About the Cover:

During the weekly maintenance inspection, Amy Rigatti, a senior laboratory engineer, uses a white-light fiber-optic probe to check the surface of one of the 60 final turning mirrors for possible plasma scalds. These mirrors, located in the OMEGA target area, are some of the largest conventional optics on the system. The largest mirror is 14 in. × 27 in. × 3 in. and weighs approximately 70 lbs.

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Publications and Conference Presentations
In Brief

This volume of the LLE Review, covering the period January–March 1997, includes an article on the status of the optics on the OMEGA laser system after the first 18 months of operation. A vigorous program to monitor the performance of the optics has been followed since the inception of the OMEGA laser. The article presents results from these observations and defines the various types of possible damage. Many of the optics have not damaged, such as the frequency-conversion crystals, polarizers, calorimeters, and liquid crystal optics. The most significant damage has been sustained by the fused-silica spatial filter lenses. There has been no evidence of any propagation of damage downstream of damaged optics. In fact, after 1000 target shots the OMEGA laser has sustained remarkably little damage.

Other highlights of research presented in this issue are

- The development of a single-beam, ponderomotive optical trap for energetic free electrons. Numerical results show that a phase mask can form a central intensity minimum, producing a three-dimensional ponderomotive trap. A novel segmented wave plate has been manufactured and used on the T^3 laser to experimentally confirm the existence of this three-dimensional structure. Work continues to confirm the trapping properties of this unique optical device.

- A description of the new diode-pumped Nd:YLF master oscillator for the OMEGA laser. Special attention is paid to ensure long pulse operation and high stability. Experimental results are presented that confirm the excellent amplitude stability, low timing jitter, and long-term frequency stability of the new master oscillator.

- Simulations of heat transfer from localized absorbing defects to the host coating material in HfO_2/SiO_2 351-nm high reflectors. Atomic-force microscopy has shown laser-induced submicron cratering of UV multilayers, which has been attributed to nanoscale, localized absorbers. A description of the model used to simulate these absorbers is presented. When thermal conduction is the only heat-transport mechanism, very high defect temperatures are required to explain the measured damage; consequently, other physical mechanisms must be considered.

- An experimental study of target performance and mixing in titanium-doped target implosions on OMEGA. Results from a recent experiment show the predicted absorption features from a thin Ti layer. These features were used to estimate the core temperature and \( \rho R \) of the compressed target. In addition the EXAFS spectrum above the Ti K edge was observed for the first time in an implosion experiment that enabled the density of the Ti layer to be measured. These experimental techniques will be important in measuring improvements in target performance as OMEGA’s uniformity improves.

- A theoretical calculation of the dephasing time of an electron accelerated by a laser pulse. The trajectory of a charged particle, determined analytically for various pulse shapes, is then used to determine the dephasing time of an accelerated particle.

Richard Town

Editor
Status of Optics on the OMEGA Laser
after Eighteen Months of Operation

The OMEGA laser has sustained approximately 1000 target shots over its first 18 months of operation without significant damage to the optics. Both rod and disk amplifiers are used in the OMEGA laser chain; after each amplification stage at $1\omega$ the beams are spatially filtered to remove high-spatial-frequency noise in the beam and to ensure correct image relaying. Optical damage thresholds dictated the minimum beam diameter in each stage and fixed the magnification between stages. The final 28-cm beam propagates through thin-film polarizers before reaching the frequency-conversion cells. Frequency conversion to the third harmonic (351 nm) is carried out using the polarization-mismatch method developed at LLE. A set of mirrors transports the $3\omega$ beams through a final focus lens, and the last optic in the beam path serves as the vacuum barrier for the target chamber.

Fundamental to LLE’s OMEGA operating philosophy is a maintenance plan to ensure (1) prevention of costly damage to system components and (2) reliable and efficient operation of the system. One part of this preventative maintenance plan involves an estimated 3000 optics on the OMEGA laser system, not including laser glass, driver-line optics, and diagnostic components. The Optical Manufacturing Group is responsible for coordinating the inspection of these optics and tracking this information. On a periodic basis, the optical components are inspected for laser damage, coating degradation, and particulate contamination. During planned shutdown periods, extensive maintenance (cleaning, recoating) and replacement of optics occur. To date, the majority of optics on the OMEGA laser system have not been damaged, and there is no propagating bulk or surface damage to components downstream of damaged optics. While the current optics replacement rate is below the anticipated rate of 10% per year, this rate is expected to increase as the laser ages. In the sections that follow, a review of the types of optical component degradation is presented.

**Laser-Damage Classification**

In discussing laser damage, a distinction is made between operational and accidental system damage. An optic damaged when the laser operates within normal design limits is classified under operational damage; whereas, accidental damage occurs when the laser operates outside the design limits. This classification is useful because accidental damage can result in significant damage to an optic, but it is not an indication of continuing problems with that component. Tracking optics damaged due to routine laser operation results in statistical information about the longevity of a particular optic; this information is incorporated into decisions regarding an appropriate spare optic inventory. Observations of an optic’s mean lifetime are necessary to determine an effective and economical spares program.

1. **Operational Laser Damage**

   As the laser continues to operate, it is not surprising to observe operational damage in optics located at high-fluence positions of the laser. Figure 70.1 shows a staging diagram that plots the peak design fluence—average fluence times a 1.8 intensity modulation factor—at each stage of a single beamline on OMEGA. The bold lines indicate areas where laser damage is occurring at present. Specific damage morphologies are presented on p. 52.

