primary (13..17 MeV)	33.40	-23%	-6%	1%
Down-scattered (6..12 MeV)	49.58	-12%	-2%	2%

Attempt to account for L-R asymmetry

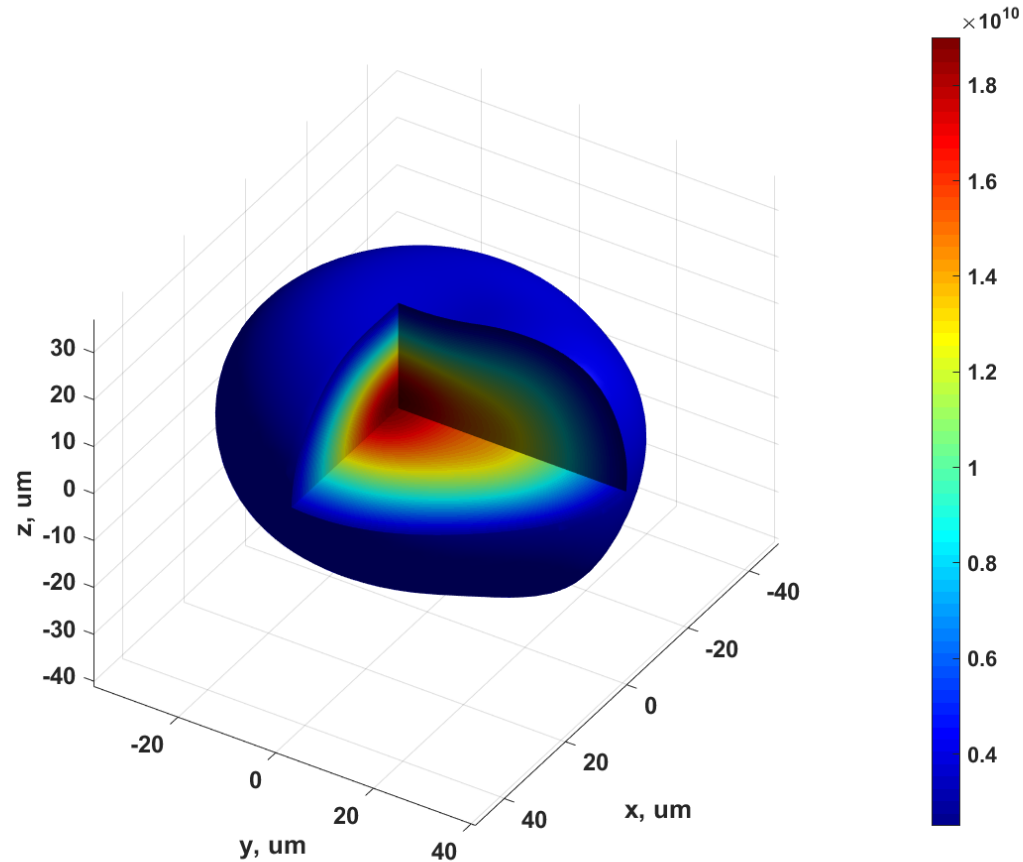
The method requires inferring 3D distribution of the primary source.

For equatorial views spherical harmonics decomposition reduces to polar Fourier transform:

$$S(\rho, \varphi, z) = \sum_{m=-N}^N S_l^m(\rho, z) e^{im\varphi}$$

Given one projection direction this results in first order polar Fourier transform:

$$S(\rho, \varphi, z) = S_l^1(\rho, z) \frac{1 - \sin\phi}{2} + S_l^0(\rho, z) \frac{1 + \sin\phi}{2}$$

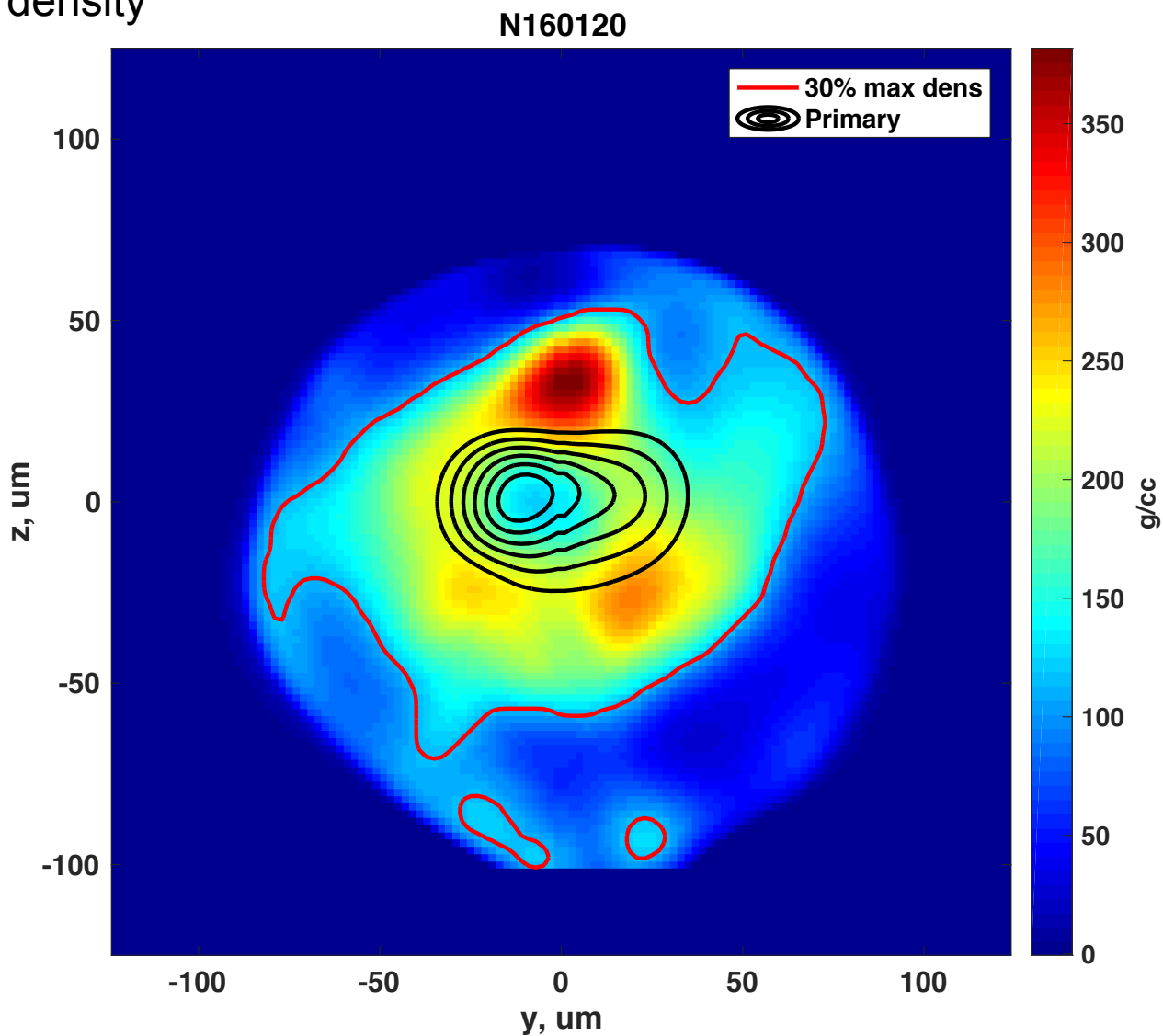


N160120: Reconstructed "hot spot"

N160120: Reconstructed density

Reconstructed density with overlaid reconstructed primary contour.

Reconstructed Mass:
313 μg (total),
174 μg (inside 30% level)



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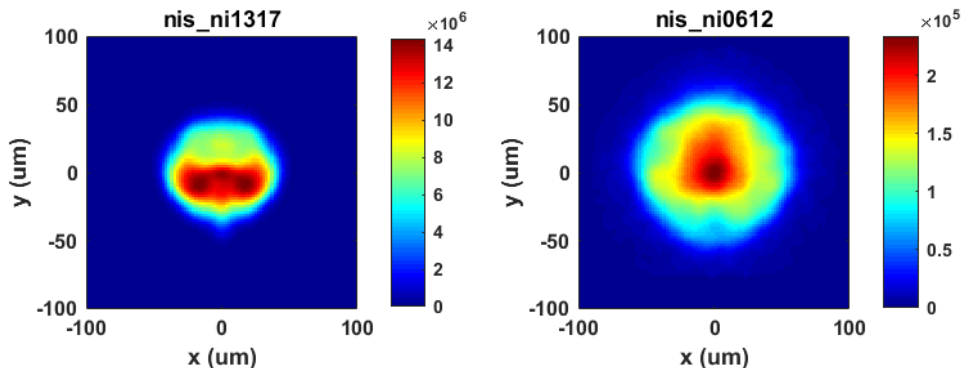
$S(x,y,z)$

3D RECONSTRUCTION

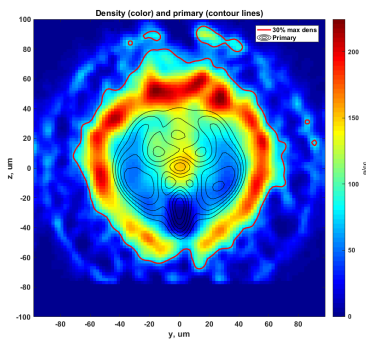
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LLNL: Brian's "Turkey shot" 3D simulation

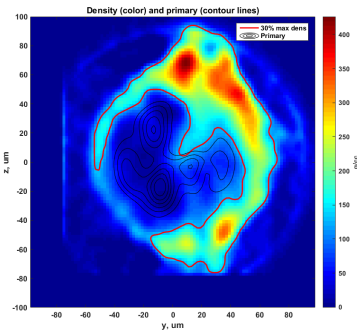
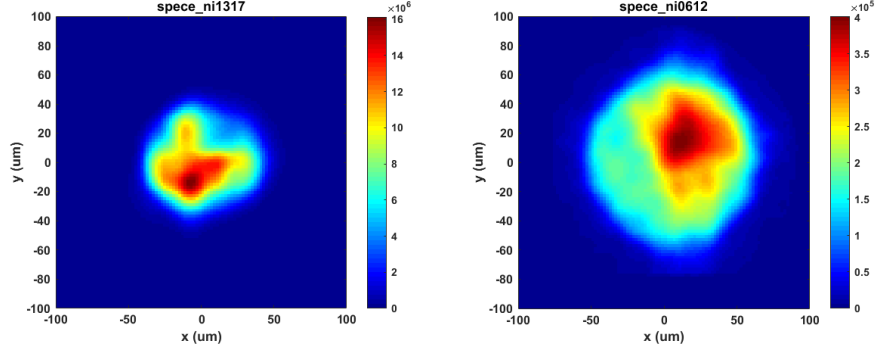
NIS line-of sight: (90, 315)



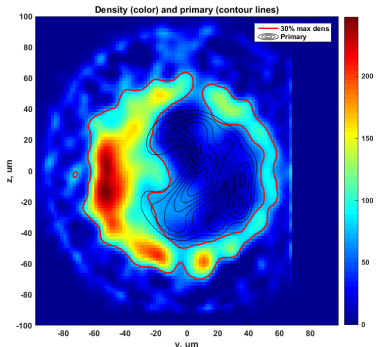
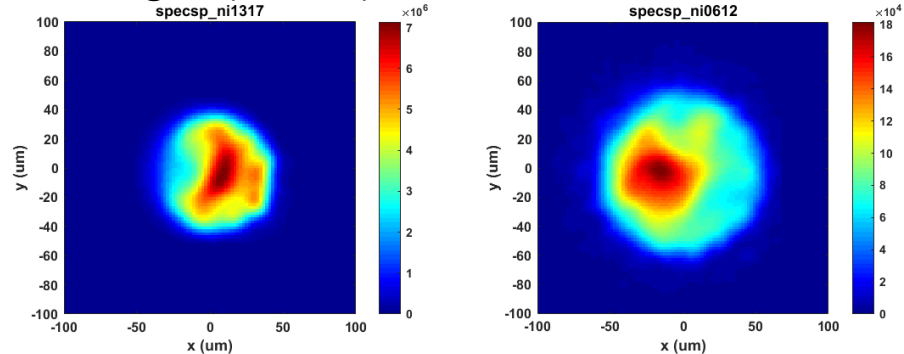
Density



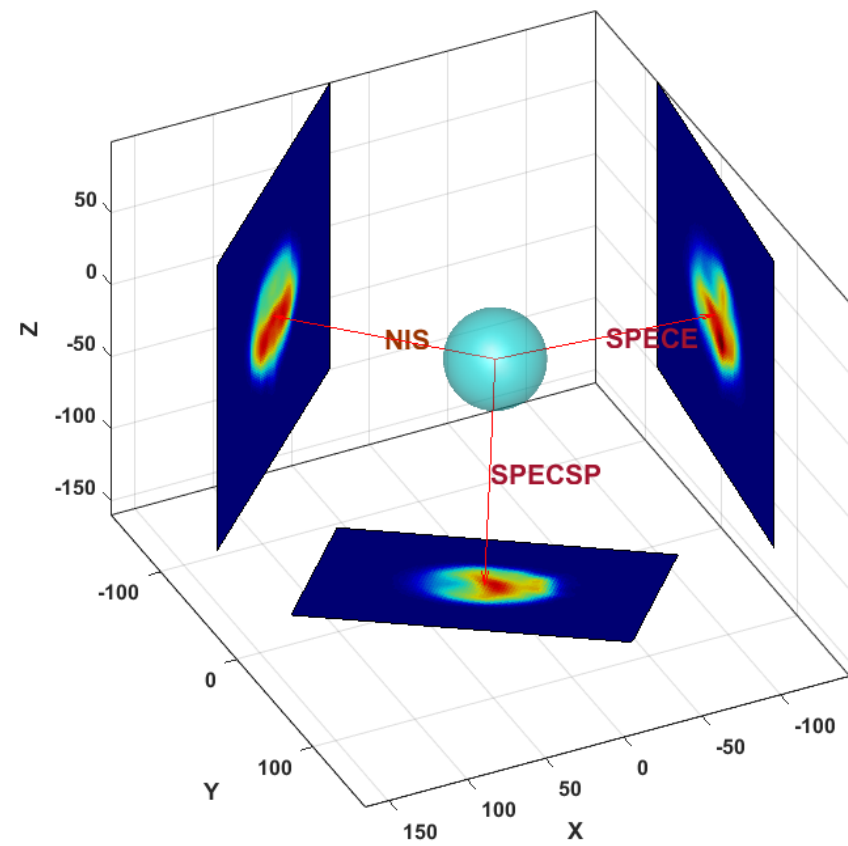
SPECE line-of sight: (90, 174)



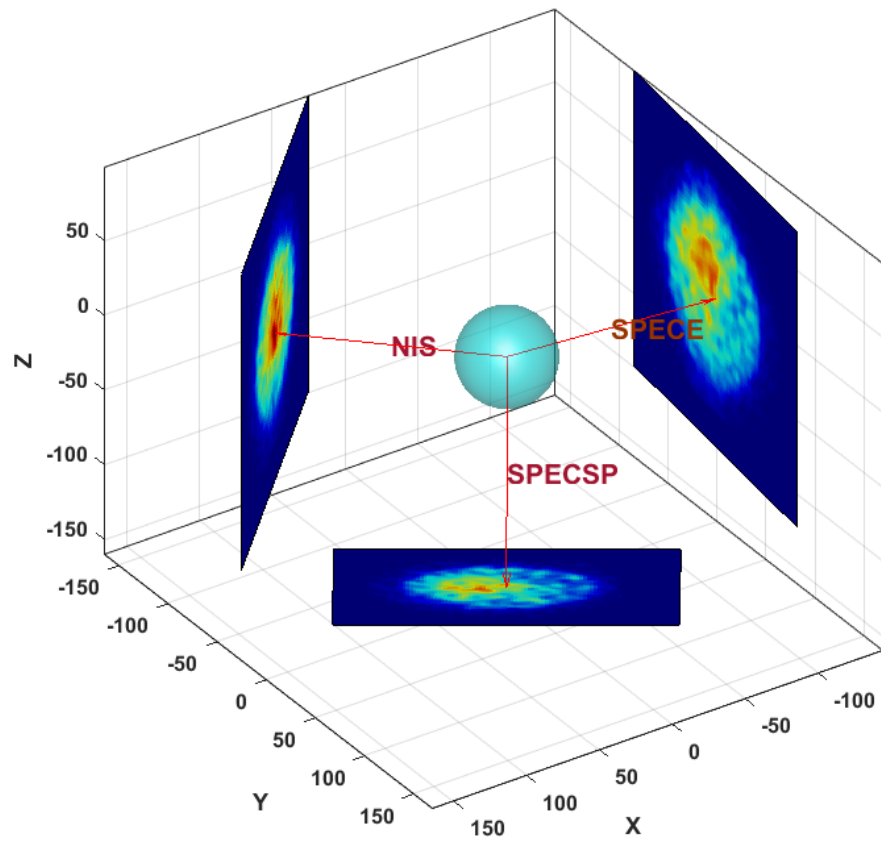
SPECSP line-of sight: (161, 56)



