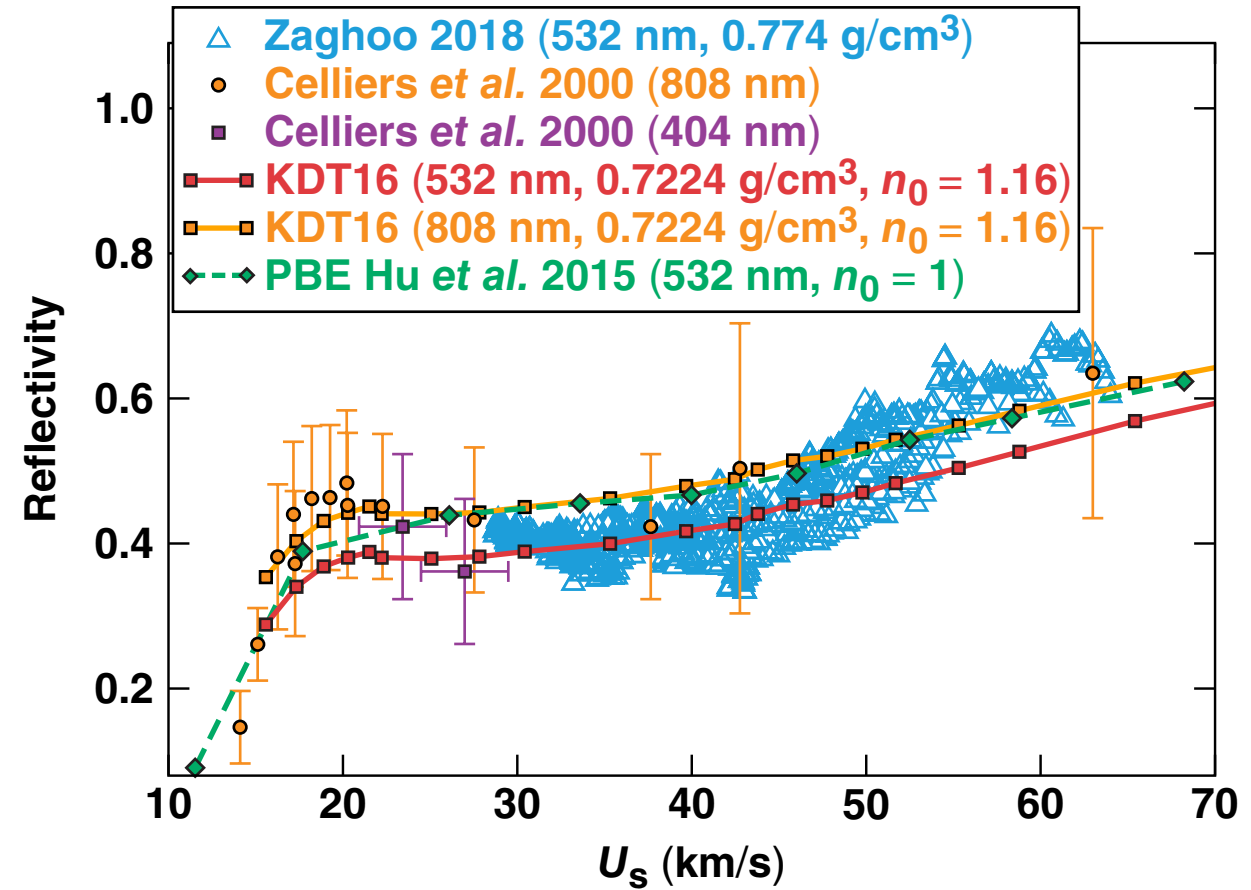
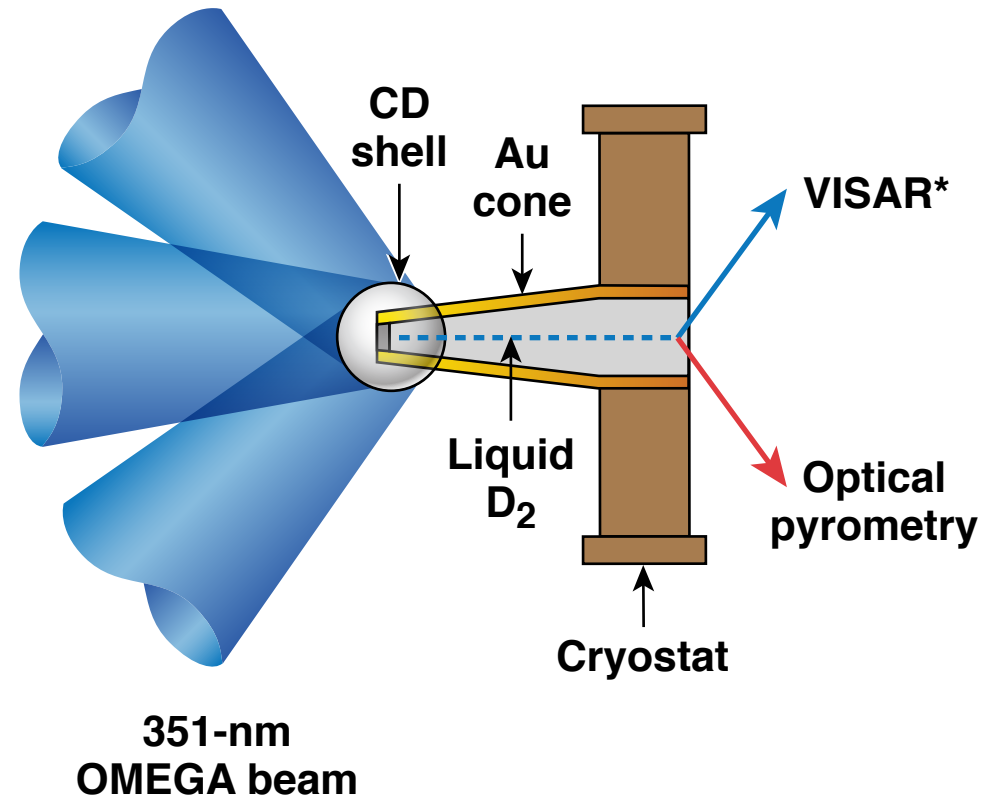