2. **Accidental Laser Damage**

   While accidental laser damage occurs infrequently, it can result in significant optics damage. During the activation stage of OMEGA, six optics were damaged in a single shot when light back-propagated after striking the edge of an improperly positioned spatial filter pinhole assembly. The ring of damage is located at the edge of the beam diameter and was caused by the radial edge gain from the rod amplifiers. This beam imprint was observed on several mirrors and the liquid crystal component shown in Fig. 70.2.

Another instance of accidental damage was the development of a small damage site in one-third of the $3\omega$ final focus lenses. A design analysis that locates the focus of unwanted surface reflections eliminated the possibility of a ghost reflection as the cause of this damage site. The single, bulk damage site is less than 1 mm in diameter and is located at the optic’s center near the exit surface. The damage has not propagated to
the blastshield optic located about 75 mm in front of the lens or to opposing beam port optics. Figure 70.3 shows a timeline of the discovery of damaged focus lenses. At the end of OMEGA activation, a large number of focus lenses were suspected to have damage, with only a slight increase since the initial observation. We believe this damage does not result from the normal operation of the laser because the plot of energy does not correlate with the number of damaged lenses reported. However, continued laser operation does contribute to the growth of the existing accidentally damaged site. During activation, a train of short pulses propagated down the system and were frequency converted to \(2\omega\) instead of \(3\omega\), which may have caused the damage. Since the sol-gel coating was designed for \(3\omega\), a 2%–3% surface reflection occurs at \(2\omega\). Analysis of multiple beam reflections inside the lens results in the formation of a \(2\omega\) caustic at the lens’ center position 2 mm from the exit surface.

### Damage Morphologies

The damage observed on an optic can be classified as either stable or unstable. Given that the optical components will damage, it becomes important to distinguish between damage that is catastrophic to laser operation and damage that is tolerable. Stable damage does not affect the laser’s performance and does not cause propagation of damage to other downstream optics. In addition, this type of damage does not appear to grow significantly on successive laser shots. Unstable damage does grow on subsequent laser shots and eventually prevents the safe operation of the laser. Unstable damage may result in catastrophic failure of a component; additionally, this type of damage could cause propagation of damage to other optics in a beamline. For these reasons, optics with unstable damage are monitored frequently for changes in damage size, and replacement occurs before the damage reaches a critical value.
1. Stable Damage

The occurrence of stable damage on OMEGA has been documented since activation of the laser system. Two forms of damage have been observed: (1) self-focusing damage in spatial filter lenses and (2) plasma scalds on transport mirrors.

**Self-focusing damage** is seen infrequently in OMEGA lenses. Currently, nine fused silica lenses have evidence of “angel-hair” tracking, which occurs in the bulk material. These tracks appear as a linear sequence of microscopic damage in the bulk of the optic aligned with the propagation axis. Table 70.I provides a list of the damaged components and the peak fluences they are subject to.

Figure 70.4 shows a photograph of self-focusing damage observed on an OMEGA lens. The large white spot is in the exit surface of the lens, and the typical diameter of this damage area is 1 mm. This large area contains a number of smaller, individual damage sites formed when the self-focusing tracks intercepted the output surface of the lens. These sites do not seem to grow on successive laser shots.

**Plasma scalds** are frequently seen on OMEGA’s $3\omega$ transport mirrors. As seen in Fig. 70.5, scalds appear as a

<table>
<thead>
<tr>
<th>Component</th>
<th>Damaged Lenses/Total Lenses</th>
<th>Design Peak Fluence (J/cm²) with 1.1-ns pulse</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage-E input spatial filter lens (1(\omega))</td>
<td>1/60</td>
<td>5.0</td>
</tr>
<tr>
<td>Stage-F input spatial filter lens (1(\omega))</td>
<td>5/60</td>
<td>6.6</td>
</tr>
<tr>
<td>Primary pickoff lens (3(\omega))</td>
<td>3/60</td>
<td>2.9</td>
</tr>
</tbody>
</table>

Figure 70.3
Observation timeline of OMEGA final focus lenses. The left axis plots the number of damaged focus lenses observed over the lifetime of the laser. The right axis plots the $3\omega$ cumulative energy per beam over that same time frame.

Figure 70.4
“Angel-hair” tracking damage observed in the bulk glass of an OMEGA stage-F input lens. The large bright area is the exit surface of the lens.
discoloration on the coated surface of the mirror. Scalds are initiated where particulates are on the mirror surface during a laser shot and are caused by an increase of temperature on the surface during plasma formation. OMEGA transport mirrors are not contained in enclosed structures but are mounted in open, upward/downward-facing structures. This open architecture, which allows personnel access to target chamber equipment, results in an increased level of contamination on target bay optics as opposed to laser bay optics, which are vertically mounted with protecting covers on the structures. These plasma-scald defects do not grow in size on subsequent laser shots, but the number of scalds per surface may increase. At this time, no reflectance data is available to determine how plasma scalds affect performance of the mirror coating.

2. Unstable Damage

OMEGA optics that exhibit unstable damage include (1) tantala/silica-coated beam splitters, (2) BK-7 spatial filter lenses, and (3) fused-silica, input spatial filter lenses. Damage to these optics continues to grow on subsequent laser shots. The rate of growth and size of damage are dependent upon the type of damage observed.

All tantala/silica beam splitters located in OMEGA’s C-split region (which is the region with the highest fluence of any multilayer coating) have significant damage after 18 months of laser operation. From Fig. 70.6, it is apparent that this damage was not accidental but operational laser damage. As the beam splitters continued to see an increase in \( I_0 \) cumulative energy, the observed number of damaged beam splitters increased. Microscopic evaluation of a beam splitter revealed coating-damage sites that were initially 50 to 100 \( \mu m \) in size and 7 \( \mu m \) deep. This depth indicates that the tantala/silica coating is damaged at the substrate interface. The size of these damage sites continues to grow on successive laser shots. Figure 70.7 shows a photograph of a beam splitter with the damage sites illuminated within the beam diameter.