3D projections

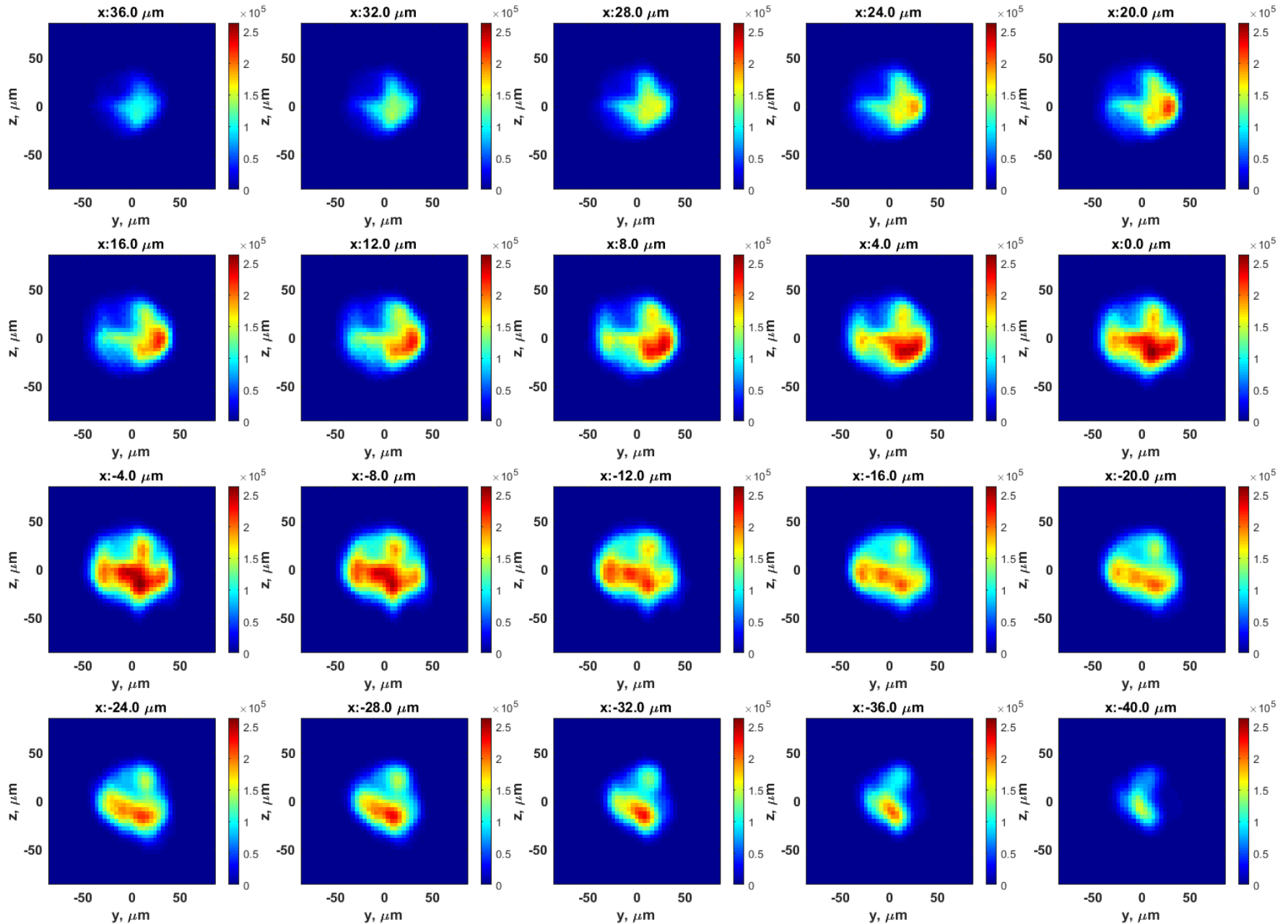


Primary

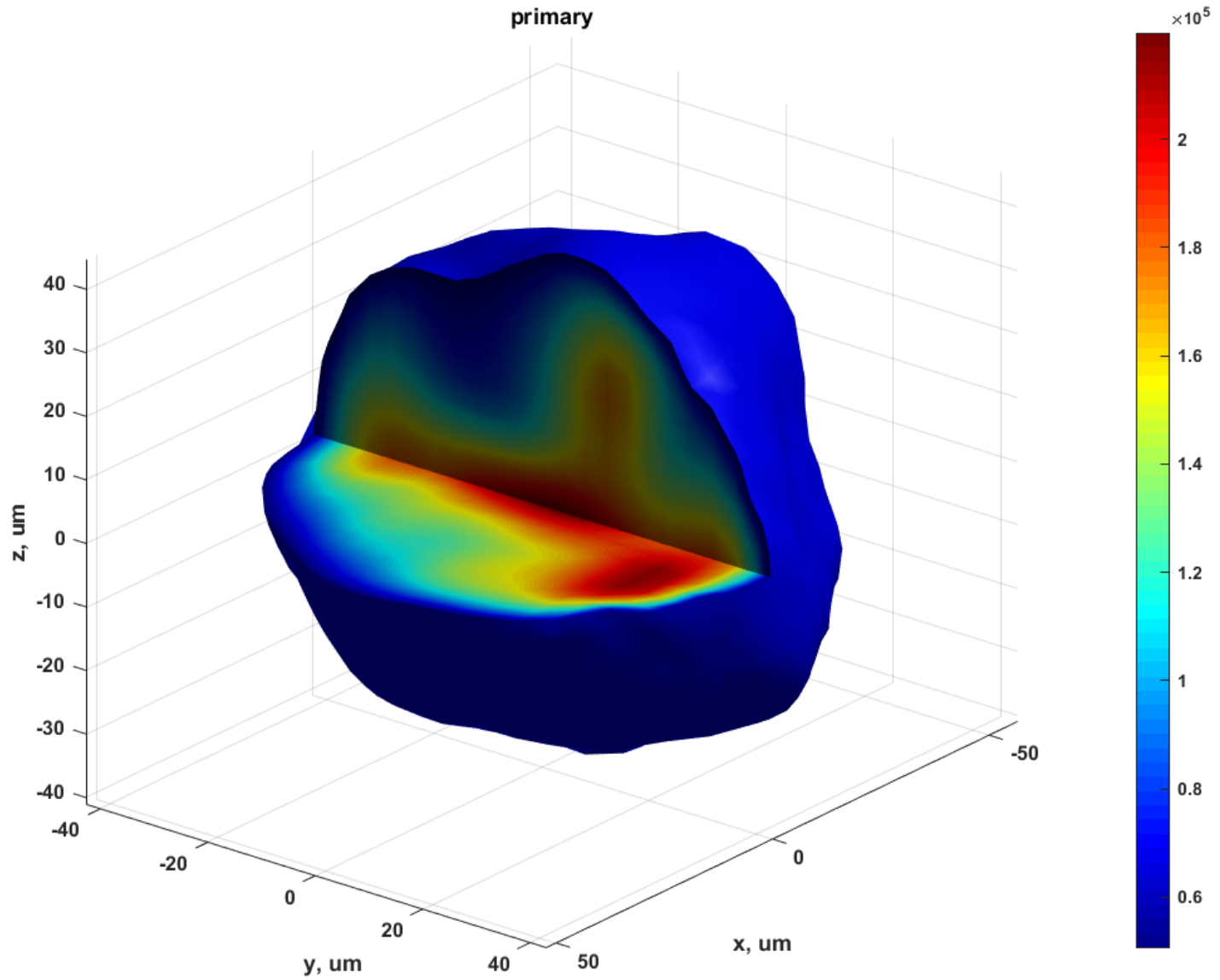


Down-scattered

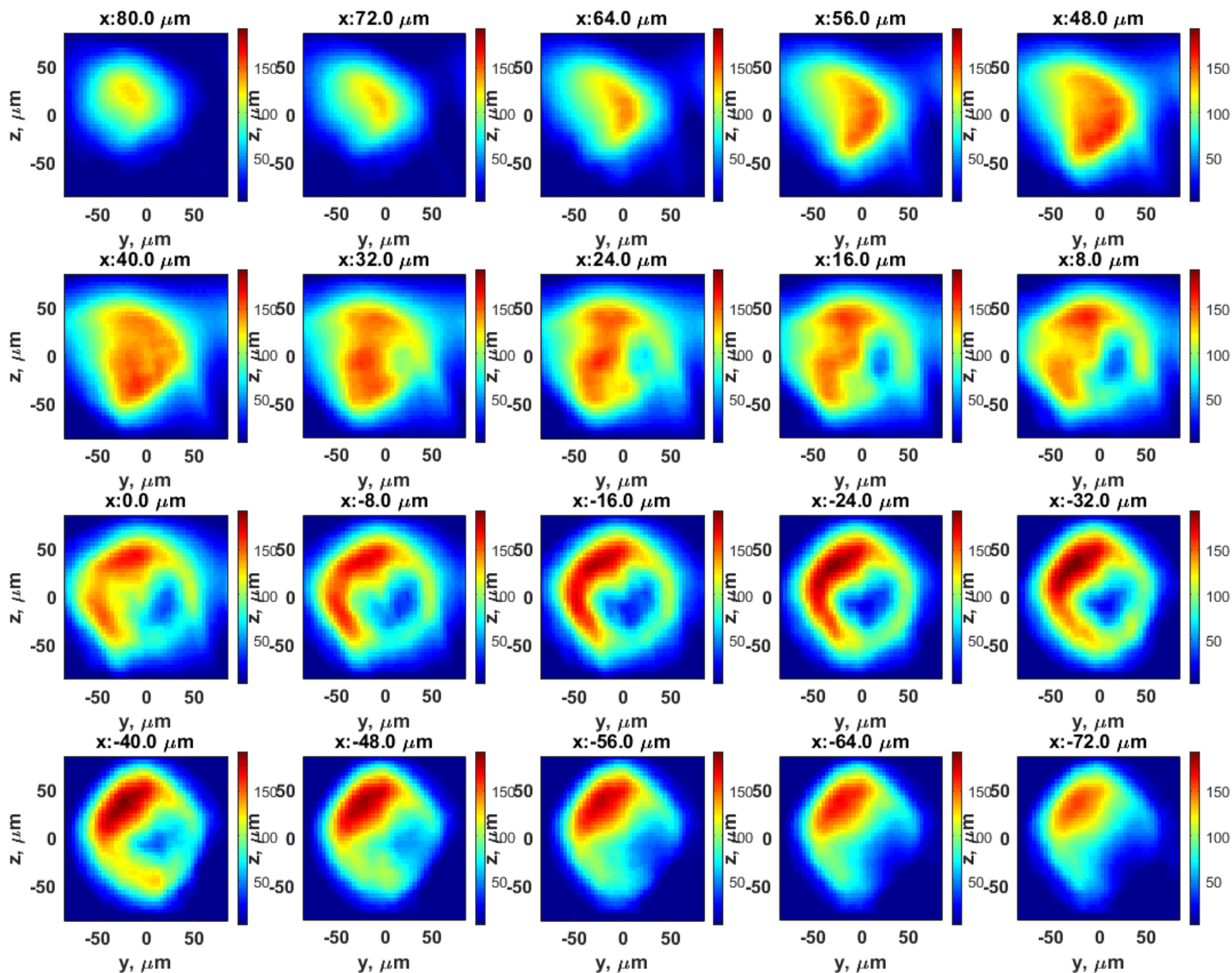
Reconstructed primary source: YZ-slices (i.e. almost orthogonal to SPECE LOS)



Reconstructed primary source



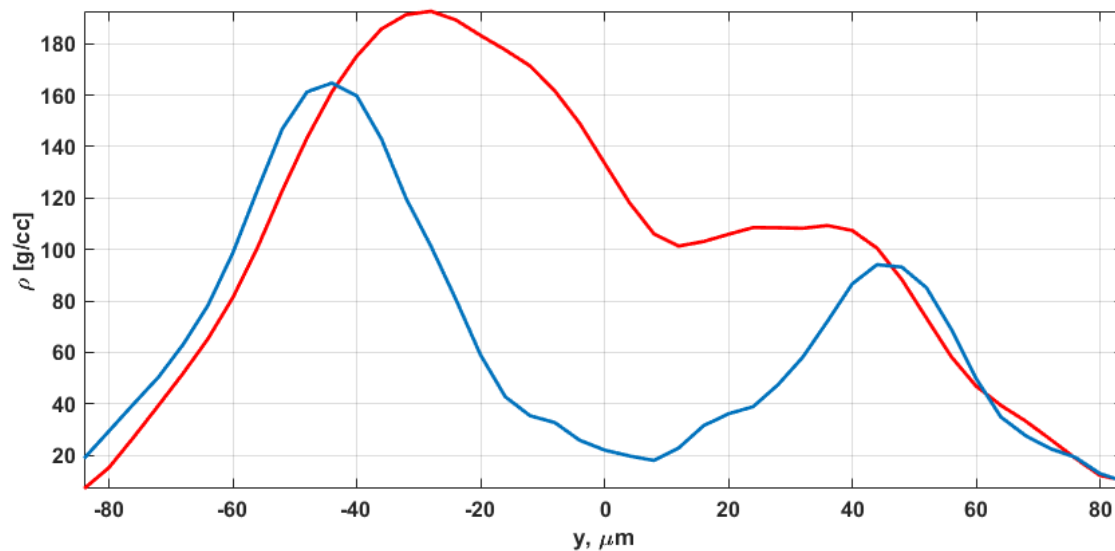
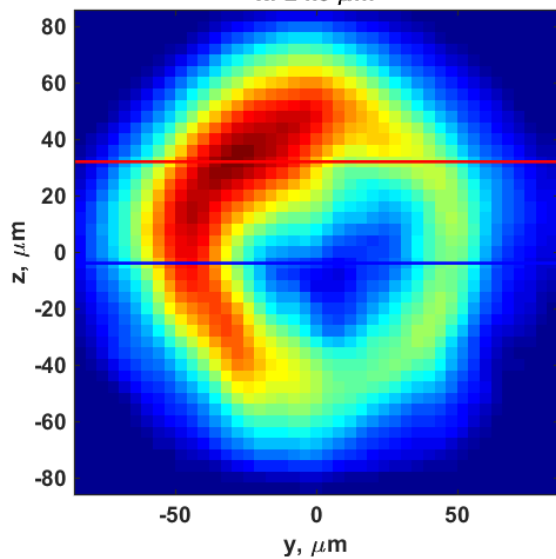
Reconstructed density: YZ-slices (i.e. almost orthogonal to SPECE LOS), color map is



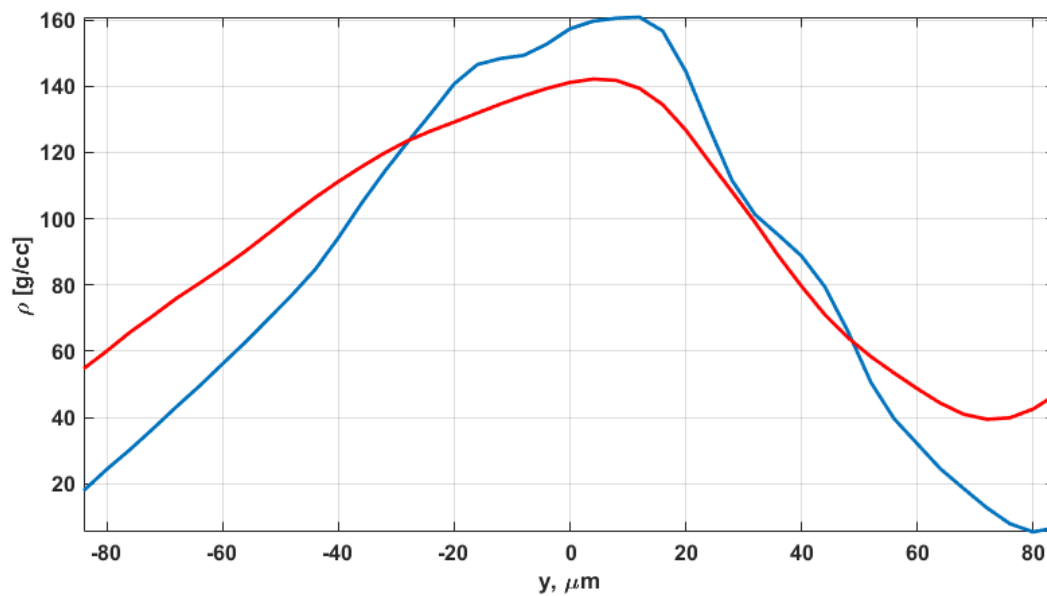
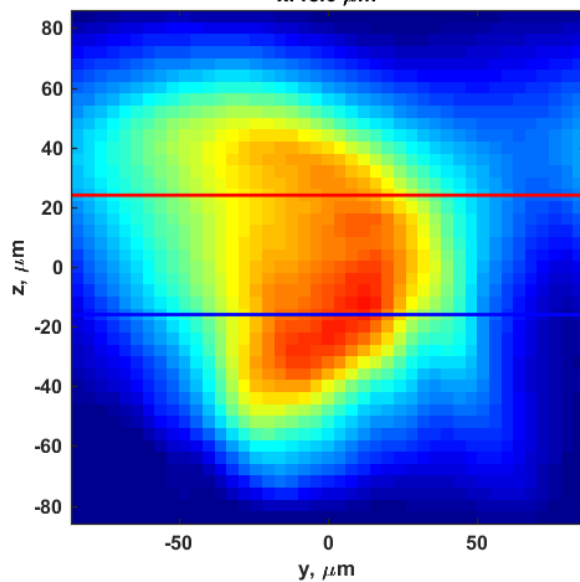
Mass: 258 μg (total), 187 μg (inside 30% level)