# Study of the Exchange-Correlation Thermal Effects for Transport and Optical Properties of Shocked Deuterium

CD shells filled with liquid  $D_2$   $\rho_0 = 0.172 \text{ g/cm}^3$



60th Annual Meeting of the American Physical Society Division of Plasma Physics  
Portland, OR  
5–9 November 2018

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Laboratory for Laser Energetics

## Summary

**Exchange-correlation (XC) thermal effects have an impact of up to 5% on the calculated properties of D<sub>2</sub> and must be taken into account for accurate predictions**



- **XC thermal effects account for the softening of the deuterium Hugoniot at  $P > 300$  GPa in agreement with recent experimental measurements**
- **The calculated reflectivity of shocked deuterium is in a good agreement with experimental measurements for shock speeds up to 50 km/s**
- **The deuterium system along the Hugoniot transforms from a semiconducting *molecular liquid* to an *atomic-poor metallic liquid* and finally to a *nondegenerate plasma***

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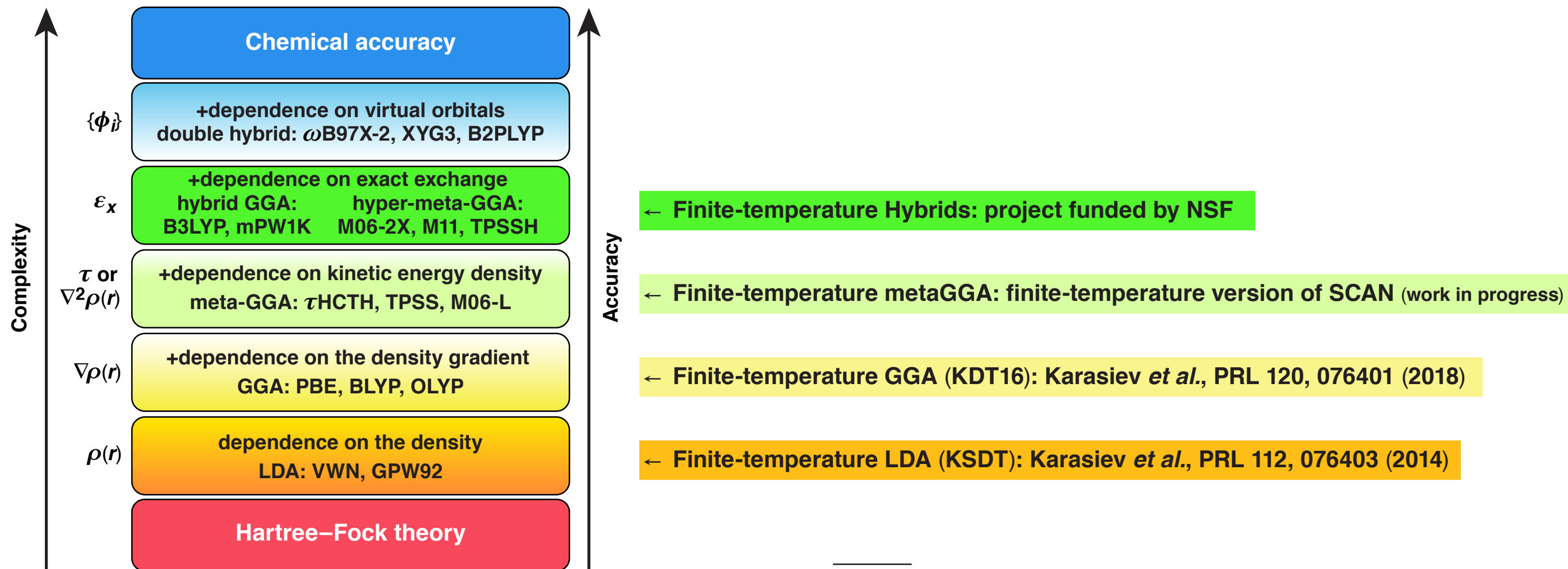
**Funding Acknowledgments:**

**This work was supported by US National Science  
Foundation PHY Grant No. 1802964**

**This material is based upon work supported by the Department  
of Energy National Nuclear Security Administration under Award  
Number DE-NA0003856**

# We are developing temperature-dependent XC functionals to improve density functional theory (DFT) predictions

Jacob's ladder\* of the zero-temperature XC functional approximations



Development has to start from the lowest rung because low-rung functionals are used as ingredients for higher rungs

PBE/GGA: J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. **77**, 3865 (1996); **78**, 1396(E) (1997).  
 PZ/LDA: J. P. Perdew and A Zunger, Phys. Rev. B **23**, 5048 (1981).  
 \* J. P. Perdew and K. Schmidt, AIP Conf. Proc. **577**, 1 (2001).