During the OMEGA Upgrade, two types of beam splitters were produced using either the tantala/silica design or the hafnia(metal)/silica design. Hafnia(metal)/silica-coated beam splitters located in the same area as the tantala/silica beam splitters show no signs of coating damage, even though they have the same test damage threshold. These test damage thresholds (reported in Fig. 70.8) were taken on a limited number of sites, and, as a result of this limited statistical process,
defect sites may have been missed. The results on OMEGA are equivalent to full-aperture testing, and this type of testing has revealed significant differences in damage thresholds between the two materials. The highest fluence seen by a multilayer coating is in the C-split area (which is 4.1 J/cm²). Beam splitters in other areas see a lower fluence (typically ~1 J/cm²), and neither design has demonstrated any sign of significant damage in these low fluence areas.

Isolated bulk damage sites have been seen in a number of OMEGA BK-7 spatial filter lenses. A summary of the location and number of damaged optics is provided in Table 70.II. The peak design fluence is the average fluence times a 1.8 intensity modulation factor.

Each lens has one to four damage sites, ranging in size from 50 to 800 µm, occurring at varying depths within the bulk glass. Photographs of damage sites from an OMEGA lens are shown in Fig. 70.9. Microscopic evaluation revealed damage sites with radial fractures forming a circular pattern perpendicular to the beam. This type of fracture pattern is characteristic of platinum-inclusion damage. Previous data reported by LLNL showed that platinum inclusions in phosphate glass cause fractures when irradiated by laser pulses above a threshold value of 2.5 to 3.0 J/cm² with a 1-ns pulse. These fractured sites do grow upon repeated irradiation, but this growth rate is slow with respect to a bimonthly inspection cycle. During inspection cycles, sizes are visually estimated by observation with a white-light source. Quantitative microscopic evaluation is difficult on in-situ optics inspection, so an accurate estimate of damage growth rate is not available. Currently, we have not observed any damage propagation from these lenses to other optics in the beam path.

<table>
<thead>
<tr>
<th>Component</th>
<th>Damaged Lenses/Total Lenses</th>
<th>Design Peak Fluence (J/cm²) w/1.1-ns pulse</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stage-C relay lens (in/out)</td>
<td>8/60</td>
<td>2.3</td>
</tr>
<tr>
<td>Stage-E output lens</td>
<td>7/60</td>
<td>3.0</td>
</tr>
<tr>
<td>Stage-F output lens</td>
<td>34/60</td>
<td>3.6</td>
</tr>
</tbody>
</table>

Figure 70.7
Coating damage observed on a 5.5-in. × 7.5-in. OMEGA stage-C, tantala/silica beam splitter. The highest fluence seen by a multilayer coating is in the C-split area.

Figure 70.8
Damage thresholds for tantala/silica and hafnia(metal)/silica beam-splitter coatings measured at 1054 nm with a 1-ns pulse at p-polarization.

Table 70.II: Summary of the number of optics with bulk damage sites.
Large-scale fractured damage sites have been observed in OMEGA’s stage-C, -D, -E, and -F input fused-silica spatial filter lenses. These areas of the system see some of the highest $1/\omega$ fluences and exceed the 2.5 J/cm$^2$ criterion for the use of fused silica as opposed to BK7 glass (see Fig. 70.1 for the peak fluence in the OMEGA laser chain). The highest peak design $1/\omega$ fluence is at the F-input lenses with a fluence of 6.6 J/cm$^2$. The lowest $1/\omega$ fluence seen by these lenses is the C input, which has a fluence of 4.1 J/cm$^2$. Figure 70.10 shows a good correlation between the number of damaged lenses and the $1/\omega$ cumulative energy per beam plotted over the same time frame. As the $1/\omega$ cumulative energy per beam increases, the number of lenses with fractured damage sites also increases, indicating a form of operational damage.

The damage occurs on the exit vacuum side of the lens at random locations, and the sites grow in size on subsequent laser shots. The damage does not correlate to hot spots in the beam and is believed to be initiated at surface particulate sites. Some possible contamination sources are particulate blowoff from the pinhole and debris from fabrication of the spatial filter vacuum tubes. A fraction of the beam strikes the edge of the pinhole, causing material to vaporize and redeposit on the vacuum side of the input spatial filter lens. Investigation into the cause of this damage is ongoing. The fracture pattern from one of these damage sites is seen in Fig. 70.11.

The vacuum surface of an OMEGA spatial filter lens is under tensile stress, and any damage to this vacuum surface can...
lead to catastrophic crack growth if the flaw size reaches a critical value $a_c$. The critical flaw depth $a_c$ depends on the shape of the flaw with respect to the applied stresses and can be calculated from\(^{14}\)

$$a_c = \frac{(K_c)^2}{\pi(Y\sigma)^2},$$

where $K_c$ = fracture toughness of the glass, $Y$ = geometrical factor of the flaw, and $\sigma$ = bending stress induced by atmospheric pressure.

Actual defects on OMEGA spatial filter lenses are shallow and elliptical, and these defects can be simulated with a half-penny-shaped defect ($Y = 1$) that has a surface diameter twice the defect depth. For an OMEGA stage-F input lens, 25 mm thick and 283 mm in diameter, a critical flaw depth of 8 mm is calculated for a half-penny defect on the vacuum side of a lens subjected to a tensile stress of 615 psi. A defect of this size will be easily detected before catastrophic failure occurs.