Density profiles for representative YZ slices

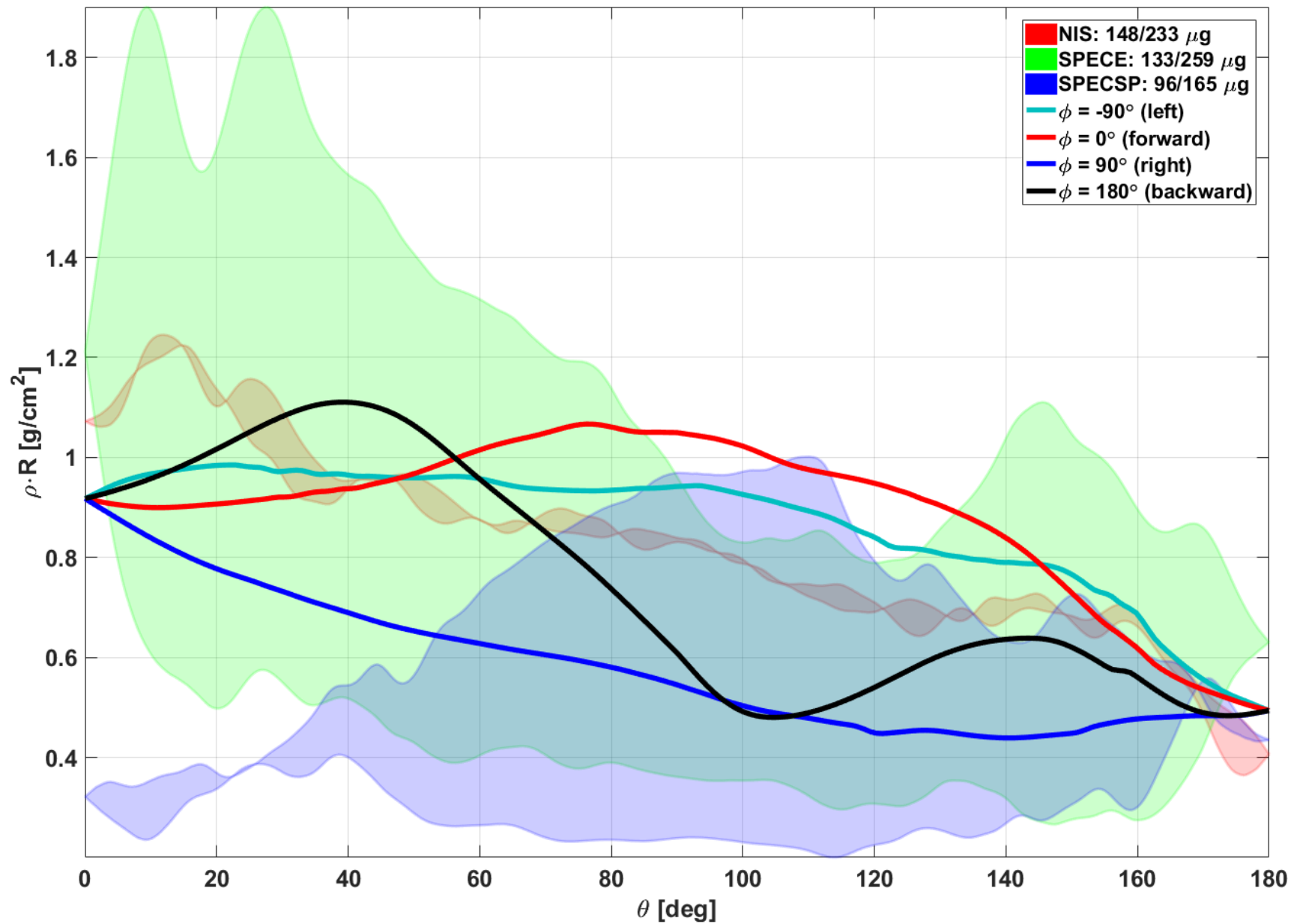
x: -24.0 μm



x: 48.0 μm

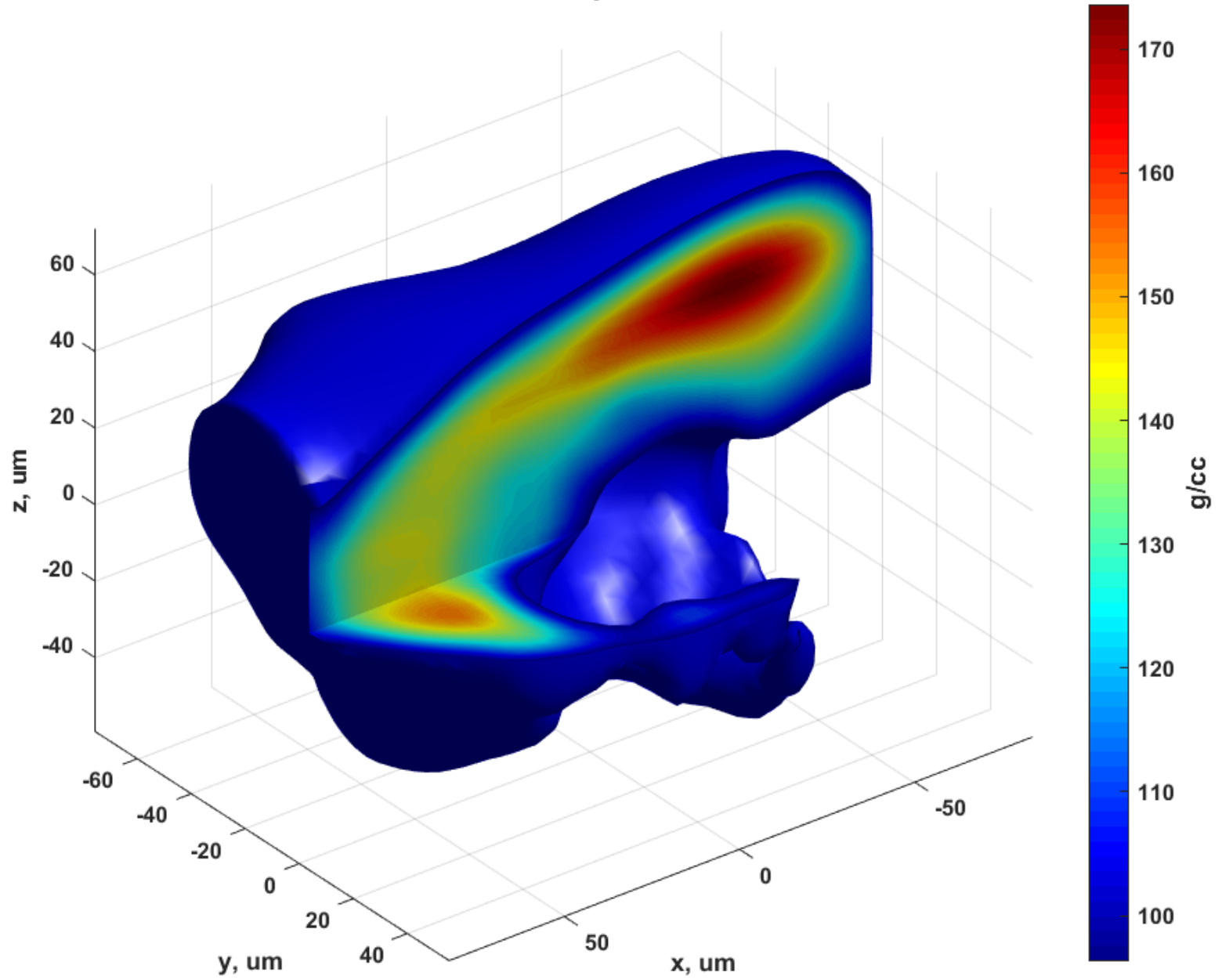


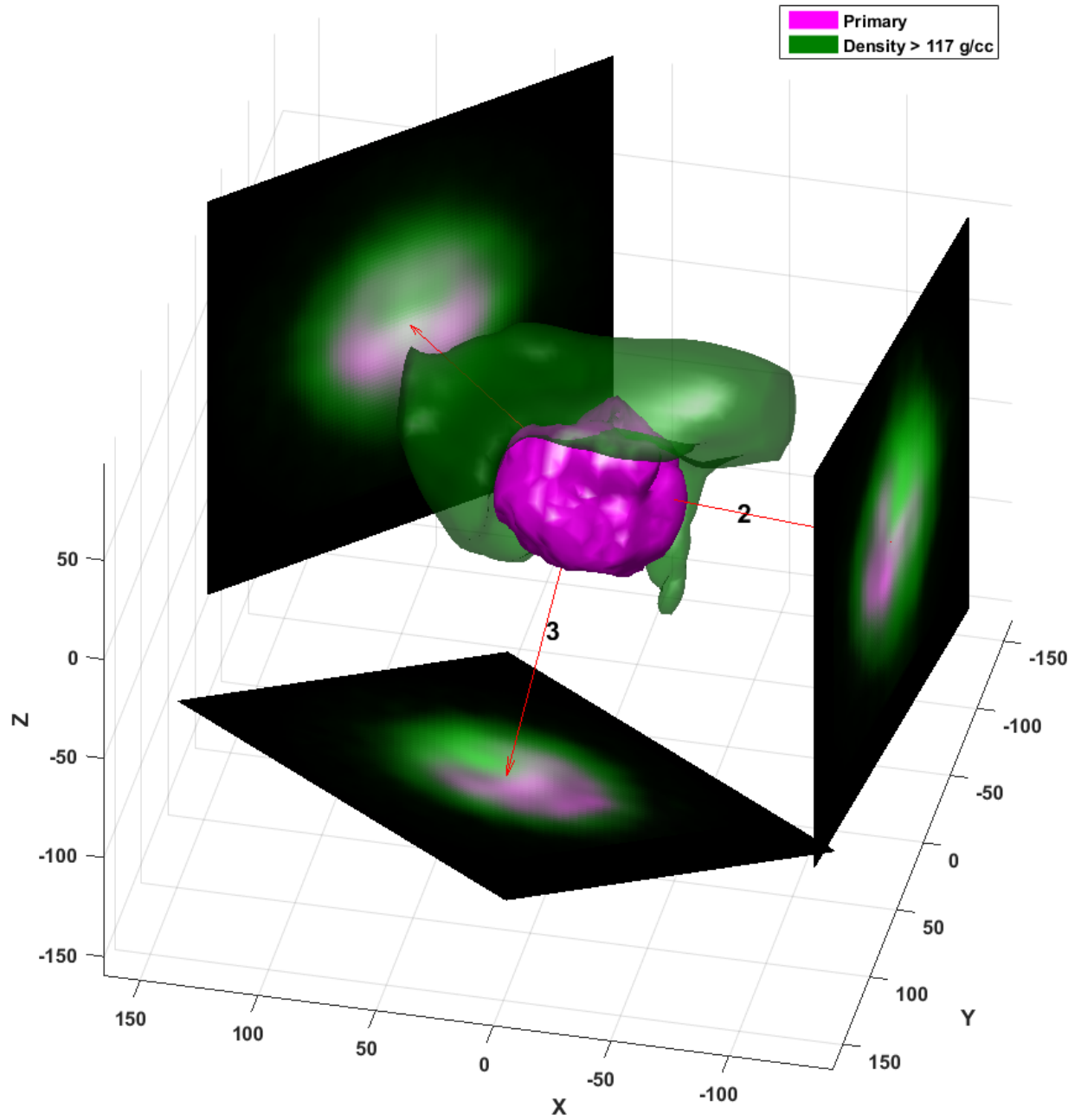
Rho-R as a function of polar angle



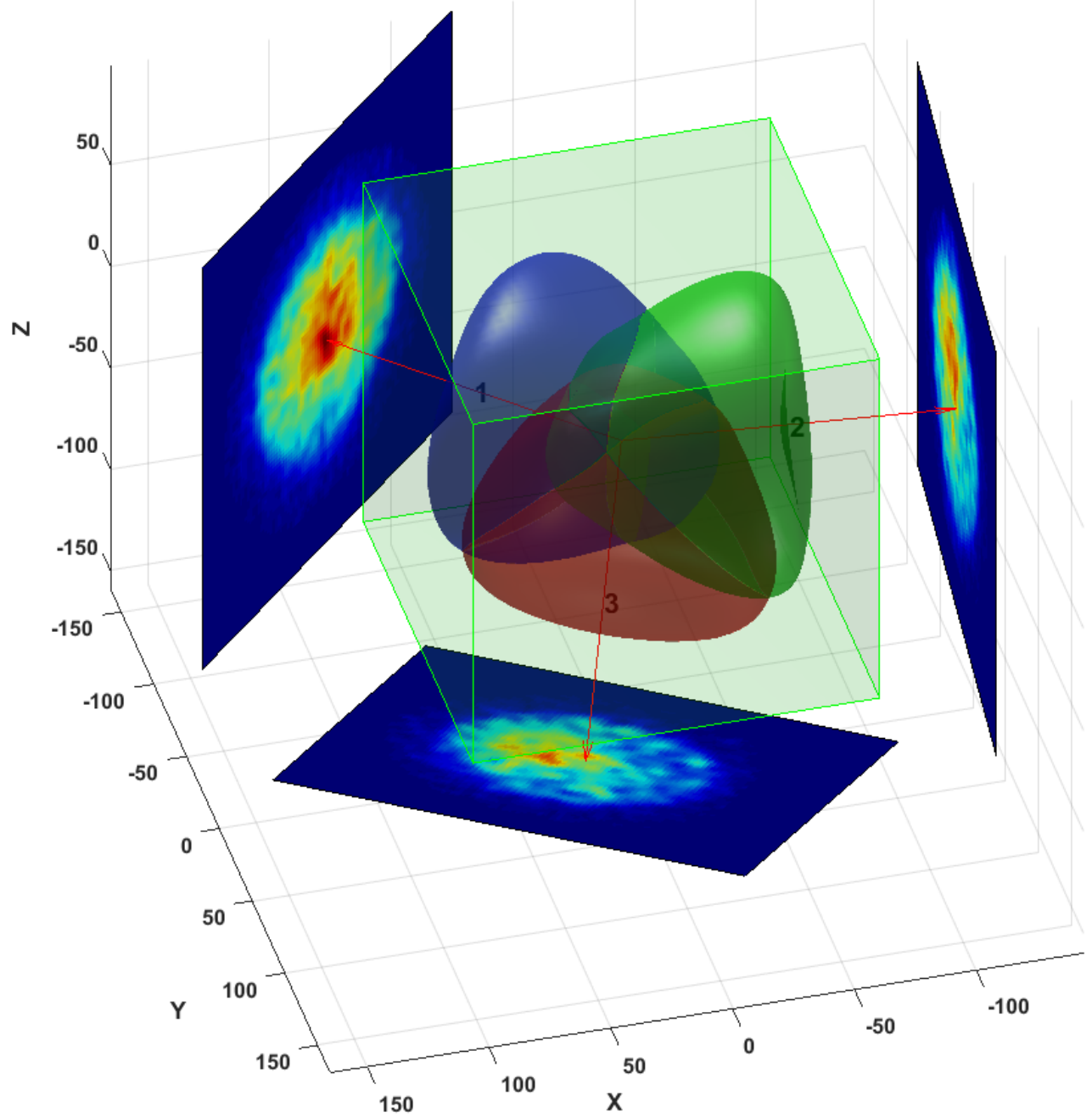
Mass: 258 μg (total), 187 μg (inside 30% level)

density





Down-scattered image projection kernels $\phi(\mathbf{r}, \mathbf{p})$ for the reconstructed primary source



Conclusion & Future Plans

1. A method to reconstruct cold fuel density using a single scattering model has been developed and validated against MCNP model
2. The method provides density in ***physical units***, i.e. g/cc
3. The method applied to the experimental data provided physically plausible and interesting results
4. The method requires inferring 3D distribution of the primary source. Given one projection direction this results in assuming axial symmetry of the reconstructed objects. This could be deceiving for reconstruction of a fuel assembly with this large 3D structure. Multiple views will alleviate this restriction and improve the density reconstruction
5. Source localization, i.e. array characterization, is of paramount importance

Nearest goals:

1. Extensively validate the technique using both simulation and experimental data
2. Develop an iterative procedure to account for the attenuation terms
3. Combine with polar x-ray images in attempt to account for low order asymmetry

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Thank you!
and...
Questions?

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Preliminary analysis of N160602 Gamma Ray Imaging



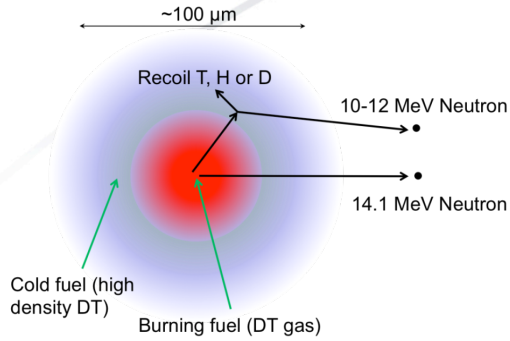
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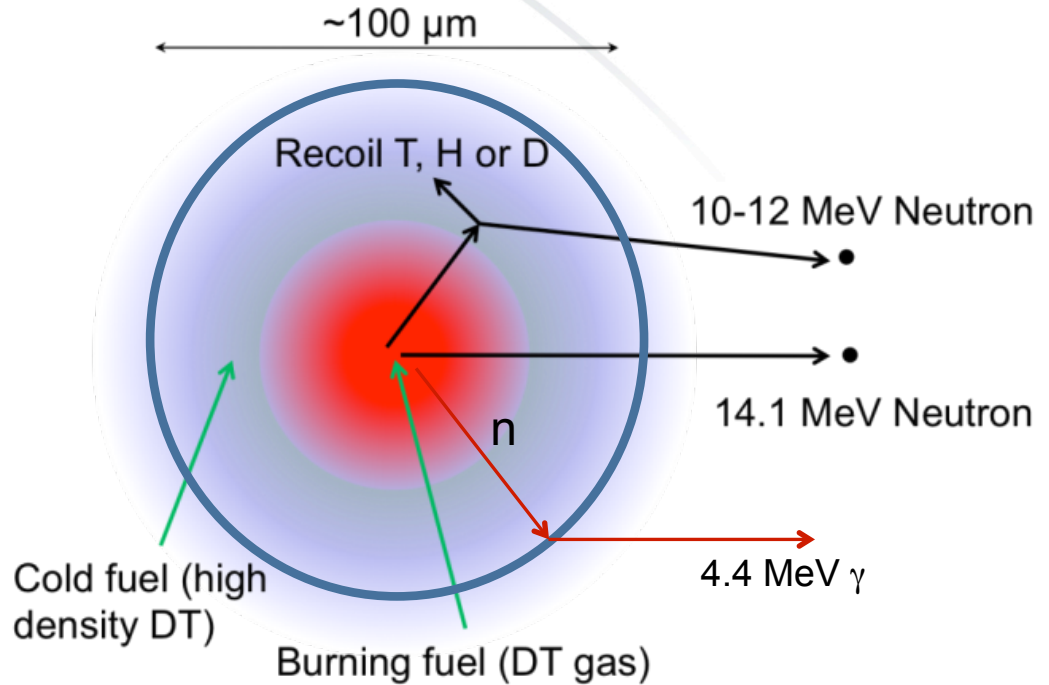
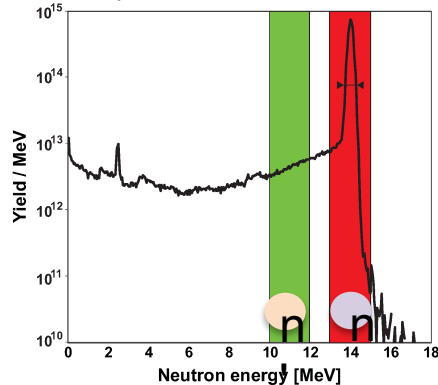
June 21, 2016



Neutron images provide the shape and size of the imploded fuel at stagnation. Gamma imaging can measure the ablator location.



Neutron images are used to diagnose NIF implosions. Temporal separation of neutrons after 28 m drift results in ability to collect two neutron images: Primary (13-17 MeV), Down-Scattered (10-12 MeV)

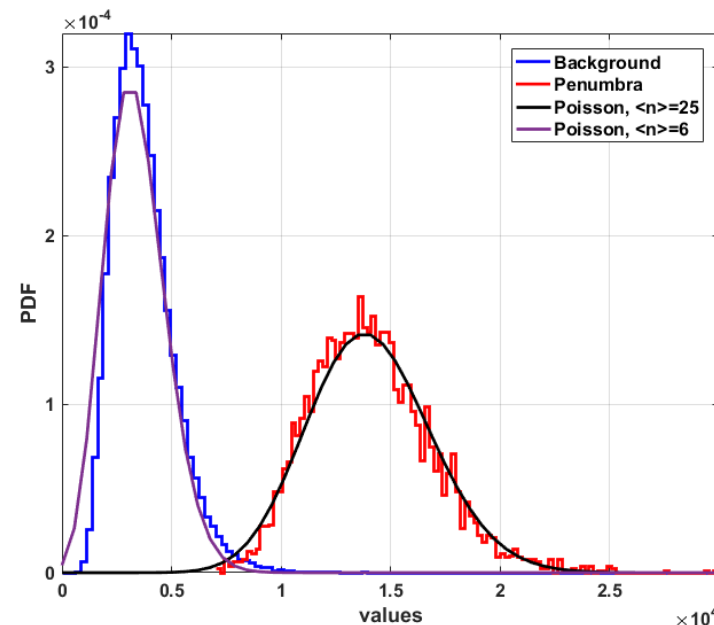
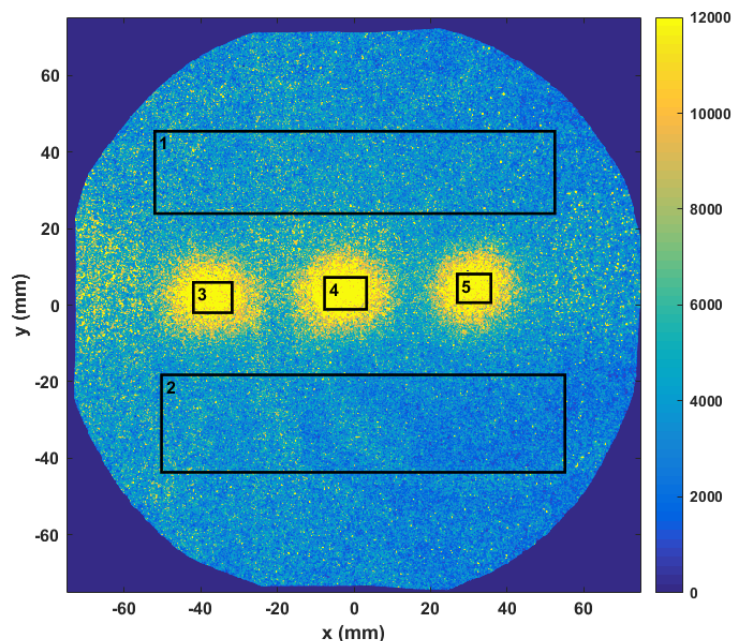


Gamma Ray Imaging

At yields $>10^{16}$ neutrons and sufficient remaining ablator mass there should be enough $\text{C}(n,\gamma)$ reactions to form images of the ablator location.