# The XC thermal effects for the homogeneous electron gas (HEG) are significant in warm-dense-matter (WDM) regime\*

$f_{\text{XC}}$  = XC free energy per particle

$\varepsilon_{\text{XC}}$  = XC energy per particle at  $T = 0$

$f_{\text{S}}$  = non-interacting free energy

Measure of relative importance of thermal effects

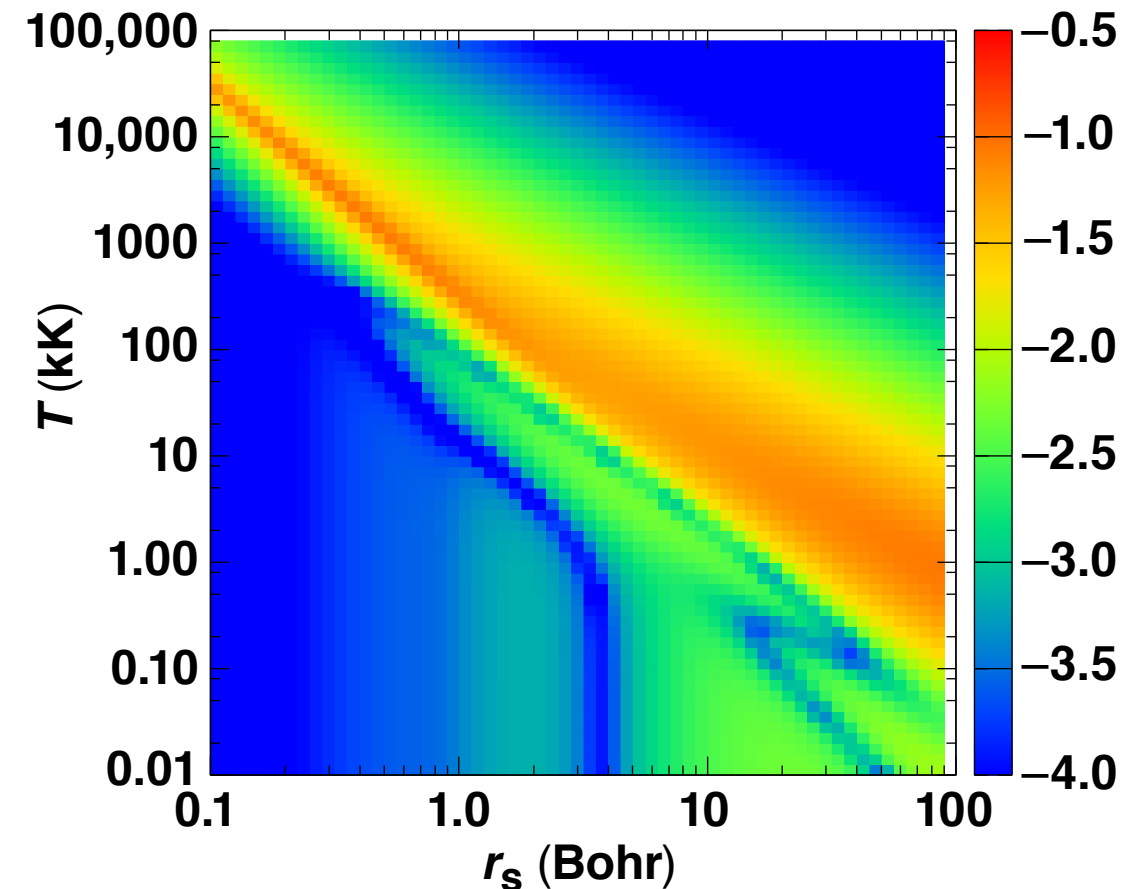
$$A = \log_{10} \frac{|f_{\text{XC}}(r_{\text{S}}, T) - \varepsilon_{\text{XC}}(r_{\text{S}})|}{|f_{\text{XC}}(r_{\text{S}}, T)| + |\varepsilon_{\text{XC}}(r_{\text{S}})|}$$

- At low temperature the XC thermal effects are negligible
- In high temperature limit the free-energy is dominated by the noninteracting part  $\rightarrow$  XC is negligible and does not play a role

In this work we use Karasiev–Dufty–Trickey (KDT16) GGA-level XC free-energy functional to address the issue of thermal effects

See details in:

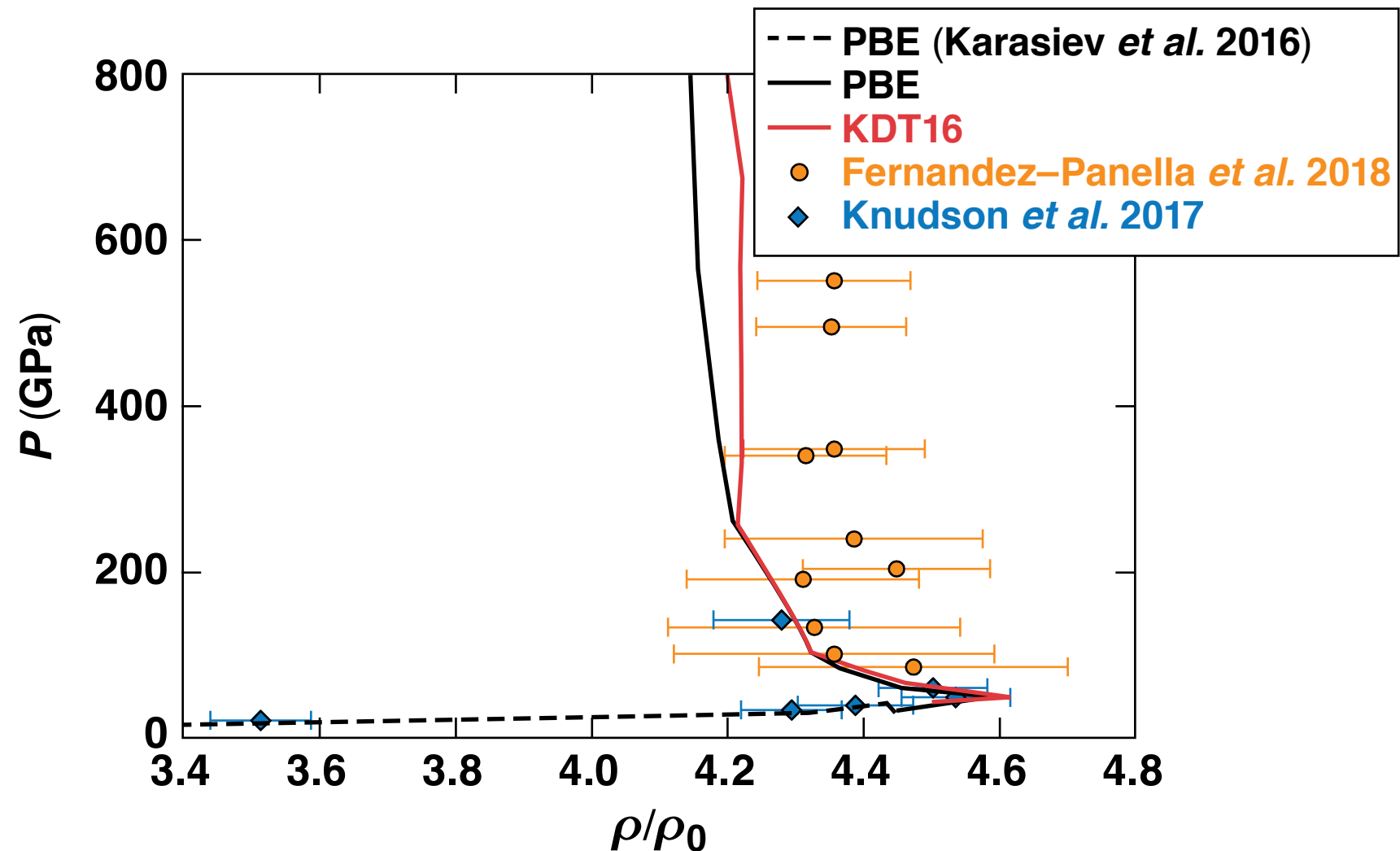
Karasiev *et al.*, Phys. Rev. Lett. 120, 076401 (2018).



\*V. V. Karasiev, L. Calderín, and S. B. Trickey, Phys. Rev. E 93, 063207 (2016).

## Results

The D<sub>2</sub> Hugoniot becomes ~2% softer at high pressure ( $P > 300$  GPa) as a result of thermal XC effects; agreement with recent experimental measurements is improved



- Energy  $\Delta E$  and pressure  $\Delta P$  corrections caused by the thermal XC effects are larger than 4% but have the same sign
- There is some cancellation between  $\Delta E$  and  $\Delta P$  corrections in the Hugoniot relation\*

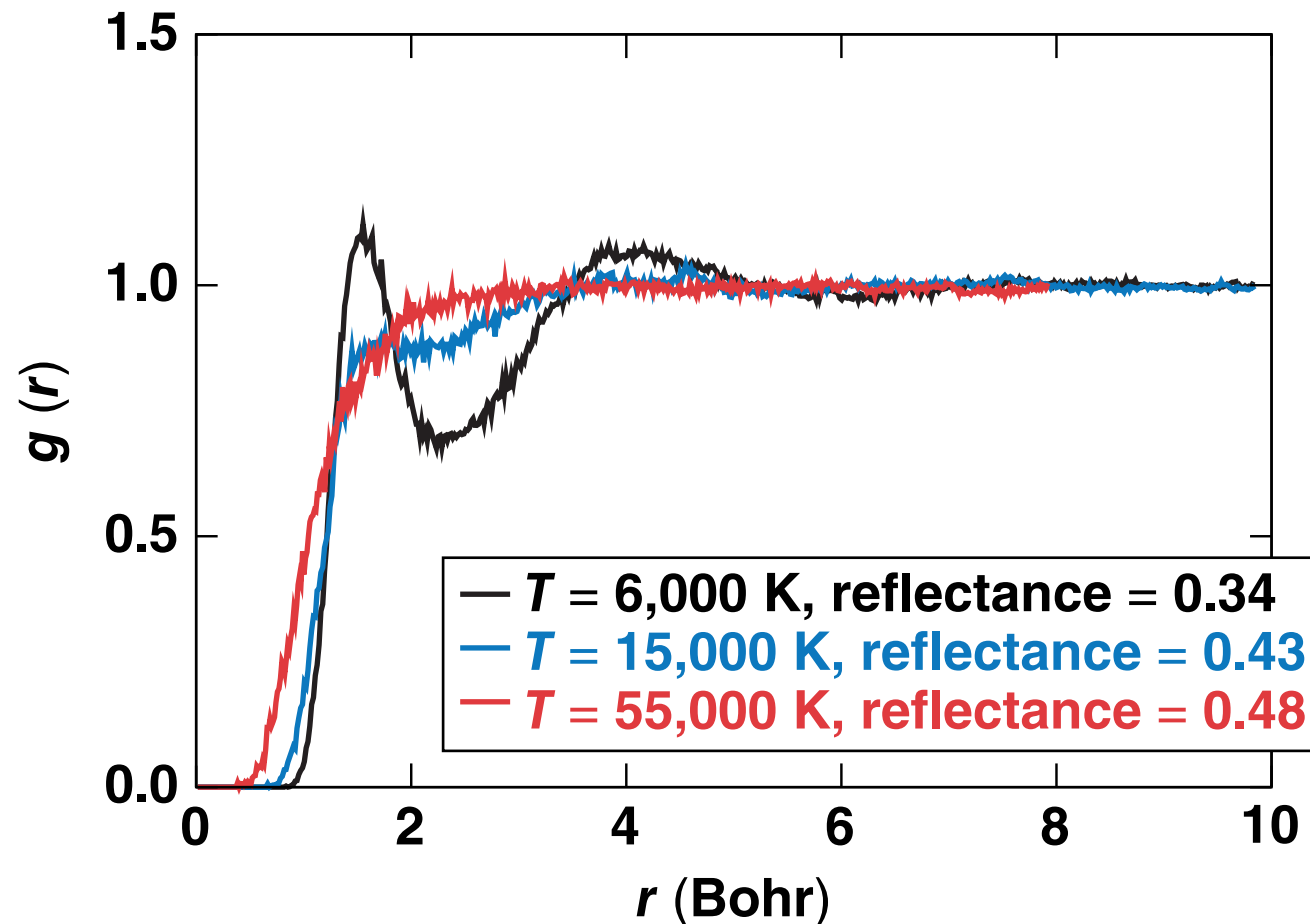
$$E - E - \frac{1}{2}(P - P_0)\left(\frac{1}{\rho} - \frac{1}{\rho_0}\right) = 0$$