It is also important to understand how these lenses will fracture to avoid implosion of the lens when it is under a full vacuum load. Lens fracture on Nova and Beamlet was modeled at LLNL, where it was reported that the design of a “fail-safe” lens probably requires a stress $\sigma < 700$ psi.\(^{15}\) A fail-safe lens would generate one large fracture and would not implode. The maximum bending stress for an OMEGA stage-F input lens is 615 psi and occurs at the center of the lens. If the model is correct, these lenses under full vacuum should not implode into several fragments when defects reach their critical flaw size but should crack into two pieces and lock together as long as the mount restrains the radial motion of the fragments. Although damage on the vacuum side of OMEGA spatial filter lenses has been observed, there has been no incident where an OMEGA spatial filter lens has cracked into several pieces. For safety concerns, OMEGA optics will be removed when defects reach one-half their critical flaw size (i.e., when the depth is 4 mm). For convenience we measure the surface trace in situ and replace any lenses with a surface trace of 8 mm (which would imply a depth of 4 mm if the flaw is penny shaped). We have replaced two lenses that had surface traces of 8 mm. Later depth measurements showed only a depth of 2 mm, well within the criteria for failure.

### Optical Property Changes

OMEGA’s sol-gel coatings show a significant change in reflectivity when exposed to a vacuum. A guided wave spectrometer is used to measure the reflectivity of optics mounted on OMEGA. While the instrument is not photometrically accurate, the shape of the spectral curve does provide information on the performance of the coating. The spectral data in Fig. 70.12 was taken on a $1\omega$ (1053-nm) sol-gel-coated spatial filter lens. While the S1, non-vacuum-side, reflectivity curve is as expected for a $1\omega$ antireflection coating, the S2, vacuum-side data indicates that the porous sol-gel coating has adsorbed some organic material, which has affected its coating performance. Evaluation of the contaminated sol-gel coating by gas chromatography mass spectrometry detected the presence of...
vacuum pump oil. This coating problem is seen on all OMEGA sol-gel-coated spatial filter lenses that are pumped by a mechanically pumped system. Hard-oxide dielectric coatings pumped under similar vacuum conditions and sol-gel coatings pumped by an ion sublimation pump show no change in reflectivity after exposure to a vacuum. Since OMEGA’s optical layout was designed with the assumption of a 4% light loss per surface, damage is not expected from ghost reflections and no system damage has occurred as a result of this coating problem.\textsuperscript{16} Two solutions to this sol-gel-coating problem are being investigated: (1) replace the sol-gel coatings with hard-oxide dielectric coatings and (2) improve the spatial filter pumping system. Sol-gel coatings were used on all fused silica spatial filter lenses since these lenses have the highest $\omega$ fluence on the system and sol-gel coatings have, in the past, shown considerably higher damage threshold than hard-oxide coatings. Recent improvements in the hard-oxide coating process have resulted in increased damage thresholds, which now make them viable replacements to the sol-gel type.

### Target Chamber Optics

After 1000 target shots, no target chamber optics have been replaced because of damage. The inside target surface of the blastshield optics has degraded from the impact of target debris, and the damage is in the form of shallow pits ranging in size from 50 $\mu$m to 1 mm. Recently, self-focusing damage has been observed in several blastshields’ optics, which serve as the vacuum barrier for the target chamber. Damage to the outside blastshield surface (non-vacuum side) is minimal and usually occurs as a result of mishandling during blastshield replacement. Degradation in the blastshields’ sol-gel coating occurs with prolonged exposure (over 100 days) to the target chamber. This degradation leads to reduced transmission of laser energy to target center. The on-target imaging system (OTIS) diagnostic is used to measure the irradiation uniformity and can therefore be used as an \textit{in-situ} measurement of the performance of the sol-gel coating. We use the OTIS measurement to recommend replacement of the optics with the lowest UV transmission. The baseline replacement rate of blastshield optics is 20 per month; optics are replaced during a regular maintenance day.

### Conclusion

LLE has implemented a plan to maintain the quality of OMEGA optics. This preventative maintenance plan involves frequent inspections and \textit{in-situ} cleaning of optics by a skilled support group as well as proper training of laser operations personnel to prevent optics handling damage. Damaged optics are placed on a critical optics list and are tracked frequently for damage growth. This critical optics list is used to report the current condition of OMEGA optics to the Laser Facility Manager.

This article has focused on specific optics that have started to damage after 18 months of OMEGA laser operation. Components that have \textit{not} damaged include frequency-conversion crystals, polarizers, calorimeters, and liquid-crystal optics. In addition, there has been no propagating bulk or surface damage to components downstream of damaged optics.

### ACKNOWLEDGMENT

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9. C. T. Cotton (private communication).


16. C. T. Cotton (private communication).
A Single-Beam, Ponderomotive-Optical Trap for Energetic Free Electrons

Traditionally, there have been many advantages to using laser beams with Gaussian spatial profiles in the study of high-field atomic physics. High peak intensities are achieved due to their focusability, they are easily generated in most laser systems, and their focal region can be described analytically. However, free electrons interacting with such a field are rapidly accelerated out of the high-intensity region via the ponderomotive force (which is proportional to the gradient of the laser intensity).1,2 As a result, the electrons’ interaction time with the intense portions of the laser focus can be much shorter than the pulse duration. In order to observe harmonic generation from oscillating free electrons, one must first control the expulsion of electrons from the focal region.3 This confinement can be most easily achieved by creating an intensity minimum at the focus, thereby using the ponderomotive force to push the electrons toward the central minimum. If this intensity minimum is non-zero, then the electrons can interact with intense fields while remaining trapped. Such ponderomotive trapping has been proposed in the past,4,5 and specific laser-based schemes to trap electrons in the radial direction have been described.6,7 To our knowledge, such focal spots have not been generated with a high-power laser. In addition, these proposed traps would not confine electrons in the axial (laser propagation) direction. In this article we will present a novel scheme to trap electrons in three dimensions with a single laser beam.