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Noise analysis of N160602 data (260 micron pixel) indicates higher signal level than expected



No	Background (1,2)	Penumbra (3,4,5)
Mean	3730	14100
STD	1550	2840
SNR	2.4	5.0
$\langle N_V / \text{pixel} \rangle$	~6	~25

Poisson distribution: $P(n|\bar{n}) = \frac{(\alpha\bar{n})^n e^{-\alpha\bar{n}}}{n!}$

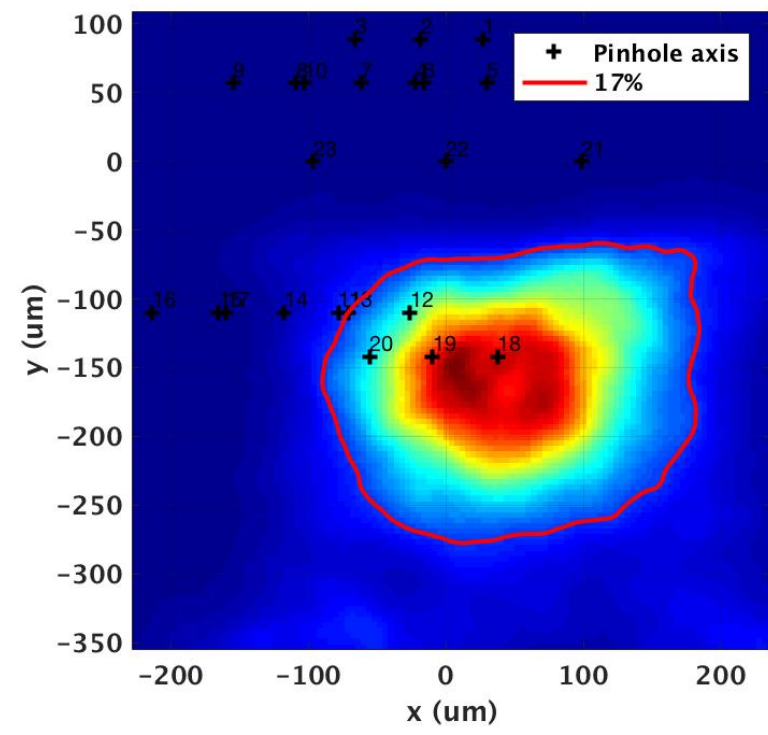
Back of the envelope:

$$N_V \Delta S = \frac{Y_V \Delta S}{4\pi R^2}$$

$Y_n \approx 1.6 \times 10^{15} \Rightarrow Y_V \approx 8 \times 10^{12}$ into 4π
 0.26 mm pixel @ 28 m \Rightarrow ~55 gammas per pixel
 ~15% DQE (plastic scintillator)
 \Rightarrow ~8 gamma per pixel (x2+???)

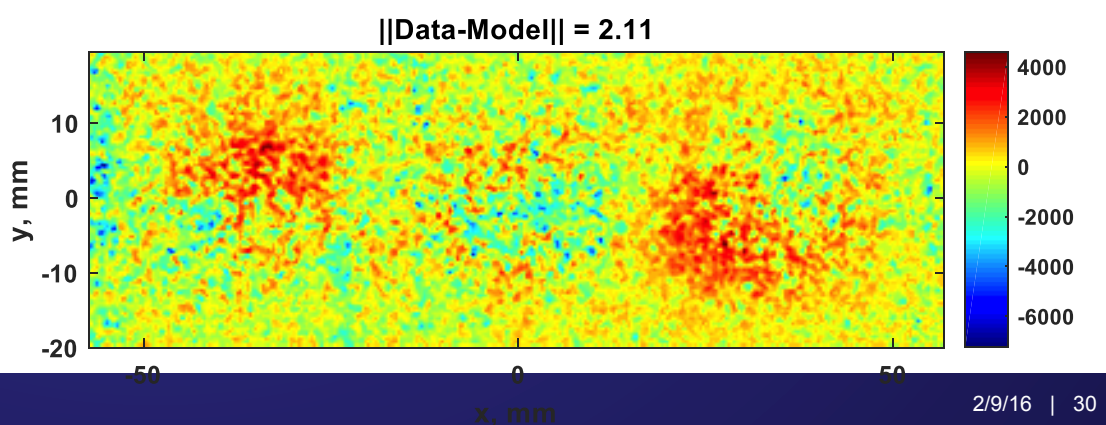
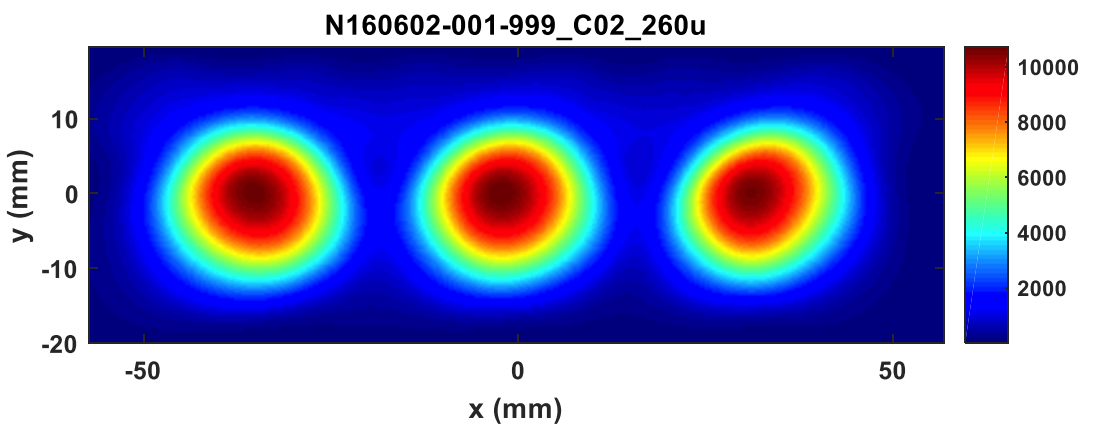
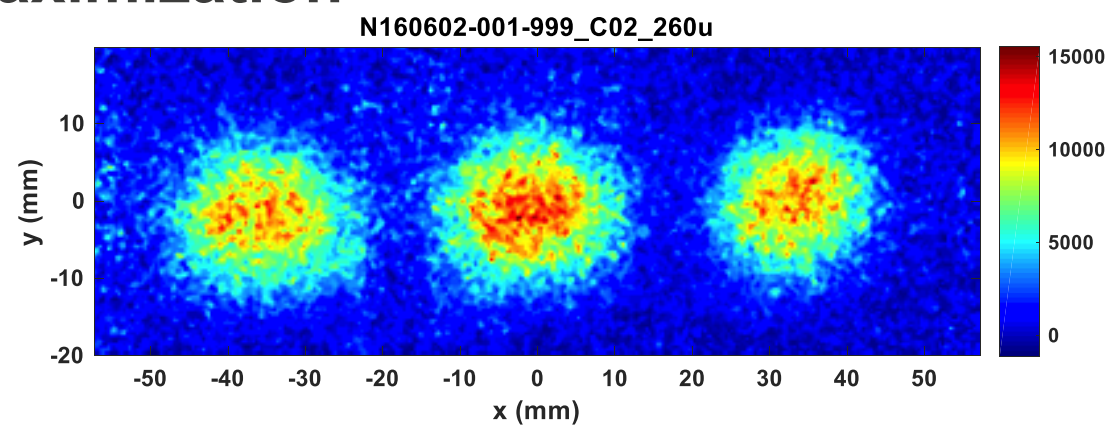
GRH measurement of C-12 gamma would help interpret this data

N160602: Expectation Maximization



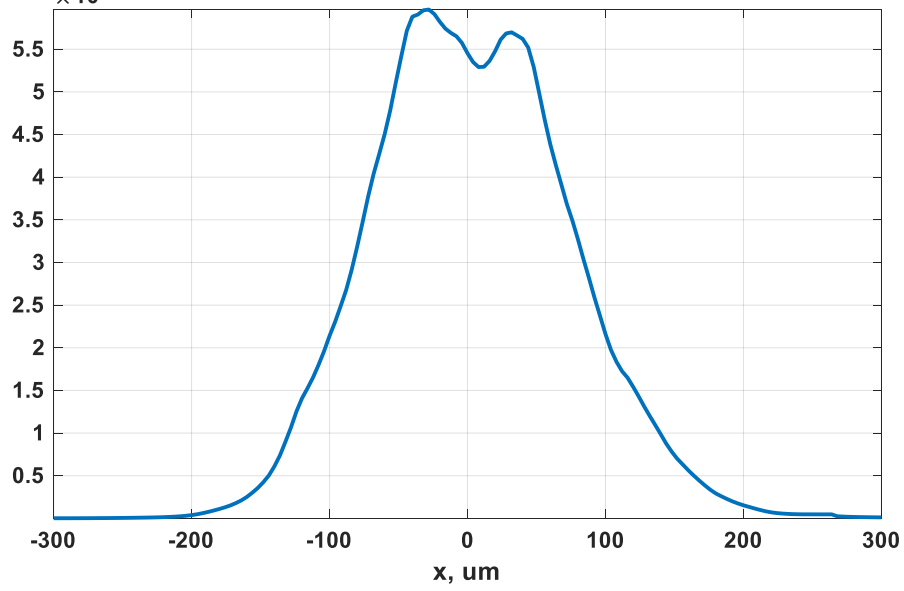
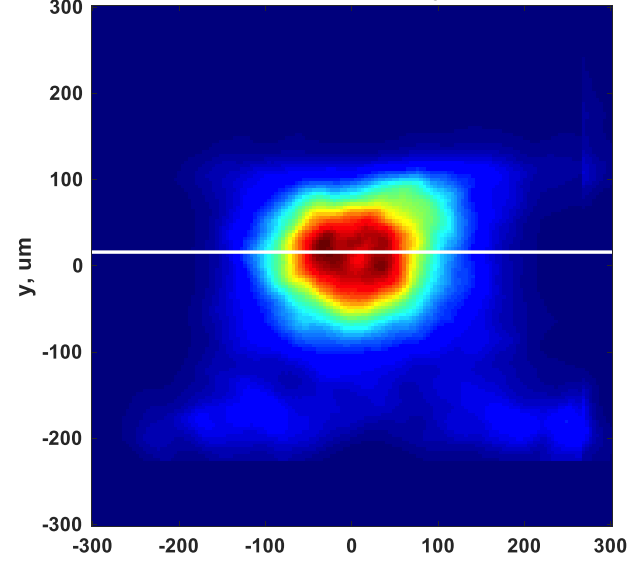
Position: (52, -163)
 Size @17%: (278,217)
 P0 = 129
 P2/P0 = -16%

 EMMML, stop @ $\Delta\chi^2/\chi^2 < 10^{-4}$

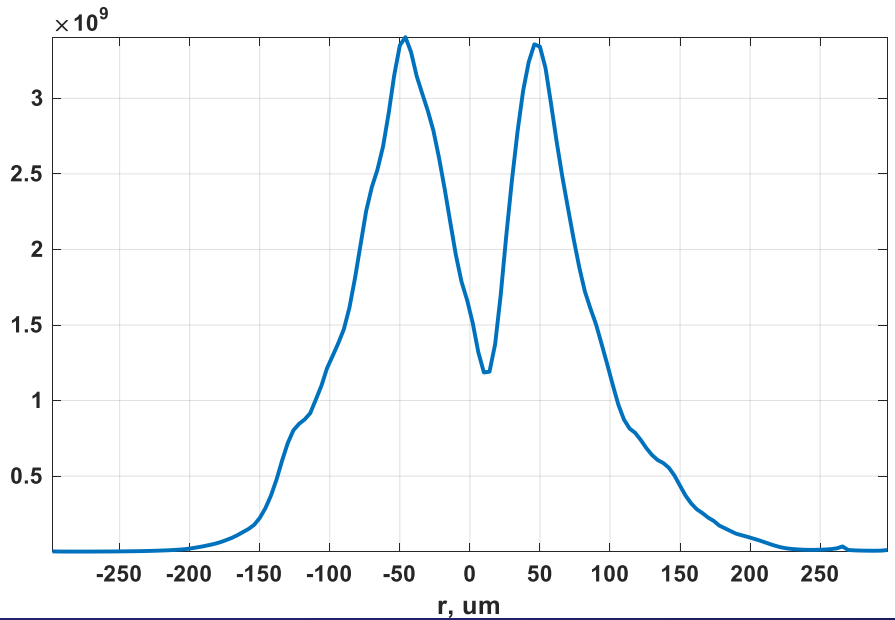
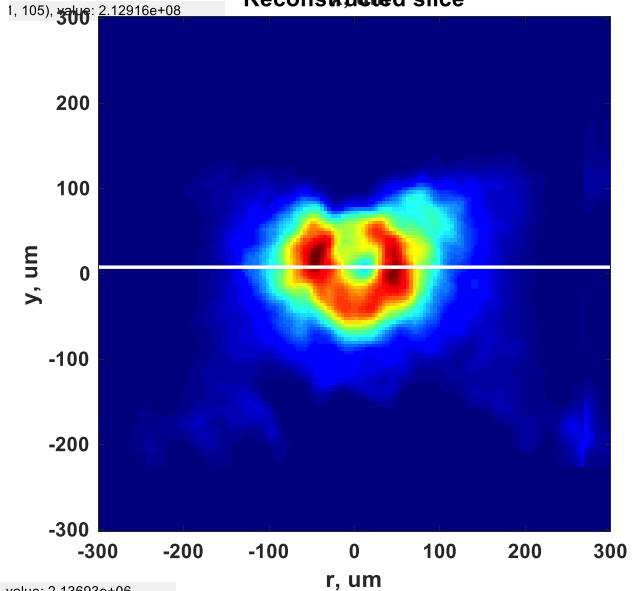


Abel inversion: $S(\rho, \phi, z) = S_{left}(\rho, z) \frac{1 - \sin\phi}{2} + S_{right}(\rho, z) \frac{1 + \sin\phi}{2}$