Fernandez-Pañella *et al.*, (submitted) (2018);  
Knudson, Desjarlais PRL, 118 035501 (2017).

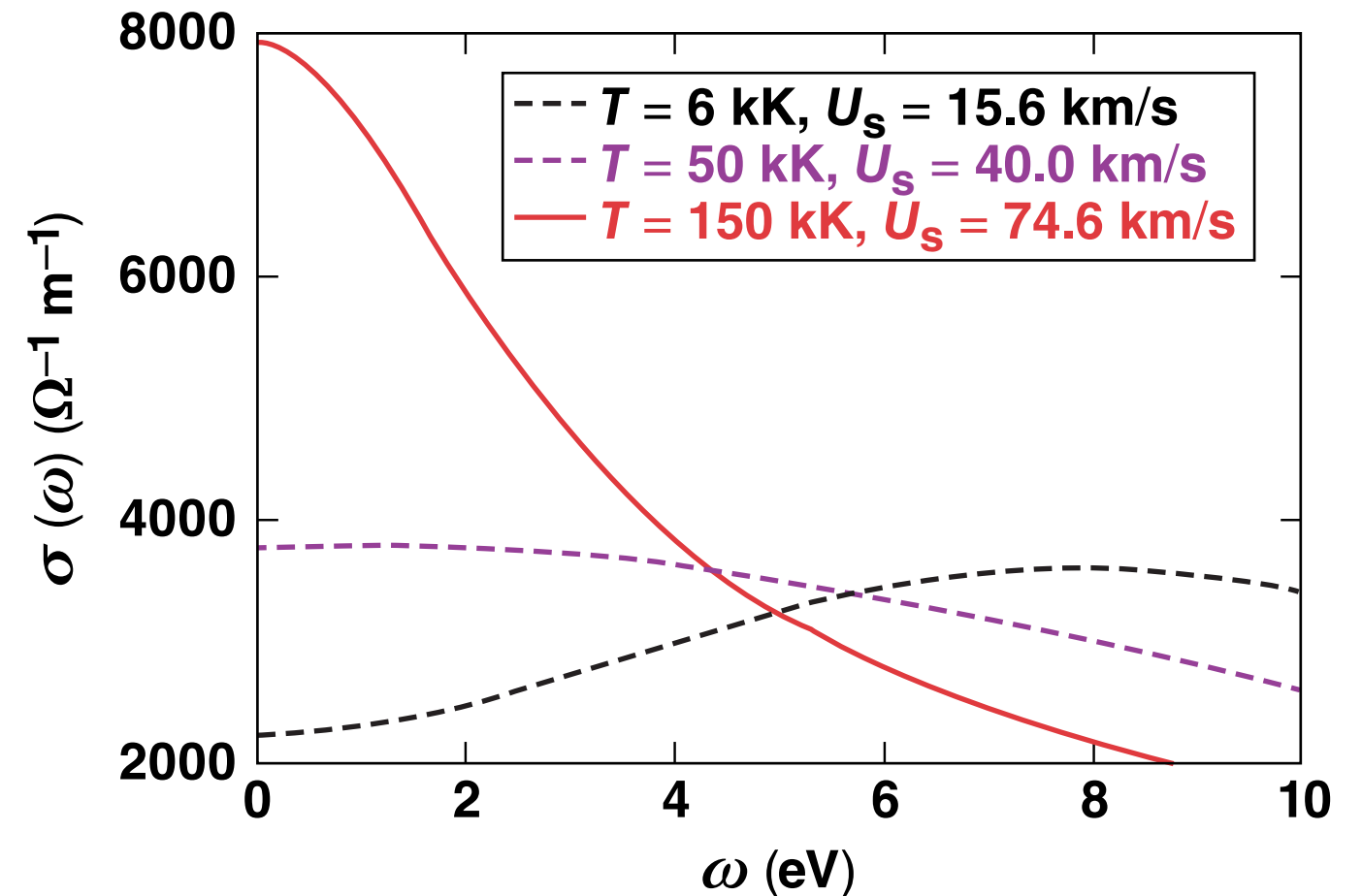
\*V. V. Karasiev, L. Calderín, and S. B. Trickey, Phys. Rev. E **93**, 063207 (2016).