Numerical Results

A “trapping” focal region consists of an intensity minimum surrounded on all sides by higher intensities. To understand how to create such a region, it is important to adopt a formalism to describe the propagation of light. Huygens’ principle, which states that we can consider every point on a wave front to be a point source for a spherical wave, makes it possible to find the field distribution in some “observation” plane if the field distribution in an earlier “source” plane is known.8 A computer program has been written to calculate the three-dimensional focal region from an arbitrary, monochromatic laser beam. The “source” plane is the field distribution at the lens, and the “observation” plane is scanned through the focal region. The incident intensity distribution can be created mathematically (Gaussian, super-Gaussian, flat-top, etc.) or can be entered as a digitized image. The incident phase front is assumed to be uniform, and the lens is assumed to be perfect (although the addition of aberrations is possible). The beam can be passed through phase and amplitude masks on-line in an effort to alter the shape of the focal region.

By passing the beam through amplitude masks, losses are introduced into the system, yet the shape of the focal region is changed only slightly. Figure 70.13(a) shows an incident Gaussian beam [where \( w \) is the \( 1/e^2 \) (intensity) radius]. Figure 70.13(b) shows the intensity distribution of the focal region as a function of \( z \) (axial or laser propagation direction) and \( r \) (radial direction). The Rayleigh range (\( z_0 \)) and the \( 1/e^2 \) waist (\( w_0 \)) are shown in the figure. Figure 70.13(c) shows the focal spot at \( z = 0 \). Blocking the center of the beam [Figs. 70.13(d)–70.13(f)] or blocking an annular section [Figs. 70.13(g)–70.13(i)] has little effect on the intensity distribution near the focus. A centrally peaked distribution is formed in all cases.9

As Casperson has shown,10 modulating the phase of the incident beam can result in deep far-field amplitude modulation with little loss in total energy. This can be accomplished by placing phase masks in the path of the beam. Of particular interest is the effect of binary phase plates, which add either zero or \( \pi \) phase to portions of the beam. If half of the Huygens’ spherical waves encounter a \( \pi \)-phase shift while the other half do not, we can expect complete destructive interference where they meet. For a focused laser beam, this occurs at the center of the focal region. A simple, two-zoned binary phase plate is shown in Fig. 70.14(a). By passing a Gaussian beam through this plate and focusing it, an altered intensity distribution [Fig. 70.14(b)] is formed. It is important to note that this distribution is not symmetric about the \( z \) axis and, therefore, would confine particles in only one dimension. The focal spot is shown in Fig. 70.14(c). A beam similar to the TEM\(_{01}^*\) mode (commonly referred to as a “donut” mode) can be generated by passing a Gaussian TEM\(_{00}\) through a smoothly varying helical phase plate [Fig. 70.14(d)]. Such a phase plate has been generated for millimeter11 as well as optical wavelengths.12,13
The resulting focal region [Figs. 70.14(e) and 70.14(f)] confines electrons in the radial direction only. It is also difficult to “tune” the trap minimum away from zero. A scheme has been proposed that combines a donut beam focus with a centrally peaked focus. The added complexity of mixing two beams results in a focal region with a tunable center intensity, but the trap would not confine particles in the axial direction.

The binary phase plate shown in Fig. 70.14(g) contains only two zones, yet the focal spot [Fig. 70.14(i)] is surprisingly similar to the one generated by the complicated helical plate. The donut shape near \( z = 0 \) confines electrons in the radial direction, and the centrally peaked regions away from \( z = 0 \) provide axial trapping [see Fig. 70.14(h)]. The focal region is shown in detail in Fig. 70.15. The \( \pi \) region of the phase plate

---

Figure 70.13

The effects of amplitude masking on the intensity distributions of a focused Gaussian beam. The first column shows three different near-field intensity distributions. The second column shows the intensity distributions as a function of \( z \) and \( r \) (the center of each image corresponds to \( z = 0, r = 0 \)). The third column shows the focal spots. In order to show the maximum contrast, each image is normalized to its peak value. Note that all of the focal regions are centrally peaked.
A SINGLE-BEAM, PONDEROMOTIVE-OPTICAL TRAP FOR ENERGETIC FREE ELECTRONS

has a diameter of 1.65 \( w \) [where \( w \) is the \( 1/e^2 \) (intensity) radius of the incident Gaussian beam]. This results in a \( \pi \)-phase shift for half of the incident field. The calculated intensity in the focus is normalized to the peak intensity in the absence of the phase plate. The \( r \) and \( z \) positions are normalized to the unaltered beam waist \( w_0 \) (\( 1/e^2 \) radius) and the unaltered beam Rayleigh range \( z_0 \), respectively. Figure 70.15(a) shows a surface plot and Fig. 70.15(b) shows a contour plot of the trapping region. There is an exact zero in intensity at the center of the focus, with intensity walls ranging from \( \sim 8\% \) to \( \sim 30\% \) (of the unaltered peak intensity) in all directions. The trapping region has a volume of complete trapping of \( \sim 2w_0^2z_0 \) (bound by the solid contour line of 8.2\%). By changing the size of the \( \pi \) region of the phase plate (or, equivalently, by changing the size of the incident beam), the destructive interference at the center of the focus will not be complete, creating a non-zero minimum. Figure 70.16(a) shows the calculated focal distribution for a Gaussian beam incident on a phase plate with a

Figure 70.14
The effects of phase masking on the intensity distributions of a focused Gaussian beam. The first column shows three different phase masks. The second column shows the intensity distributions as a function of \( z \) and \( r \) (the center of each image corresponds to \( z = 0, r = 0 \)) when the phase mask is placed before the incident beam. The third column shows the focal spots. In order to show the maximum contrast, each image is normalized to its peak value.
π-region diameter of 2.20 \( w \). Figure 70.16(b) shows a contour plot of the trapping region. In this case, the bottom of the trap is ~17% of the unaltered beam peak intensity, and the trap walls range from ~24% to ~50%. The trapping volume is ~\( w_0^2z_0 \). This focal region is ideal for trapping electrons in a high-field region.