Reconstructed 2D projection

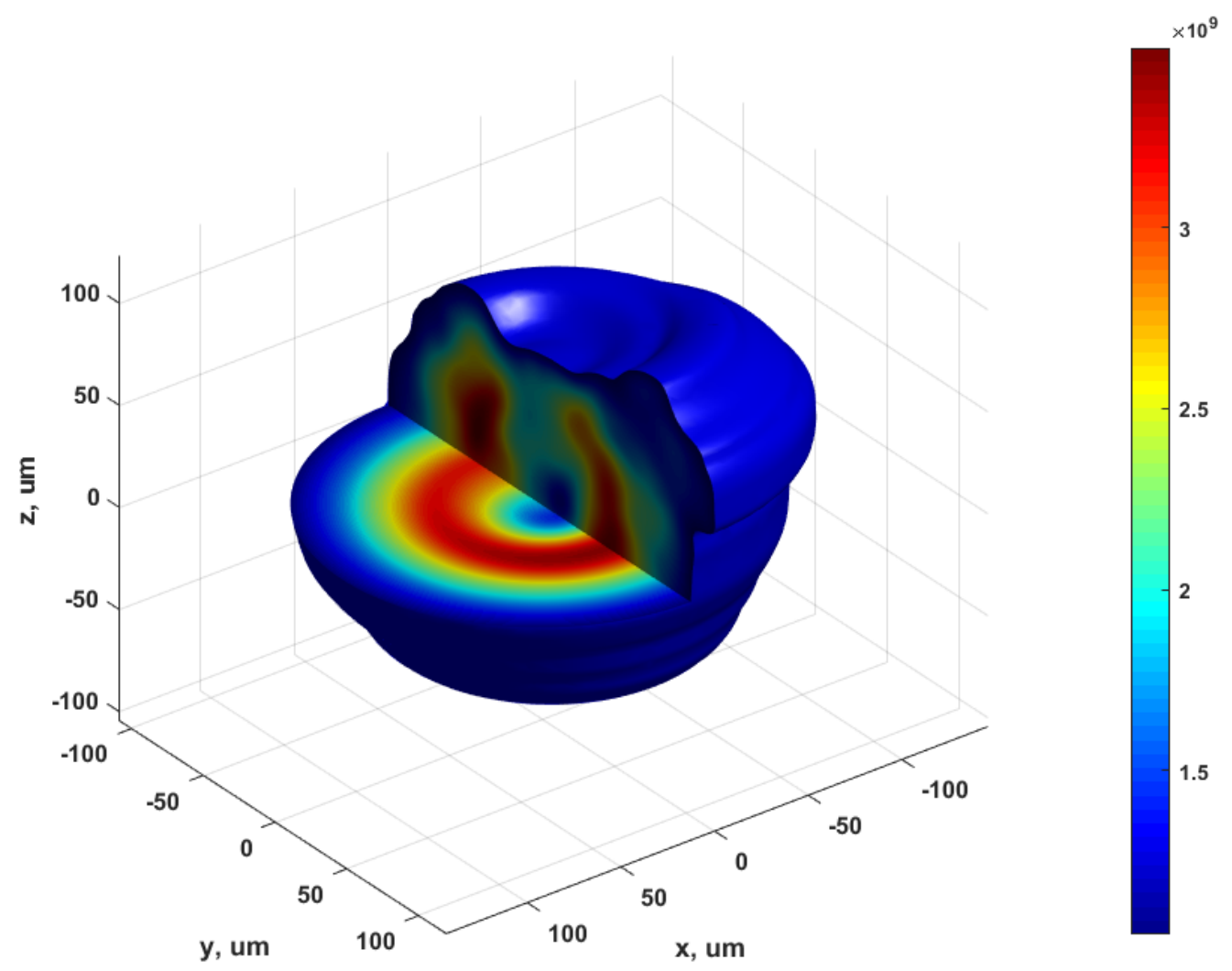


Reconstructed slice

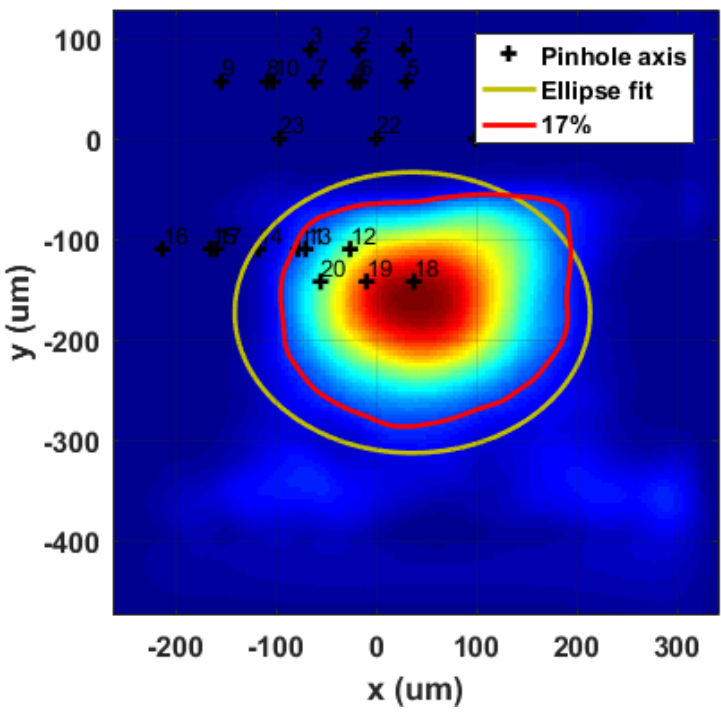


01), value: 2.13693e+06

N160602: 3D rendering of reconstructed gamma source

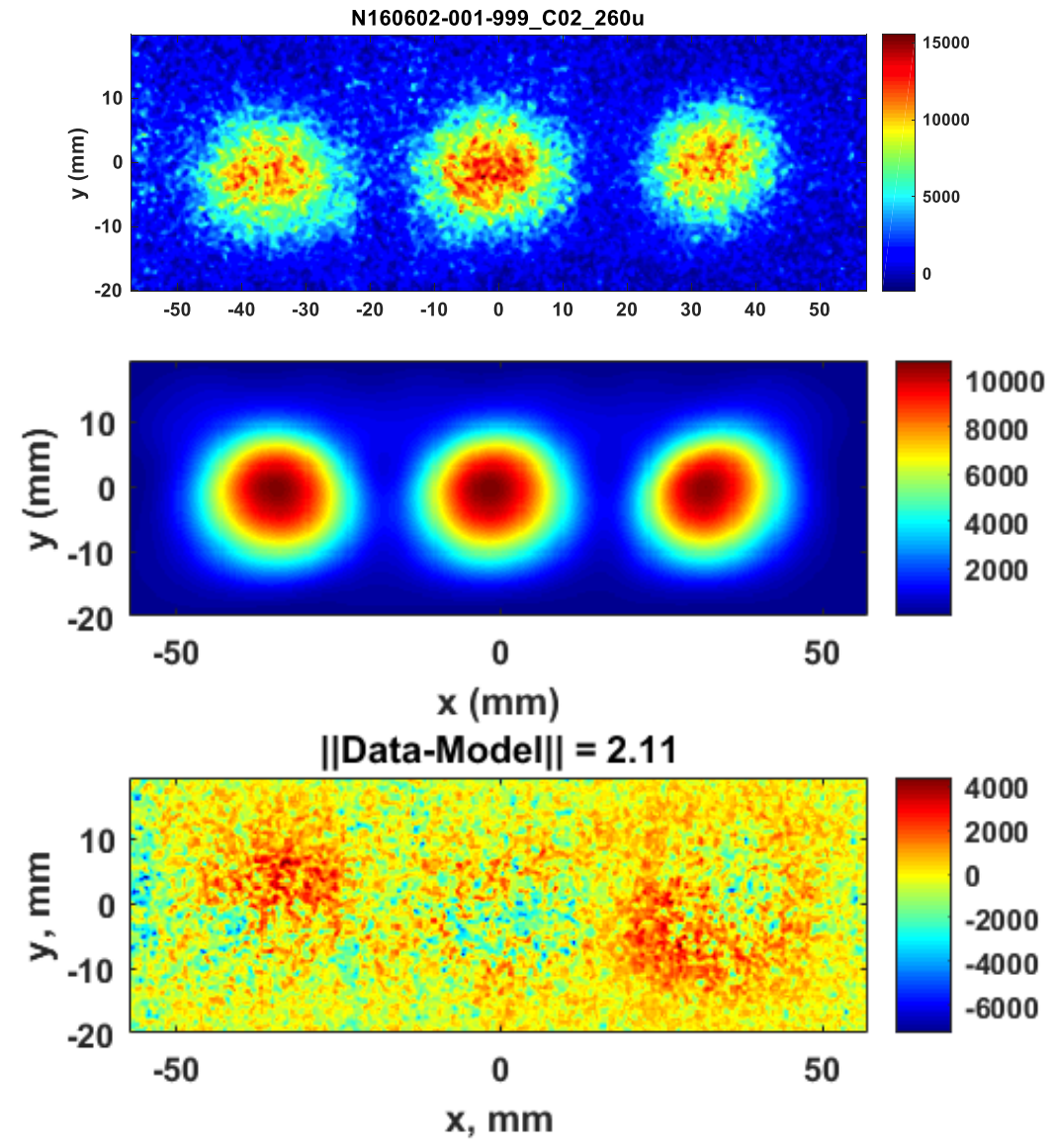


N160602: Generalized Expectation Maximization with Gibbs prior

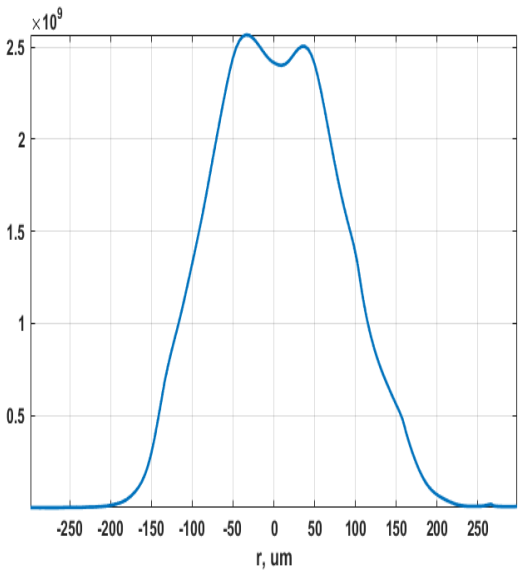
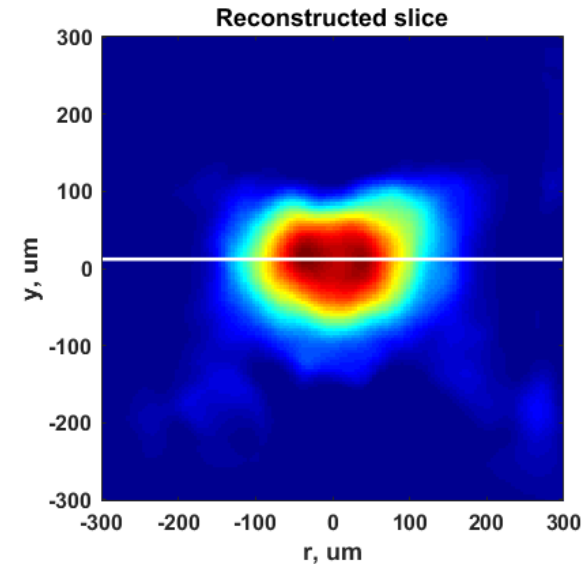
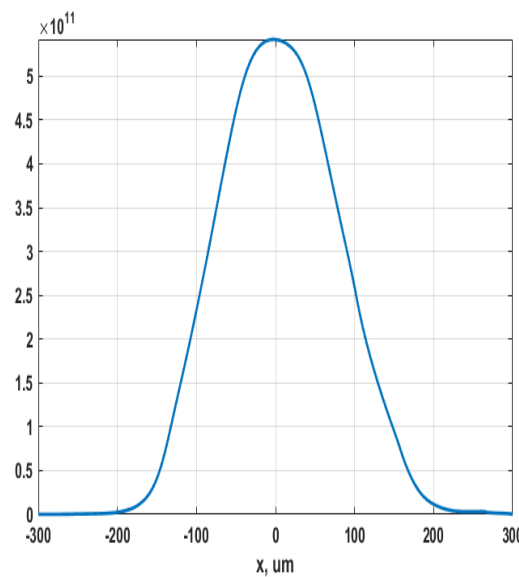
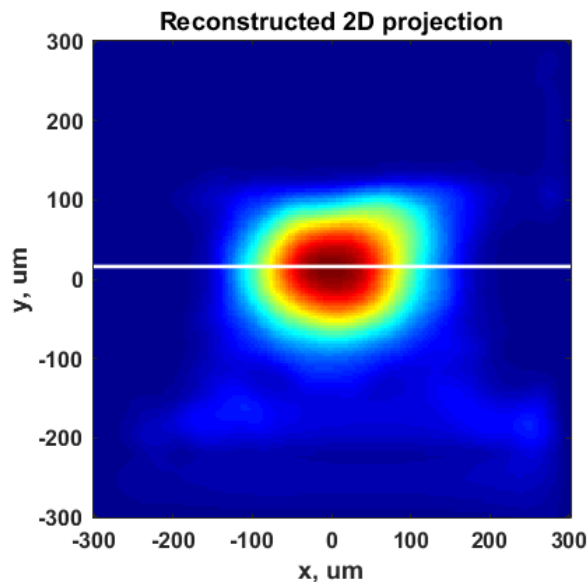


Position: (51, -164)
Size @17%: (299,229)
P0 = 138
P2/P0 = -17%

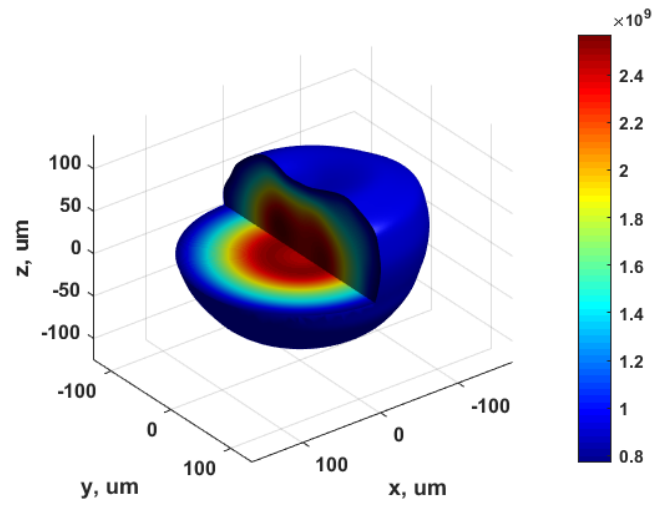
GEMMAP:
 $\lambda=10^{-3}$, stop @ $\Delta\chi^2/\chi^2 < 10^{-4}$



N160602: Abel inversion

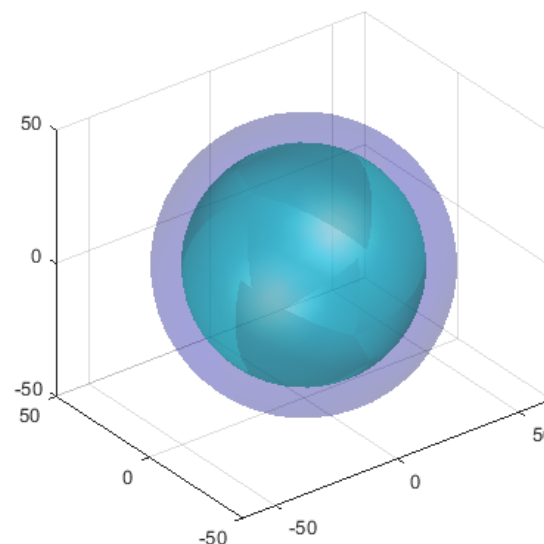


With a different prior, the void is not as obvious



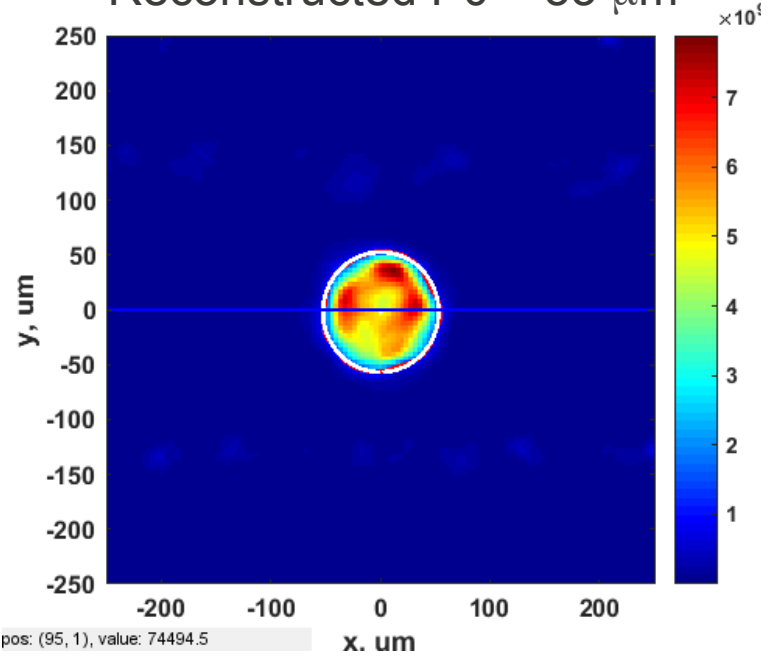
Use a simple shell model to simulate the gamma emission

- 80 μm inner diameter, 100 μm outer diameter shell source of gammas
- Signal levels are adjusted to show scaling of N160602

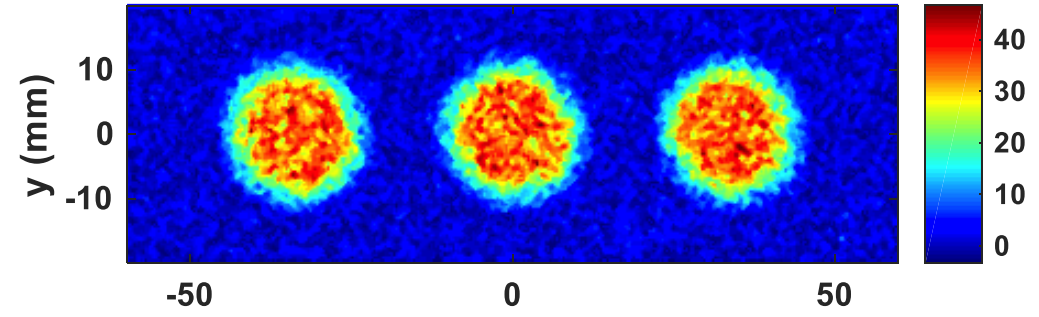


Simulated images using SNR similar to observed data (N160602) shows indications of the inner shell

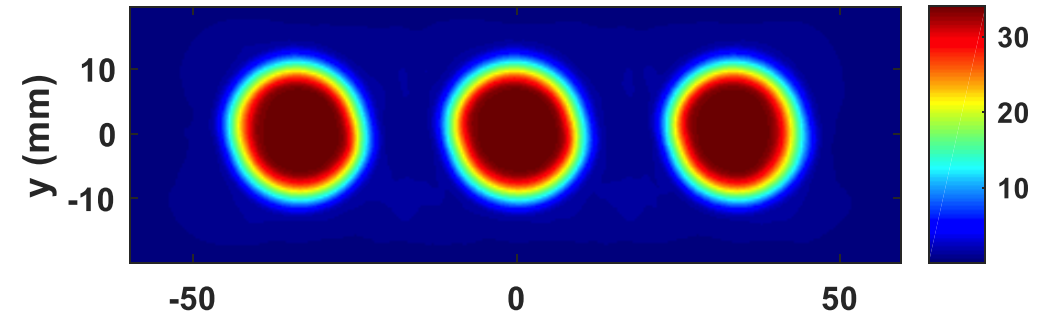
Reconstructed P0 = 53 μm



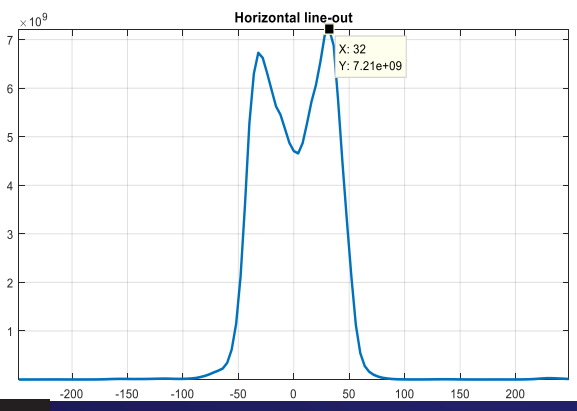
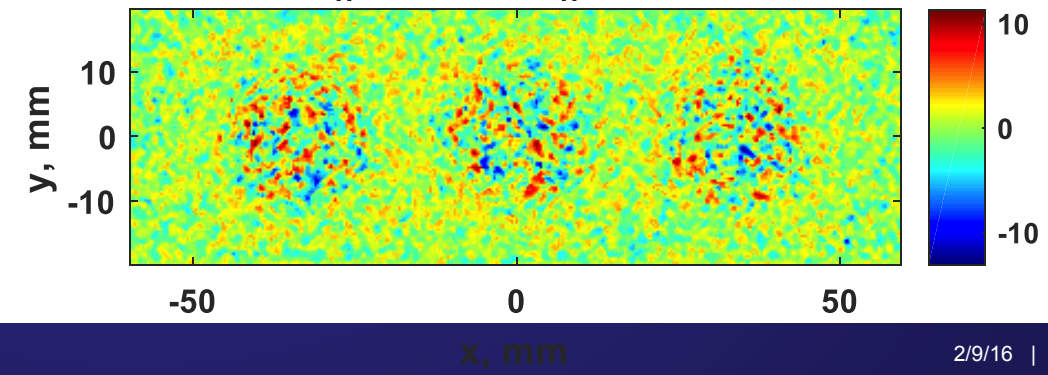
Simulated Gamma Image with SNR corresponding to N160602