## Results

Shocked  $D_2$  along the principal Hugoniot changes from molecular semiconducting liquid to atomic metallic liquid and finally to nondegenerate plasma



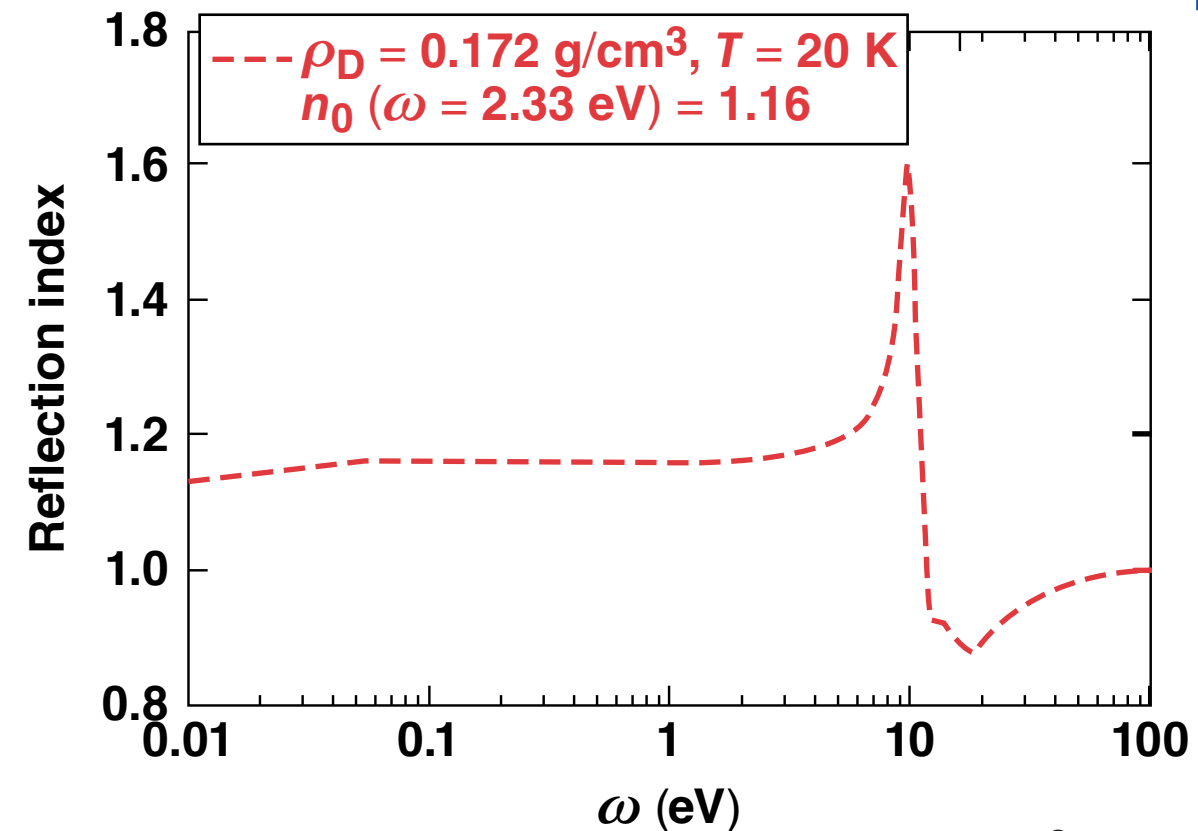
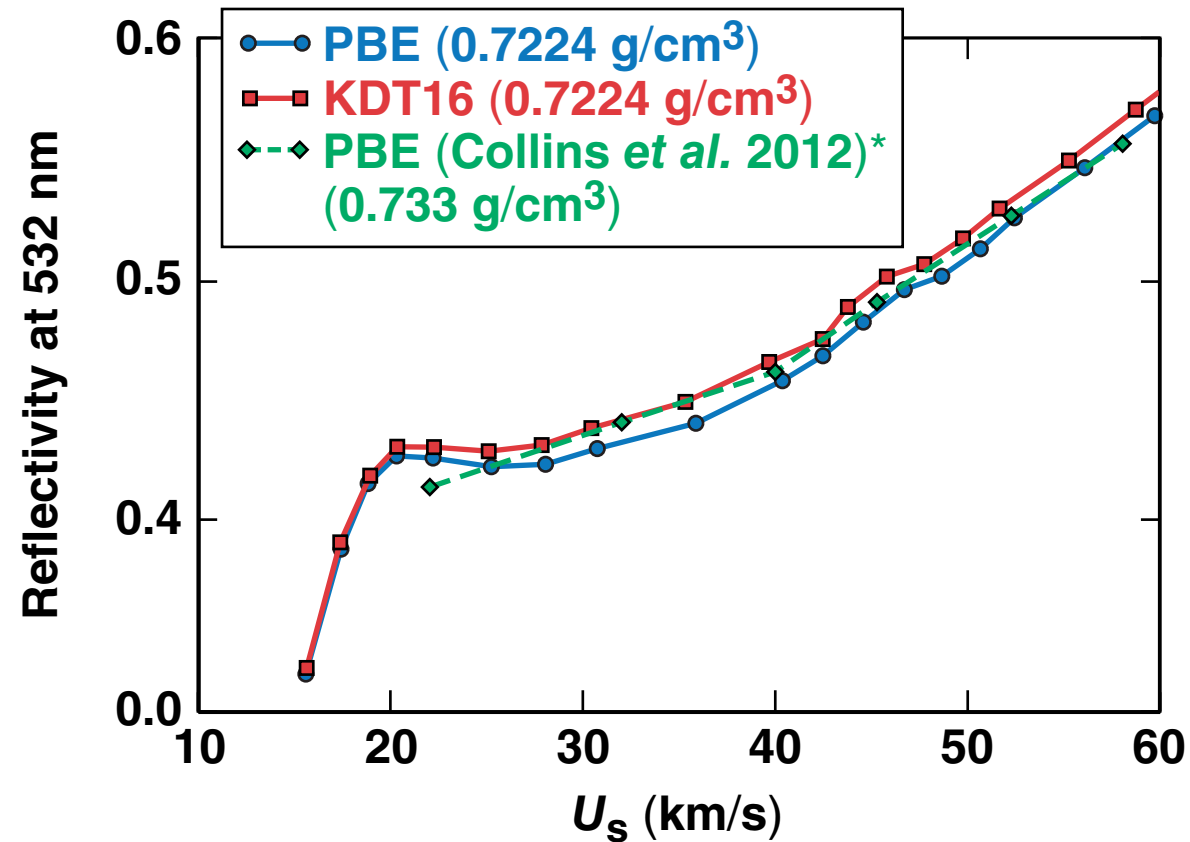
Radial D-D distribution function for three selected temperatures