**Experimental Setup**

The phase masks described above can be made by using photolithographic techniques. However, for the particularly simple geometry that produces a suitable trapping region, a novel segmented wave-plate approach has been developed. A half-wave plate is typically used to rotate the polarization angle of an incident, linearly polarized beam of light. This is a result of the retardation of π phase between two orthogonal incident polarizations. However, if part of the incident beam can be made to travel through the plate as a fast wave while the other travels as a slow wave, a π-phase shift will be created between the two portions. To accomplish this, a 4-cm disk was cut from the center of an 8-cm mica half-wave plate. The disk and annulus were then mounted individually on cross hairs and aligned to the beam path (as shown in Fig. 70.17). In Fig. 70.17, the laser is polarized in the vertical direction, and the annulus is arranged such that its \( e \) axis is vertical, while the disk has its \( o \) axis vertical. This results in a π-phase shift of a portion of the incident field. The size of the disk was chosen such that approximately half of the incident field passed through it. This resulted in near-zero intensity at the center of the focus. By rotating the two pieces as a unit, one can rotate the polarization of the incident beam without introducing additional optics or changing the shape of the focal region. Also, as long as one does not require a single polarization direction in the focal

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**Figure 70.15**

(a) A computer-generated trapping focal region with zero intensity at its center (π-region diameter = 1.65 \( w \)). (b) A contour plot of the trapping region. The volume of complete trapping is bound by the solid contour line at 8.2%.

**Figure 70.16**

(a) A computer-generated trapping focal region with 17% intensity at its center (π-region diameter = 2.20 \( w \)). (b) A contour plot of the trapping region. The volume of complete trapping is bound by the solid contour line at 23.6%.
region, the depth of the trap can be tuned by rotating the central disk away from 90°. This results in a polarization rotation of the inner portion of the beam, which will put some of the field into the noninterfering orthogonal polarization, thereby filling in the minimum. The extreme case is to rotate the disk a full 90°, back to its original position, which produced an ordinary, centrally peaked focus.

**Experimental Results**

To image the altered focal spot, the wave-plate arrangement was aligned to the beam path of the tabletop terawatt laser (T³) directly before the focusing lens \( f = 212 \text{ cm} \). The focal region was imaged with a CCD camera coupled to a 10× microscope objective (Fig. 70.18). The camera-objective combination was moved together to map out the focal region. A single laser shot was taken at each position, and each image was minimally smoothed and background subtracted. The scan was generated with ~40-mJ, ~2-ps infrared laser pulses. By firing the final, single-pass amplifier, energies of ~1 J are achieved with no noticeable change in the near- or far-field characteristics of the beam. The unaltered beam’s peak intensity typically reaches \( 10^{18} \text{ W/cm}^2 \).

Figure 70.19(a) shows the focal spot created without the wave-plate arrangement in place. The beam diameter is approximately 1.5× the diffraction limit. Figure 70.19(b) shows the focal spot with the wave-plate arrangement set to 90°. Despite the deviation of the unaltered beam from the diffraction limit, there is a well-defined minimum in the center of the altered spot. Figure 70.19(c) shows the focal spot with the wave-plate arrangement in place, but set to 0°. Here, the wave plate is set to its original, unaltered configuration, and the beam has returned to its original shape. Figures 70.20(a) and 70.20(b) show the lineouts of the altered beam in the x and y directions at \( z = 0 \). The x and y positions are normalized to the experimentally determined beam waist of the unaltered beam. Figure 70.20(c) shows the intensity of the beam at \( r = 0 \) as a function of \( z \). The intensities in Fig. 70.20 are normalized to the peak intensity of the unaltered beam.

A more detailed scan was made with a continuous-wave beam (the oscillator of the T³ laser). Figure 70.21 shows two slices through the focal volume along the \( z \) axis. Figure 70.21(a) shows the intensity distribution in the plane \( y = 0 \), and Fig. 70.21(b) shows the distribution for \( x = 0 \). In each
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Figure 70.19
Focal spots (a) without the wave-plate arrangement in place, (b) wave-plate setup in place and set to 90°, and (c) wave-plate setup in place and set to 0°.

Figure 70.20
Lineouts of the trapping focal region. (a) Lineout in the x direction, (b) lineout in the y direction, and (c) the intensity at r = 0 as a function of z. All axes are normalized to the experimentally determined values for the unaltered beam (spot size for the x and y positions, Rayleigh range for the z positions, and unaltered beam peak intensity for the intensity values).

Figure 70.21
Contour plots of the trapping focal region. (a) In the plane y = 0 and (b) in the plane x = 0. The experimentally observed volume of complete trapping is bound by the solid contour line at 10%.
plot, there is a region of complete trapping bound by intensity walls of 10% (solid line) of the unaltered beam’s peak intensity. Although the incident beam size was not matched with the size of the wave-plate pieces, a sufficiently large portion of the incident field was shifted to create a trapping region. These experimentally obtained distributions (using a pulsed or cw beam) exhibit a local minimum in intensity at the origin along all three dimensions, making them suitable focal regions for ponderomotive trapping.