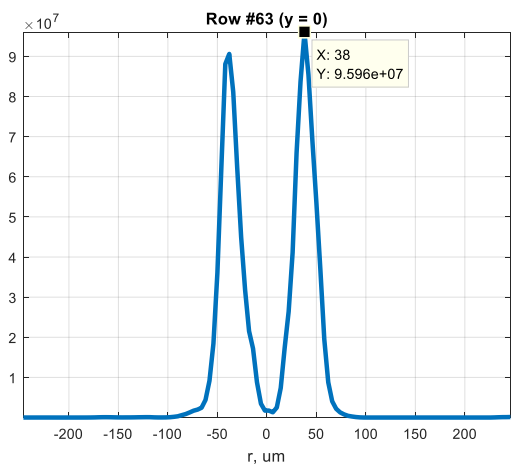
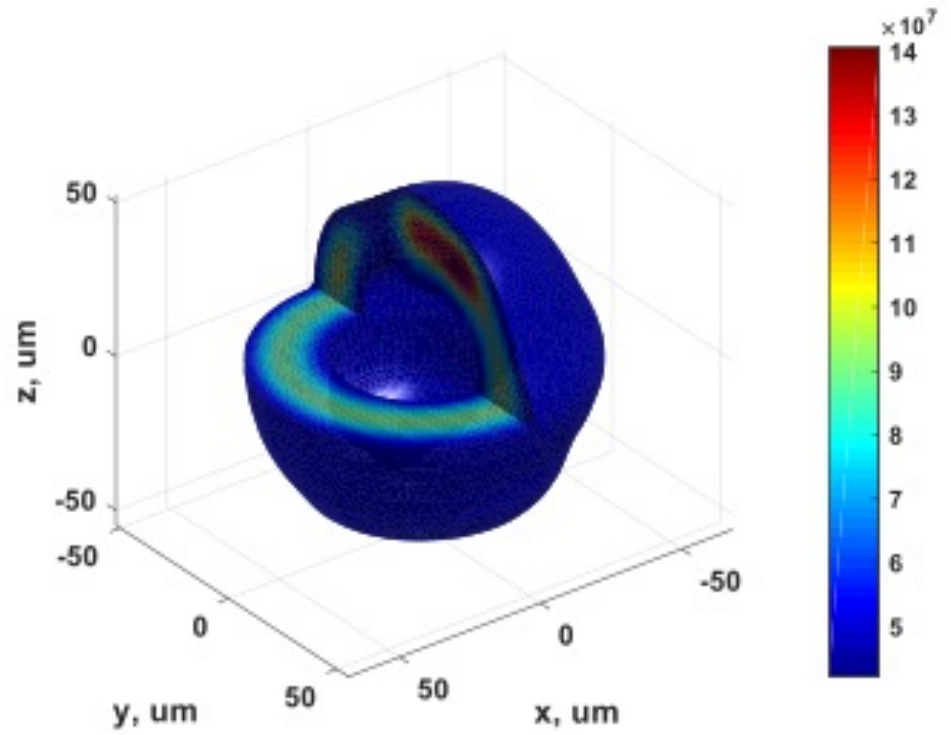
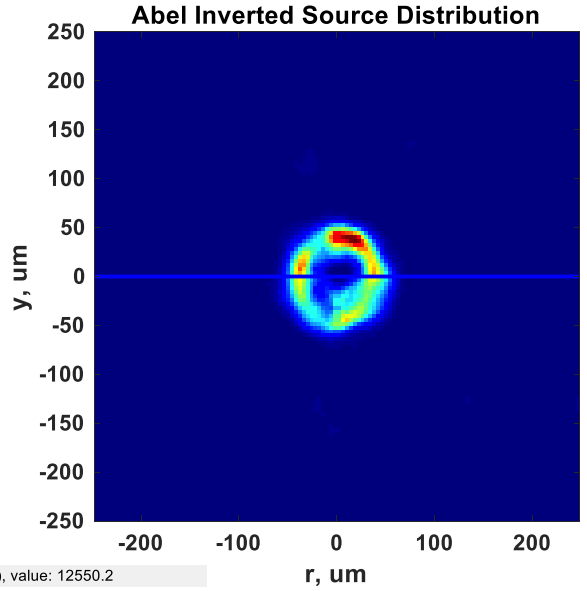
Forward Model



$||\text{Data-Model}|| = 2.74$

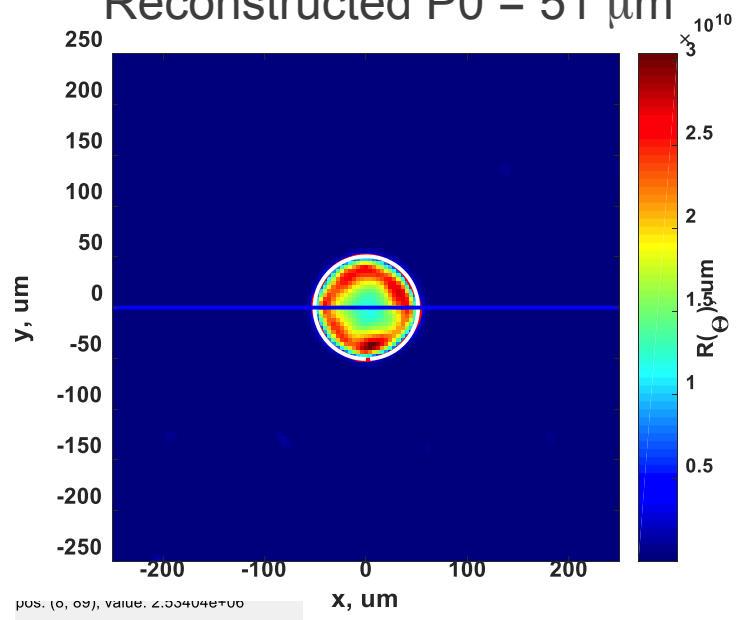


Abel inversion

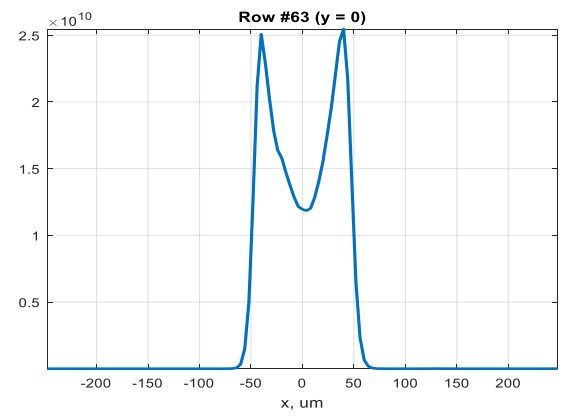


Simulated images ~3 times the signal of N160602

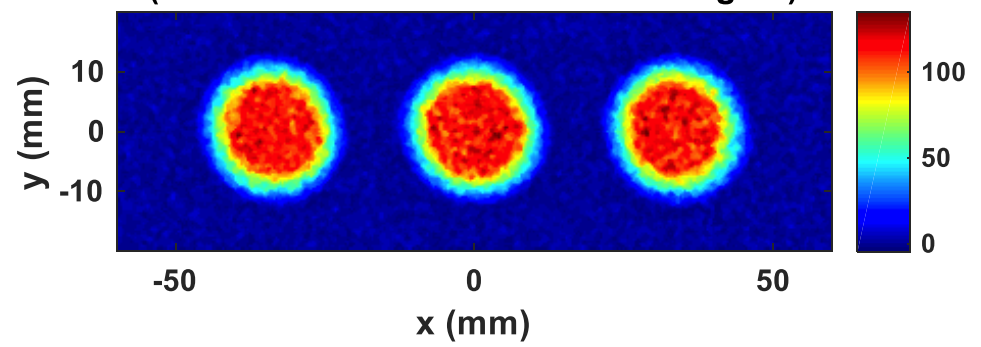
Reconstructed P0 = 51 μm



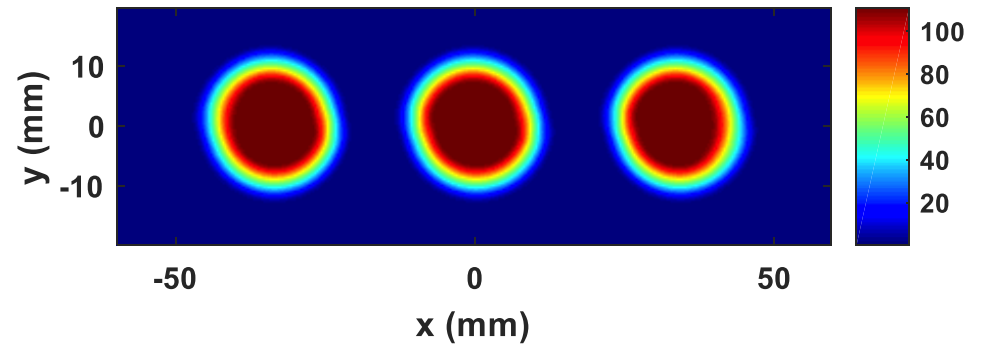
pos. (0, 0), value: 2.53404e+10



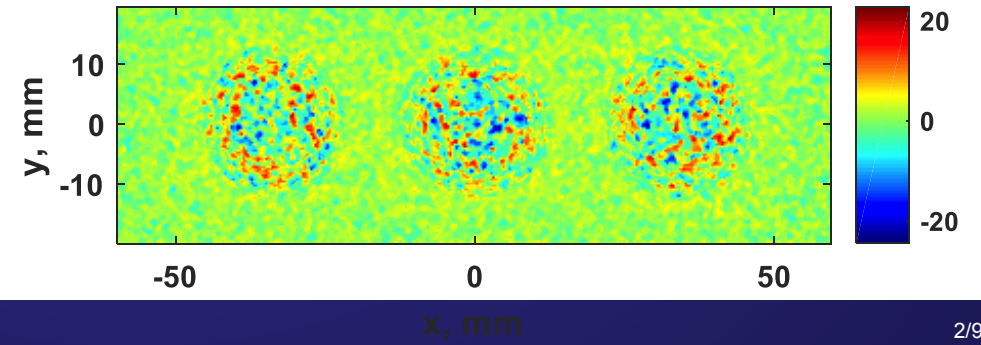
Simulated Gamma Image (Yn5e15 normalized to N160602 Signal)



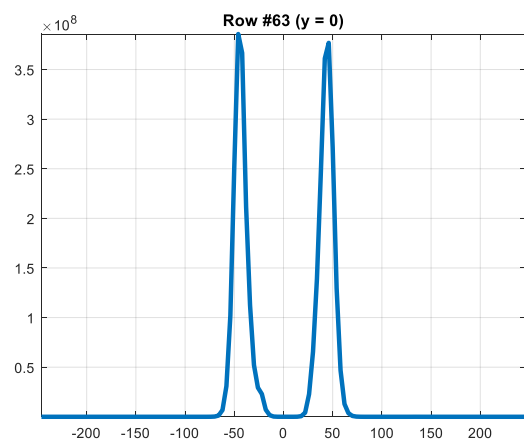
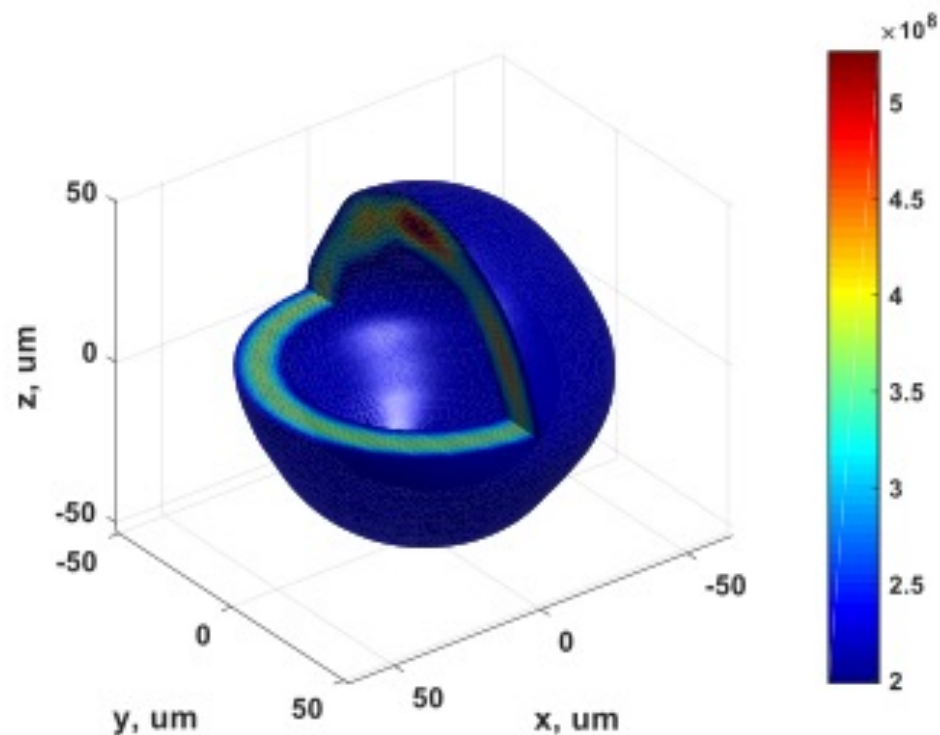
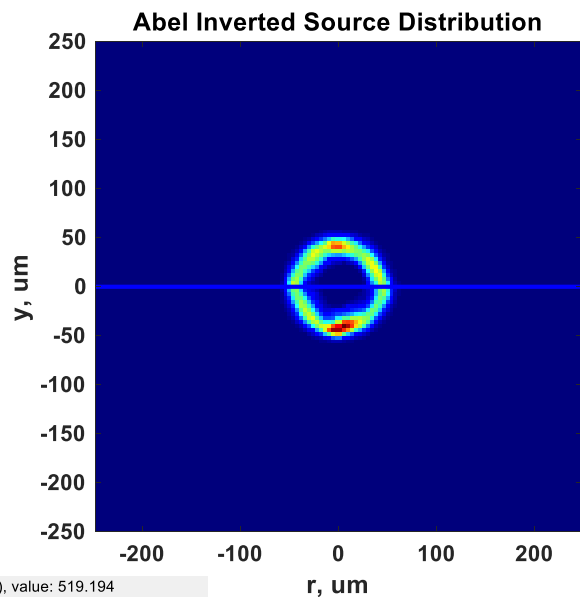
Forward Model

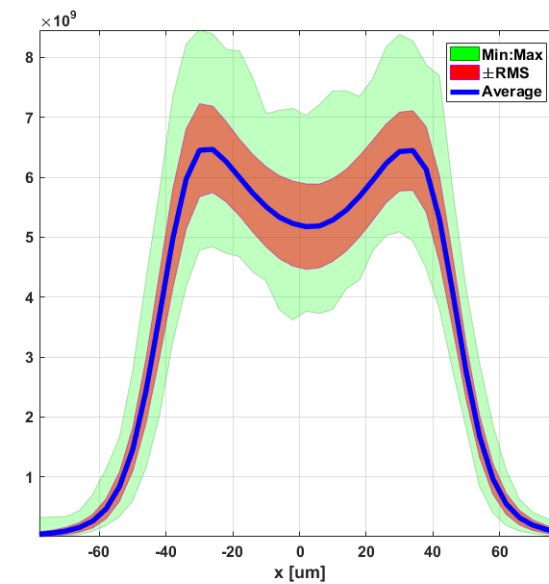
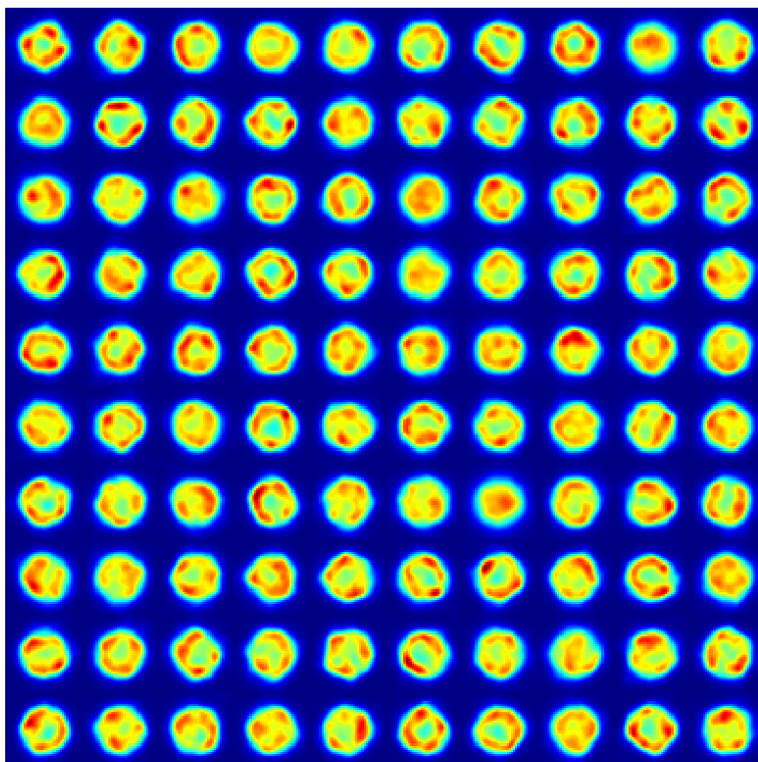
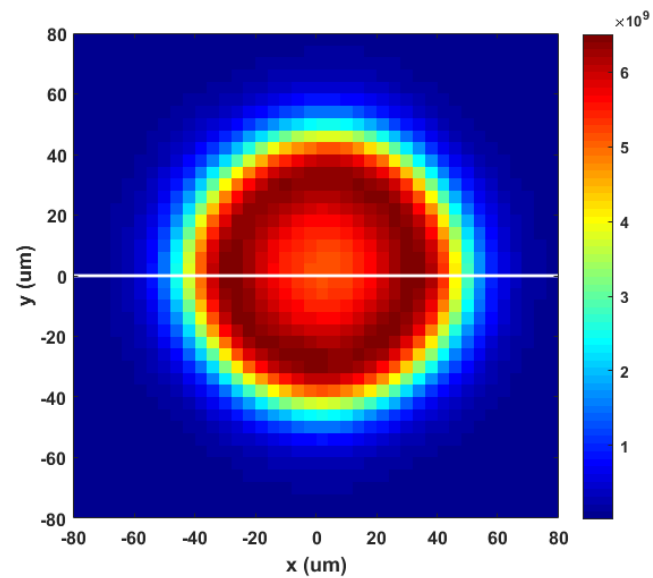
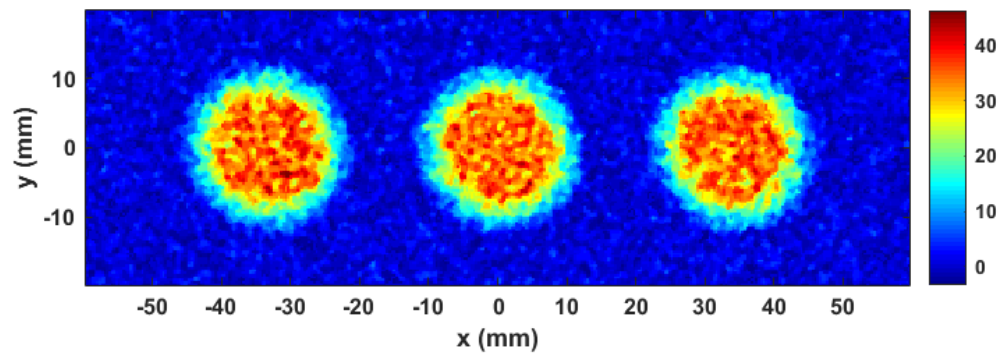