Frequency-dependent electrical conductivity

## Results

As a result of thermal XC effects, the reflectivity of D<sub>2</sub> along the Hugoniot is increased by about 4% for shock speeds above 20 km/s



Reflectivity of deuterium as a function of shock speed along the principal Hugoniot

Reflectivity is defined as: 
$$r(\omega) = \frac{[n_0 - n(\omega)]^2 + k^2(\omega)}{[n_0 + n(\omega)]^2 + k^2(\omega)}$$

$n_0$  (532 nm) = 1.16 – calculated value  
 $n_0$  = 1.14 – experimental value\*\*

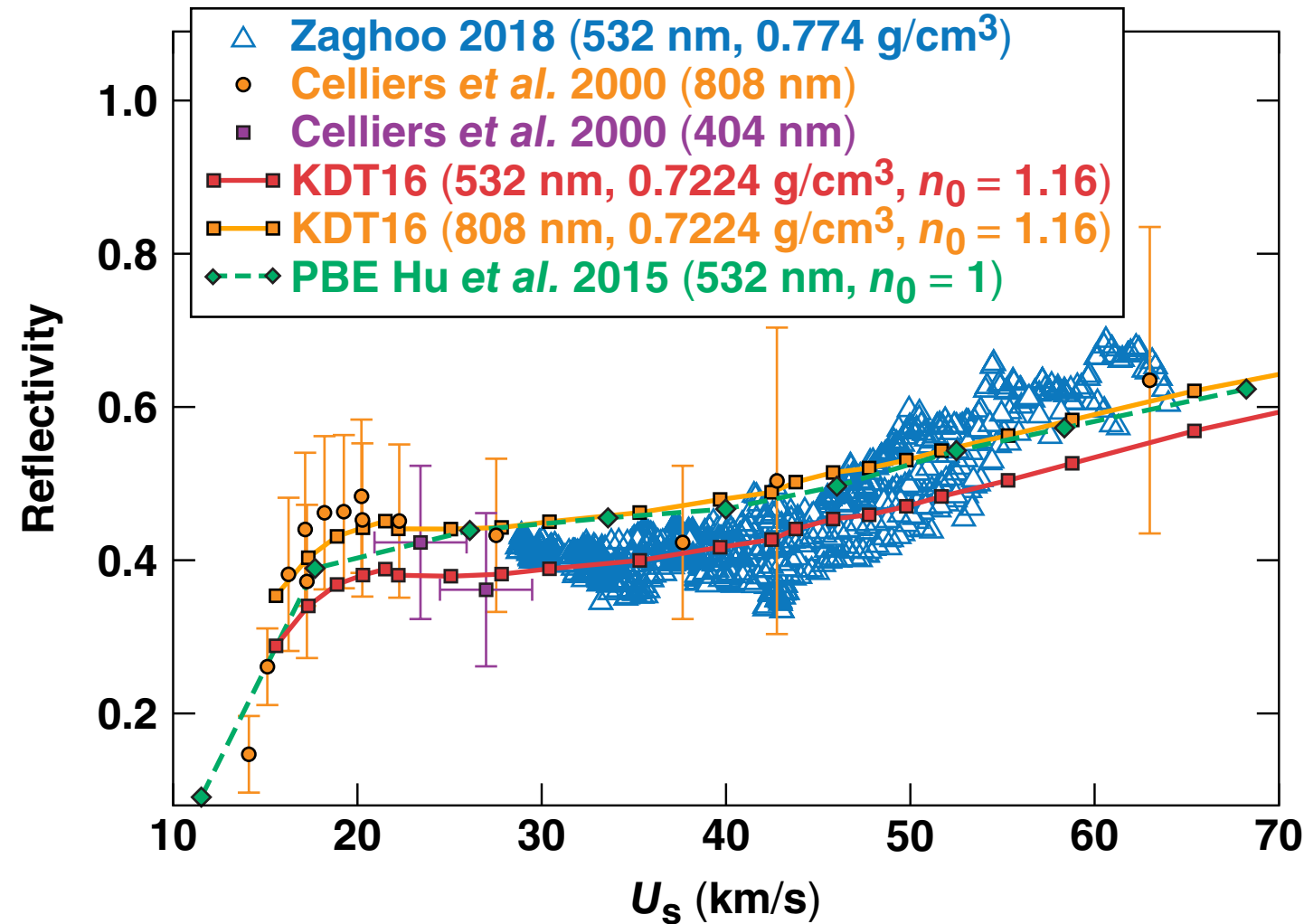
\*L. A. Collins, J. D. Kress, and D. E. Hanson, Phys. Rev. B **85**, 233101 (2012).