### Summary

In summary, we have produced, for the first time to our knowledge, a tunable, single-beam, three-dimensional, ponderomotive-optical trap for free electrons with a high-peak-power laser system. Neutral atoms and macroscopic, low-index particles could also be trapped in the low-field region. We have presented a novel, segmented-wave-plate approach as an alternative to a phase mask, along with experimental confirmation of the intensity distribution of the altered focal region. Experiments to image the linearly and nonlinearly scattered light (both 1 & 2ω) from the trapped electrons are being carried out.

### ACKNOWLEDGMENT

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### Appendix A: Huygens’ Principle

Huygens’ principle states that we can consider every point on a wavefront to be a point source for a spherical wave. As a result, if one knows the field in some “source plane (S’),” it is then possible to add the contributions from the individual spherical waves to find the field distribution in an “observation plane (S)” (see Fig. 70.22). The spherical wave emanating from a tiny element of area Δα’, surrounding the point (x’,y’,0) in the source plane, results in a contribution to the field in the observation plane,

$$\Delta \varepsilon (x, y, z) = -(i/\lambda) \left( e^{ikr}/r \right) \varepsilon (x’, y’, 0) \Delta \alpha’, \quad (A1)$$

where

$$r = \left[ (x - x’)^2 + (y - y’)^2 + z^2 \right]^{1/2}, \quad (A2)$$

$$k = 2\pi\lambda, \quad \Delta \alpha’ = dx’dy’, \quad \text{and} \quad \varepsilon (x’, y’, 0) \text{ is the electric field (magnitude and phase) in the source plane.}$$

For most applications, we may make the Fresnel approximation

$$\varepsilon^2 \gg \left( \frac{\pi/4\lambda}{(x - x’)^2 + (y - y’)^2} \right)_{\text{max}} \quad (A3)$$

and sum up all of the field contributions with the integral

$$\varepsilon (x, y, z) = -\left( e^{ikz}/\lambda z \right) \int \int \varepsilon (x’, y’, 0) \exp \left\{ ik \left[ (x - x’)^2 + (y - y’)^2 \right]/2z \right\} dx’dy’. \quad (A4)$$

To calculate the field at the point (x,y,z), ε(x’,y’,0) must be known for all (x’,y’). Equation (A4) can then be solved numerically.

For the case of a laser beam incident on a positive lens, the intensity distribution can be assumed to be Gaussian (as is typical for many laser systems) or it can be determined experimentally by imaging the near-field distribution. Determining the phase of the incident field is more complicated, as it involves interferometric methods. If the laser is well collimated and is found to focus to a spot size close to the diffraction limit, then the phase front can be assumed to be uniform. The effect of the lens is to simply add a phase proportional to the thickness of the lens material at any point. A plano-convex lens results in a “spherical” phase distribution,

$$\Phi (r’) = k (f^2 - r^2) \frac{1}{2} \quad (A5)$$

where f is the focal length of the lens and $$r^2 = x^2 + y^2$$ is the square of the radial location in the source plane. If we assume that $$f^2 \gg r^2$$ (the paraxial approximation), then we can perform a binomial expansion,

$$\Phi (r’) = kf \left( 1 - r^2/2f^2 - r^4/8f^4 - \ldots \right). \quad (A6)$$

The first term adds a constant phase to the entire beam and can be discarded, as can the higher-order terms since they are vanishingly small. By keeping only the quadratic term, we are left with a “perfect” lens in the context of this approach (in practice, aspherical lenses are not purely parabolic). A Gaussian laser beam that has passed through this lens will have the field distribution...
$\epsilon(x', y, 0) = A \exp\left(\frac{-r'^2}{w^2} - \frac{ikr'^2}{2f}\right)$, \quad (A7)

where $A$ is the field amplitude and $w$ is the beam radius at the 1/e point in the electric field amplitude (which is equivalent to the 1/e$^2$ point in intensity). It should be pointed out that all calculations in both this article and the computer codes use the scalar-wave approach.

REFERENCES


A Diode-Pumped Nd:YLF Master Oscillator for the OMEGA Laser

The OMEGA laser is a 60-beam laser-fusion system capable of producing a total of 30 kJ of ultraviolet (351-nm) energy on target, where the temporal profile of the optical pulse applied to a laser-fusion target can be specified in advance. To accomplish this, the laser system consists of a master oscillator, a pulse-shaping system, regenerative amplifiers (regens), large-aperture regenerative amplifiers (LARA), rod and disk amplifier chains, and frequency converters. A schematic of the laser chain is shown in Fig. 70.23. The pulse-shaping system (Fig. 70.24) is based on LLNL’s conceptual design and includes integrated-optics (IO) modulators driven by electrical waveform generators. The pulse-shaping system produces an optical pulse with a specific temporal pulse shape at the nanojoule energy level, which seeds the regens. The temporal profile of this low-energy seed pulse, when amplified and frequency tripled by the laser system, will compensate (1) for the temporal distortions caused by gain saturation in the regens and amplifiers and (2) for distortions caused by the tripling process and will produce the desired pulse shape on target. The overall gain of the OMEGA laser system from the pulse-shaping modulator to the target is approximately $10^{14}$. This large gain puts extremely severe requirements on stability, reproducibility, and reliability of the pulse-shaping system and master oscillator performance. This article details the OMEGA requirements, describes the new diode-pumped master oscillator, and presents results from this newly fielded master oscillator.

OMEGA’s Master Oscillator Design Requirements

The master oscillator for the OMEGA laser system must satisfy a number of requirements:

1. The wavelength of the oscillator must match that of OMEGA’s Nd:phosphate glass amplifiers (1053 nm). This requirement automatically defines the choice of the laser medium for the master oscillator to Nd:YLF.