||Data-Model|| = 3.03

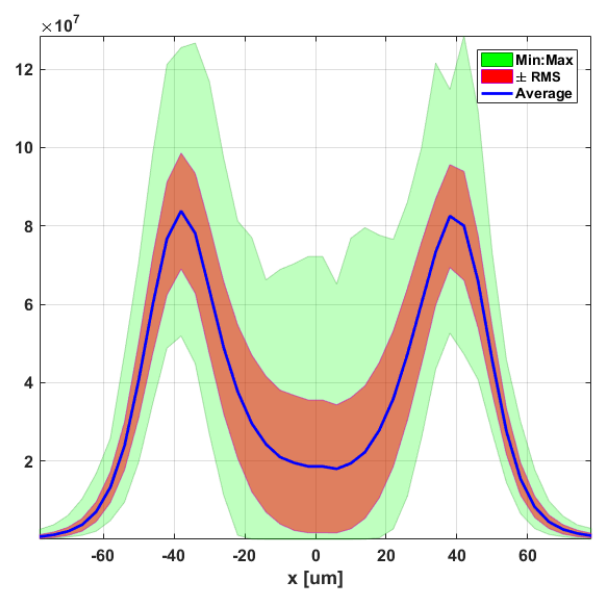
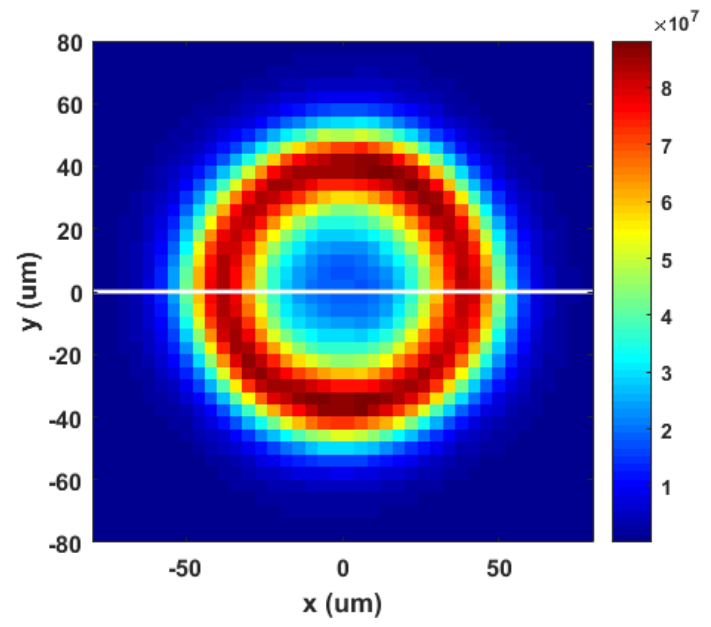
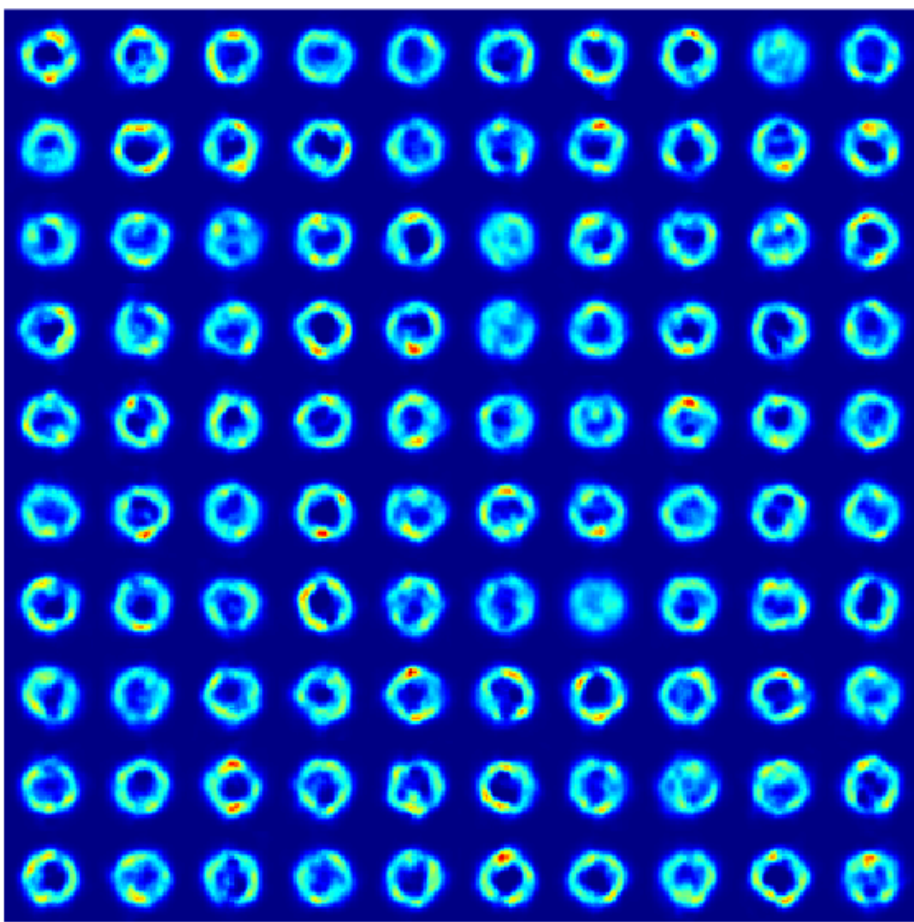


Abel inversion



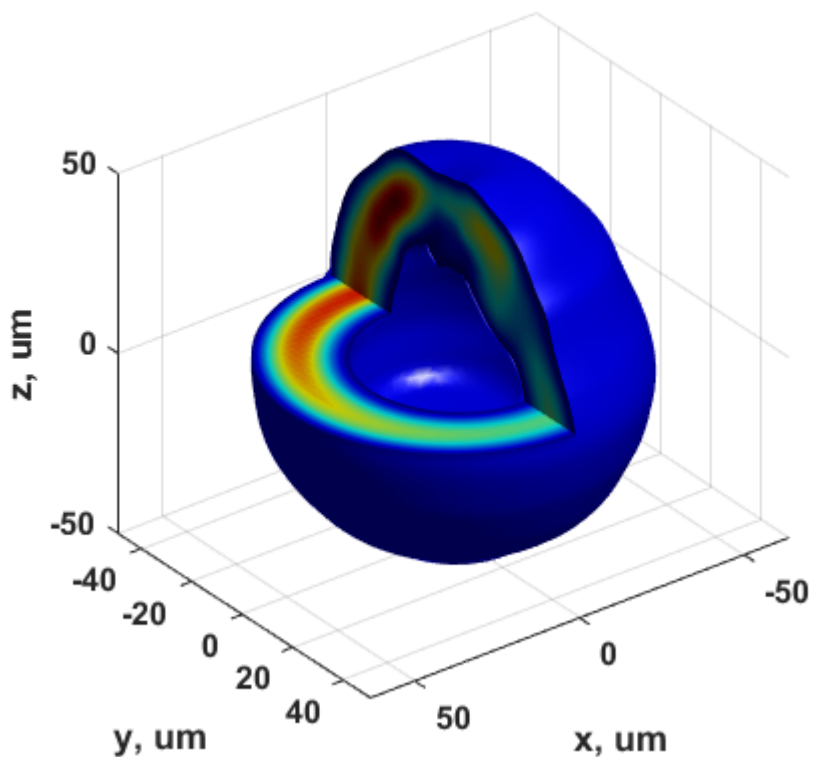


Stat Tests: Abel inversion

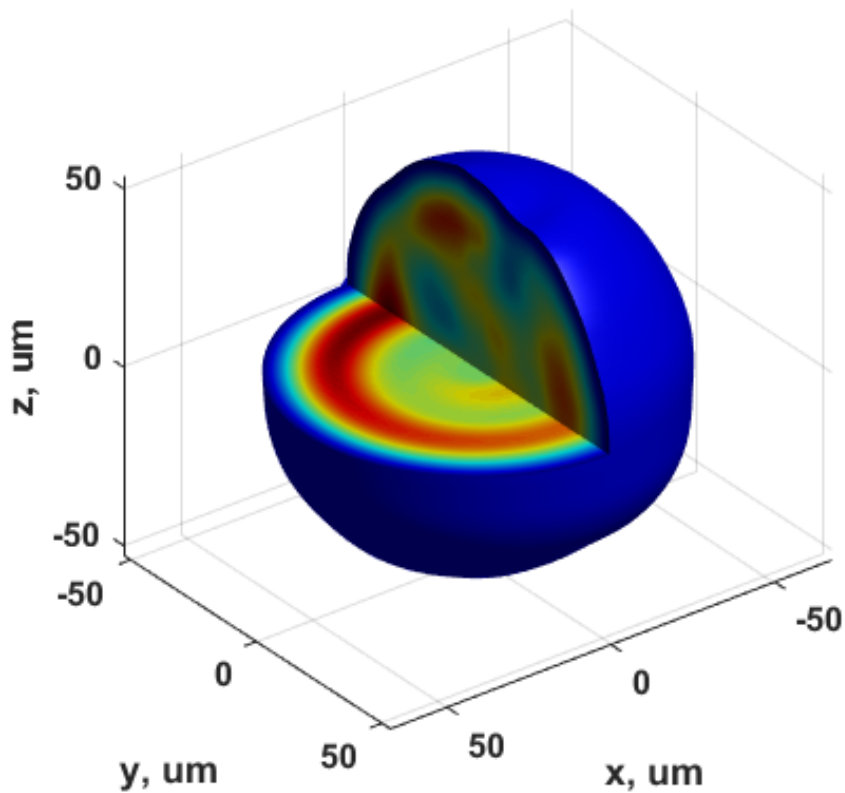


Stat Tests: "Best" and "worst" cases

~90%

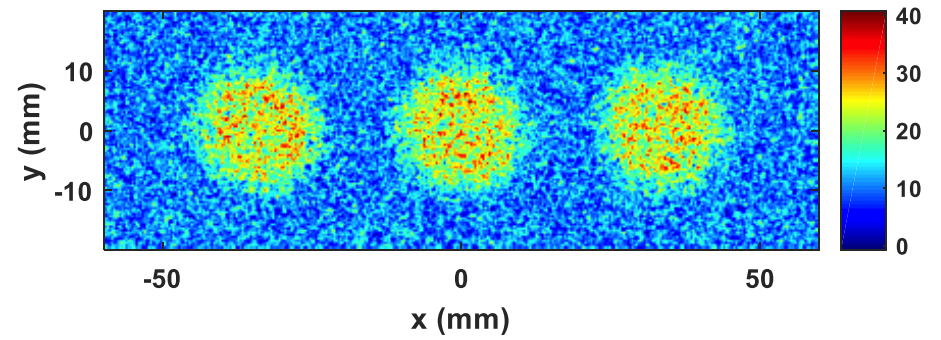
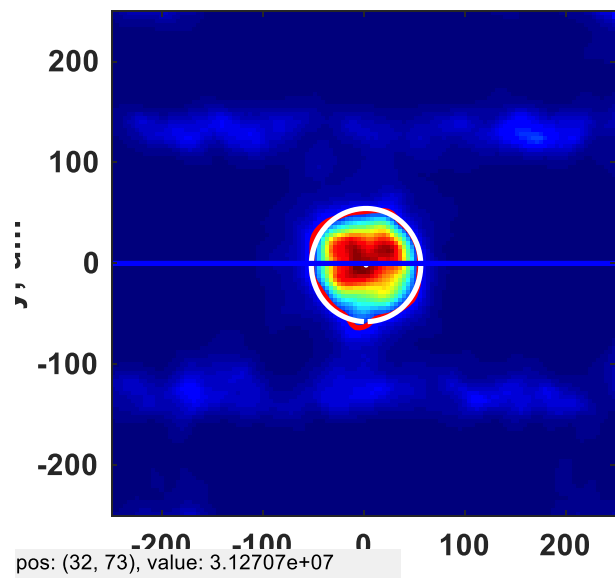


~10%

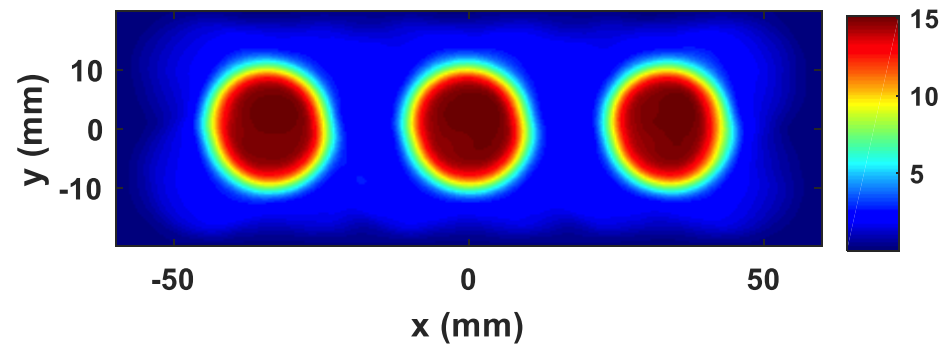


Simulated images with expected signal for N160602 (0.5% Yn)

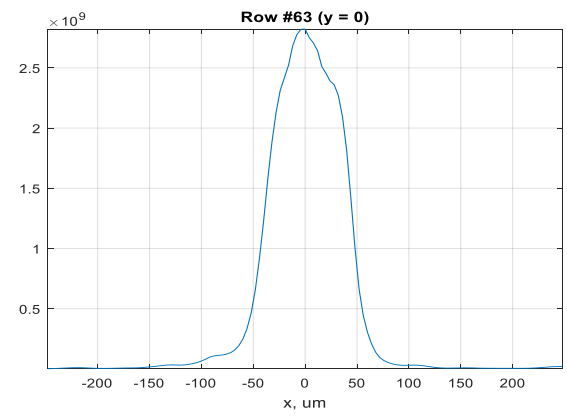
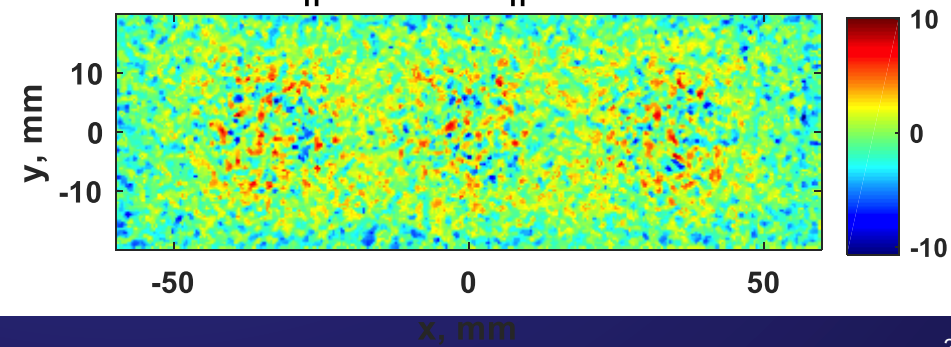
Reconstructed P0 = 55 μm



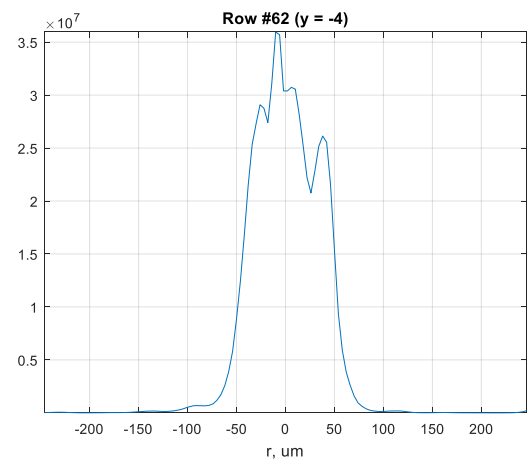
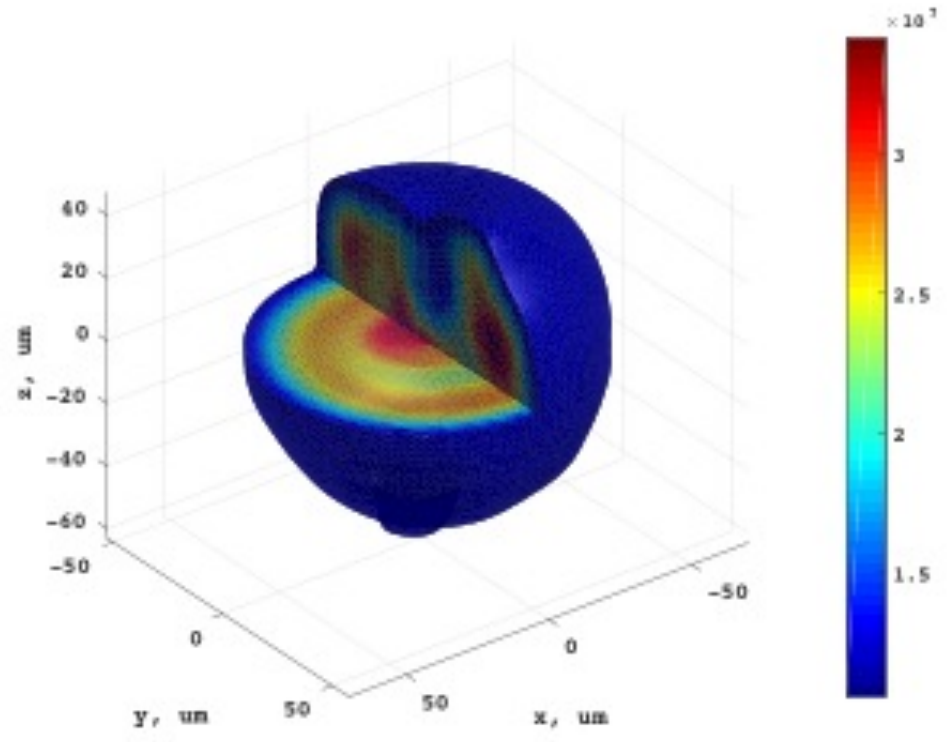
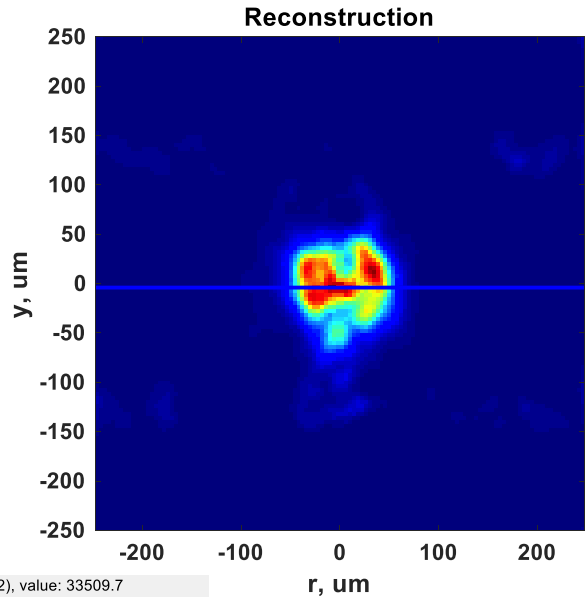
Forward Model