\*\*P. C. Souers, *Hydrogen Properties for Fusion Energy* (University of California, Berkeley, CA, 1986).



## Results

# There is good agreement with recent experimental measurements on OMEGA by M. Zaghoo

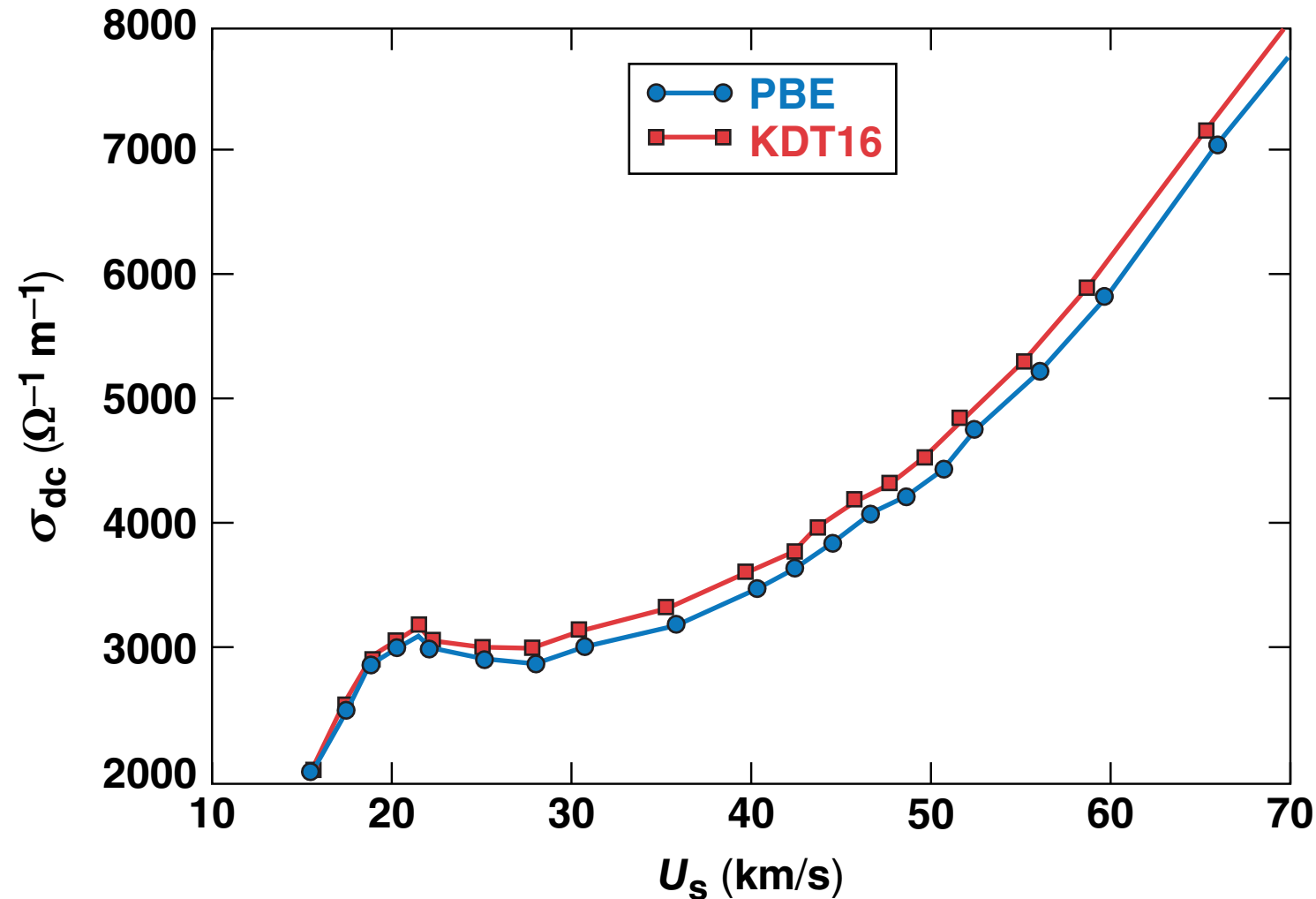


Recent experimental measurements on OMEGA: see M. Zaghoo *et al.*, “Breakdown of Fermi Degeneracy in the Simplest Liquid Metal,” to be submitted to Physical Review Letters

- Our calculations with KDT16 XC functional take into account the refraction index  $n_0 = 1.16$  of liquid deuterium in its initial state  $\rho_D = 0.172$  g/cm<sup>3</sup> and  $T = 20$  K

## Results

Due to thermal XC effects the dc conductivity of  $D_2$  along the Hugoniot is increased by about 5%



- dc conductivity is quickly increased between  $U_s = 15$  and  $20$  km/s
- The system behaves as a *liquid metal* between  $U_s = 20$  and  $30$  km/s:  $\sigma_{dc}$  decreases as  $T$  increases
- The system behaves as *plasma* for  $U_s > 40$  km/s:  $\sigma_{dc}$  increases as  $T$  increases

# Exchange-correlation (XC) thermal effects have an impact of up to 5% on the calculated properties of $D_2$ and must be taken into account for accurate predictions

- XC thermal effects account for the softening of the deuterium Hugoniot at  $P > 300$  GPa in agreement with recent experimental measurements
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