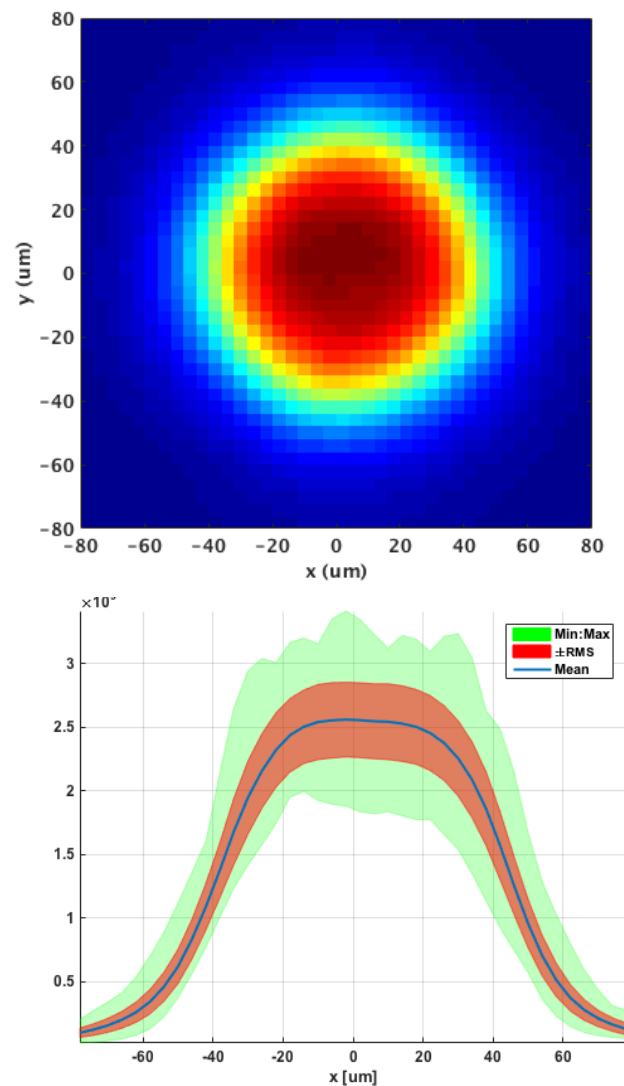
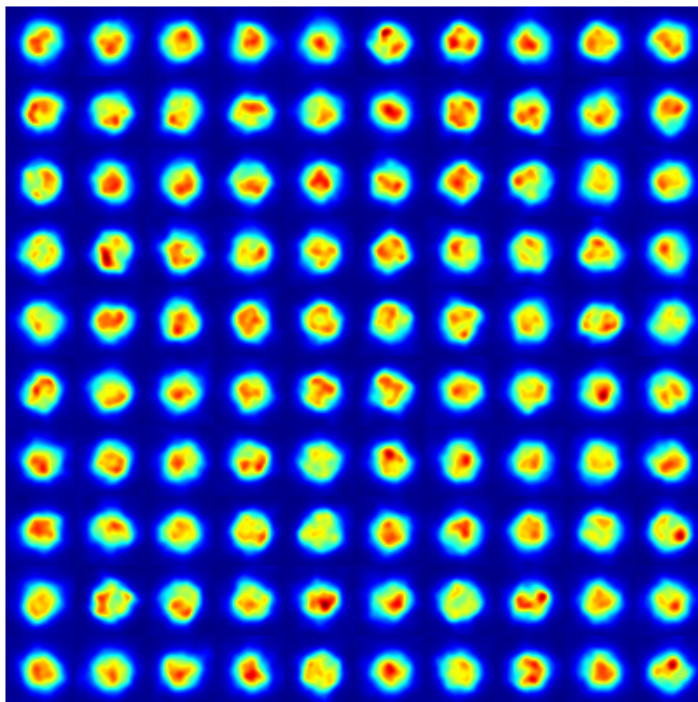
$||\text{Data-Model}|| = 2.97$



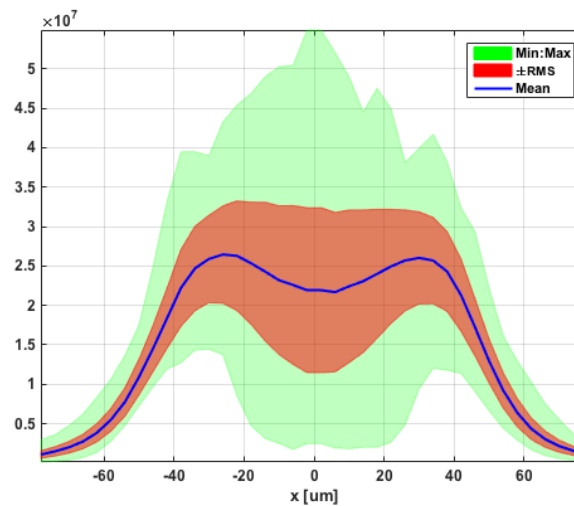
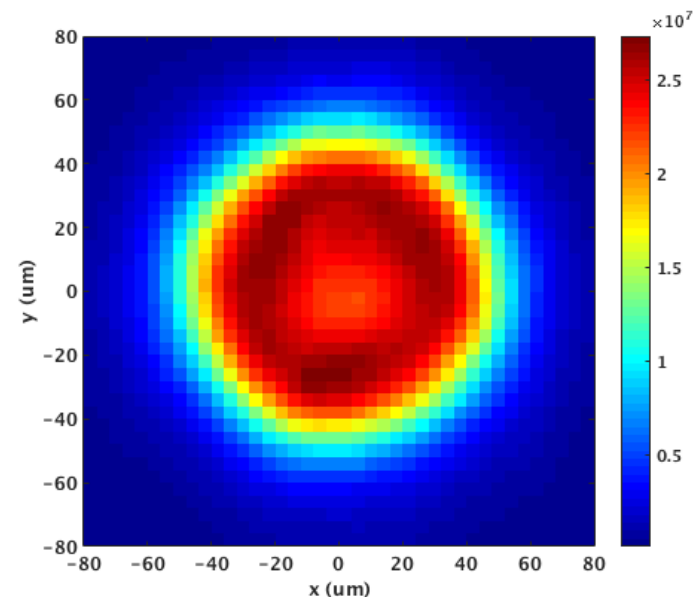
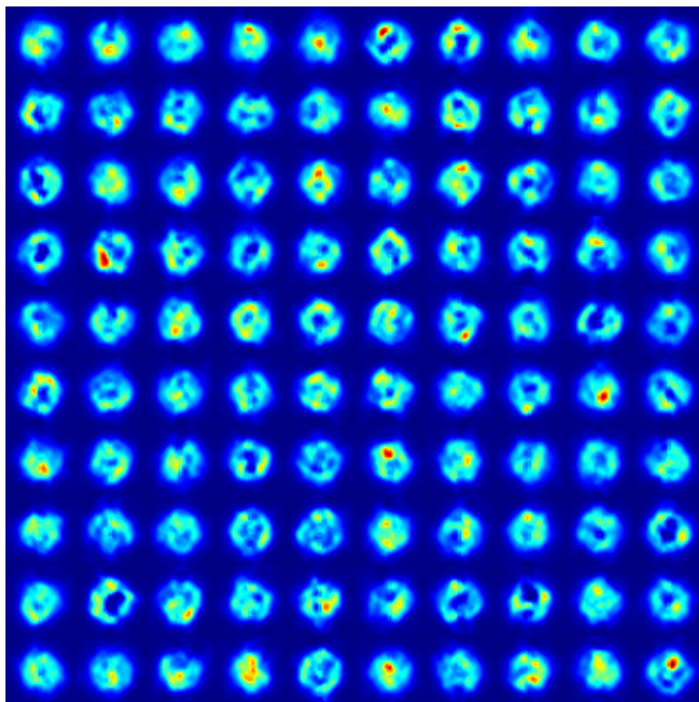
Abel inversion



Stat test: Expected gamma statistics

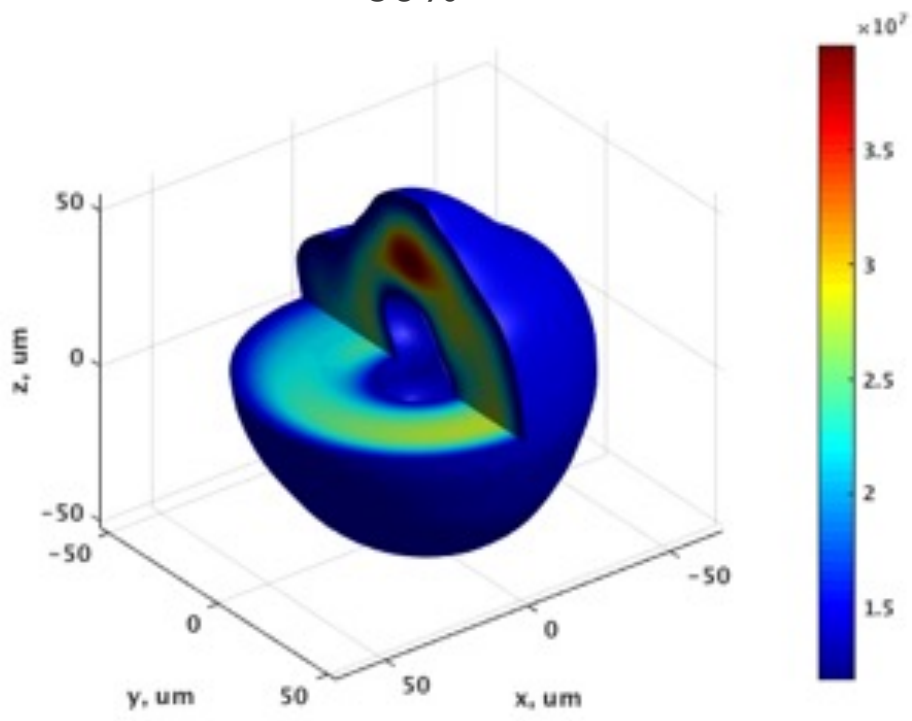


Stat test: Abel inversion

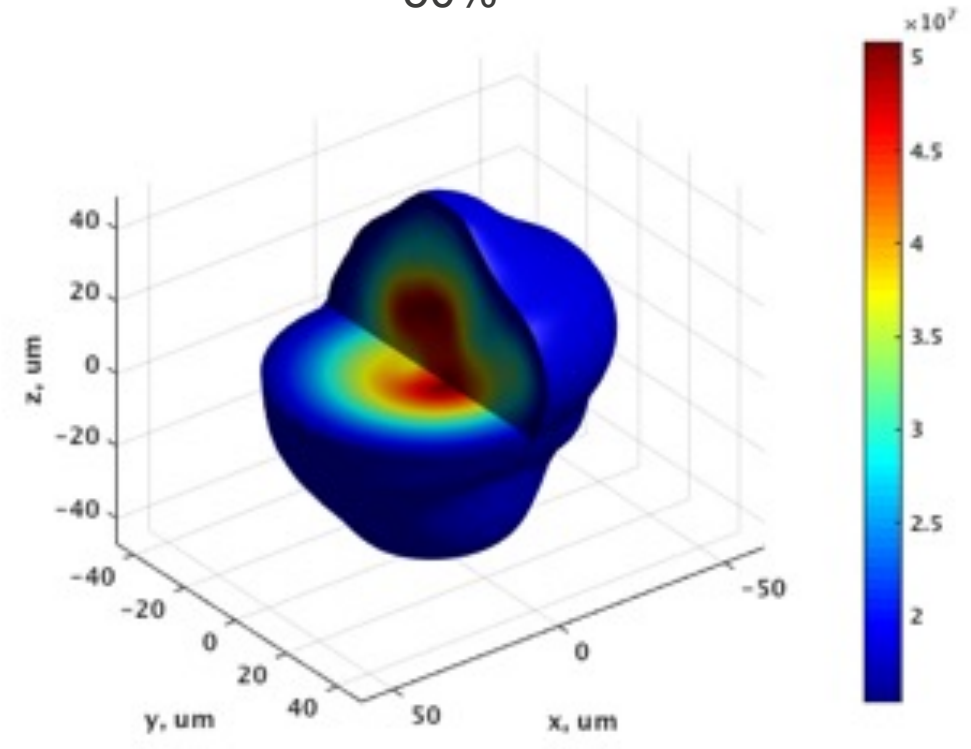


Best and worst case 3 D visualizations for expected gamma SNR

~50%



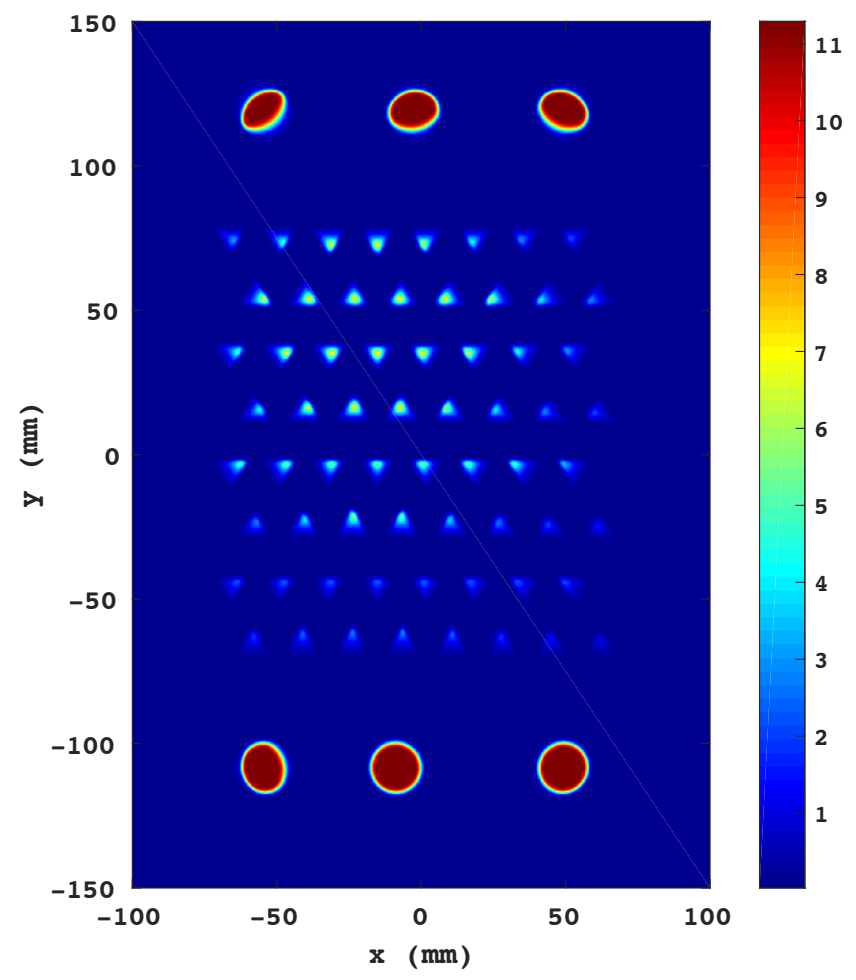
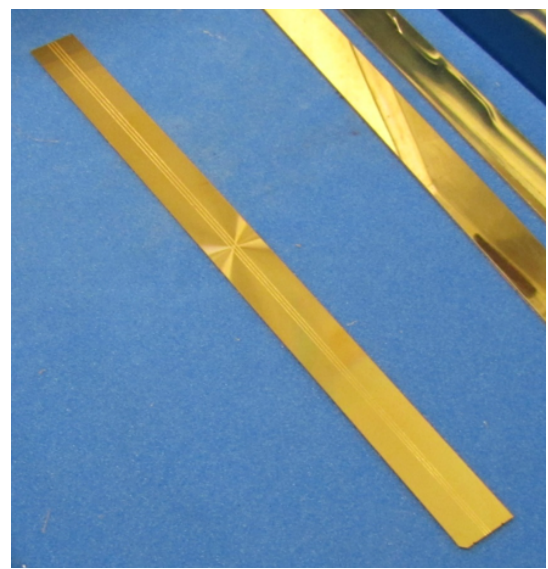
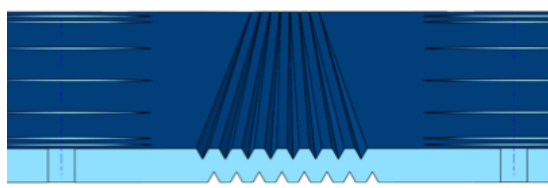
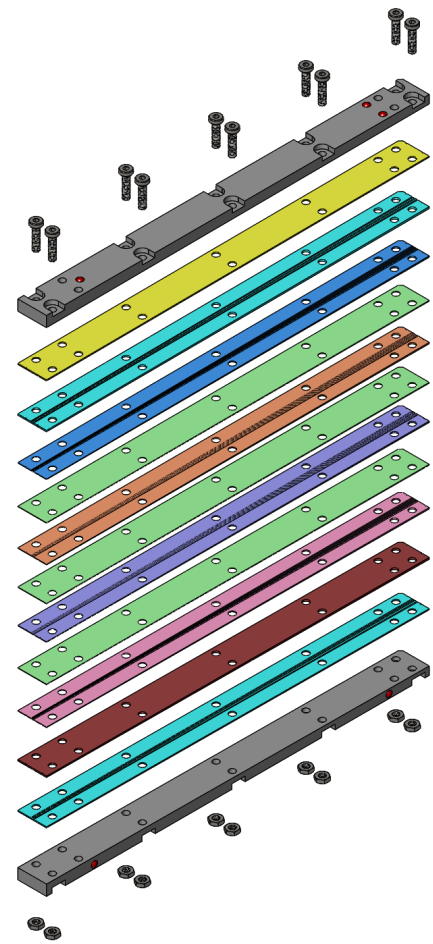
~50%



Going forward

- **Need to identify where the elevated signal levels are coming from**
- **Need to characterize penumbral apertures for gammas**
 - Previous work (N. Guler) showed that reconstructions of the neutron images using the nominal design of the apertures do not agree with pinhole reconstructions
- **New aperture array with more penumbral apertures would increase signal strength and allow better reconstructions**
- **Fabricate a new detector (LYSO based) to increase quantum efficiency**

New aperture array



Thank you! Questions?

Our Latest Publications:

Neutron Imaging System:	Merrill, et al. Rev. Sci. Instrum. 83, 10D317 (2012)
Reconstruction Algorithm:	Volegov, et al. Rev. Sci. Instrum. 85, 023508 (2014)
Array Characterization:	Volegov, et al. Rev. Sci. Instrum. 85, 123506 (2014)
NXI at Omega:	Danly, et al. Rev. Sci. Instrum. 86, 043503 (2015)
NIF CNXI concept:	Merrill, et al. Rev. Sci. Instrum. 85, 11E614 (2014)
NIF CNXI detector pack:	Simpson, et al. Rev. Sci Instrum. 86, 125112 (2015)
Coregistration technique:	Danly, et al. Rev. Sci. Instrum 83, 10E522 (2012)
3D reconstruction:	Volegov, et al. J. Appl. Phys. 118, 205903 (2015)
Density reconstruction:	Forthcoming
3D Spherical Harmonics:	Forthcoming
Gamma images reconstruction:	Forthcoming