2. The oscillator must operate in a single-frequency regime. This requirement enables the stable and reproducible generation of complex optical pulse shapes and assures optimal frequency conversion.

3. The master oscillator must be $Q$-switched to produce enough energy to split among four or more pulse-shaping channels and to properly seed the various regens.

4. The duration of the master oscillator’s $Q$-switched pulse must be $>100$ ns, and the timing jitter must be within $\pm 10$ ns to provide a constant pulse amplitude within the required 10-ns pulse-shaping window.

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**Figure 70.23**

OMEGA laser system for ICF experiments.
5. The master oscillator’s \( Q \)-switched pulse must be externally synchronizable to the OMEGA timing system.

At present, a flashlamp-pumped Nd:YLF laser is used on OMEGA. Although this laser satisfies all of the above conditions, maintenance and reliability considerations have led us to develop a new diode-pumped version with significantly improved performance. The long-term maximum amplitude has been increased, and frequency stability has been dramatically improved, while the complexity, maintenance requirements, and footprint of this new laser have shrunk significantly.

Currently, there are two major areas of interest in diode-pumped Nd:YLF laser development: high-power cw lasers and short-pulse \( Q \)-switched lasers. Even the most powerful cw lasers\(^5\) cannot provide enough energy within a 10-ns pulse-shaping window to meet our requirement of >100 nJ in a 10-ns pulse in each of four channels. \( Q \)-switched, diode-pumped Nd:YLF lasers\(^6\)–\(^9\) are usually designed to generate short (3- to 10-ns) pulses with high peak powers. The short pulse width makes this type of laser unacceptable for satisfying the requirement for a constant pulse amplitude within a 10-ns pulse-shaping window. Passively \( Q \)-switched, diode-pumped lasers (for example see Refs. 10 and 11) cannot be precisely synchronized.

To ensure that the laser generates a single frequency, the laser should operate unidirectionally. The most commonly used technique to achieve this involves using an optical diode (Faraday rotator). This technique does require additional intracavity elements and consequently increases resonator losses, thus rendering it unsuitable for our use. Kane and Byer\(^12\) have used nonplanar monolithic ring lasers; however, their use is restricted to laser materials with a large Verdet constant and no birefringence (Nd:YAG is such a material, but Nd:YLF is not). The most suitable way to provide unidirectional operation and \( Q \)-switching in a Nd:YLF laser is to employ an acousto-optic (A-O) \( Q \)-switch, which can be used for both birefringent\(^13\) and nonbirefringent\(^14\) materials.

The A-O \( Q \)-switched Nd:YLF laser meets most of the important requirements for the OMEGA master oscillator, namely the 1053-nm wavelength, single-frequency operation, high energy, and externally synchronizable requirements. However, close attention must be paid to the long (>100-ns) pulse width generation and high stability requirements.

There are no commercially available lasers with the specifications required for use on the OMEGA laser. In particular, the wavelength (1053 nm) and long pulse duration (>100-ns) requirements are not commonly required in commercial systems.
Laser Design

The diode-pumped, single-frequency Nd:YLF laser (Fig. 70.25) is based on a triangular ring cavity with two spherical mirrors and a prism that doubles as an active element. The resonator is very similar to the Nd:YAG laser described in Ref. 15. In that design one of the resonator mirrors was deposited on the laser element; however, in our design we have moved the active element away from one of the mirrors to avoid spatial hole burning.16 This residual hole-burning effect, when an active element is located at one of the ring cavity mirrors, cannot be fixed in our case by displacing the pumped volume from the cavity TEM_{00} mode as suggested in Ref. 17 because we use a fiber-coupled pumping diode and the pumped volume is larger than the TEM_{00}-mode volume. We use a fiber-coupled pumping diode so that the water-cooled laser diode can be removed from the laser head for enhanced laser stability. The diameter of the pumped volume for fiber-coupled diodes is relatively large (~0.4 mm) compared to other designs. This large volume reduces the efficiency of the laser but increases the overall stability of the diode-pumped laser. For our application the enhanced stability is more important than the efficiency of the master oscillator. The ring cavity has been chosen to provide traveling-wave unidirectional lasing and hence easier single-frequency operation. Both cavity mirrors are spherical with a 10-cm radius of curvature. The distance between the mirrors is approximately 30 mm. The angle of incidence for both mirrors is ~11°. The end mirror has maximum transmission for the pump radiation (797 nm) and maximum reflection for the 1053-nm laser wavelength. The output coupler has a 95% reflection coefficient at 1053 nm.

A 4 × 4-mm-cross-section, a-cut Nd:YLF element has Brewster-angled entrance and exit surfaces cut for 1053-nm operation (c axis is perpendicular to the resonator plane). Its on-axis thickness is 8 mm and has been calculated to compensate for the astigmatism from the two off-axis spherical cavity mirrors.18 To provide maintenance-free operation no adjustable mounts were used for cavity alignment. The laser was assembled on a 50 × 30 × 30-mm Zerodur base plate to minimize thermal drift and improve long-term stability. A precisely machined metal template allows accurate placement of the carefully machined mirrors (flattened barrels) to eliminate the necessity for fine alignment of these mirrors. The active element is glued to a miniature piezo-translator (Physik Instrumente) for cavity-length adjustment, which is in turn mounted on a Zerodur standoff glued to the Zerodur base plate. The A-O modulator (QS080-2G-RU1, Gooch & Housego) assures a unidirectional prelase phase prior to Q-switching. The A-O Q-switch has plane-parallel surfaces (AR coated for 1053 nm) and can be aligned without disturbing the cavity alignment. Unidirectional operation is achieved by using the self-feedback mechanism in the A-O Q-switch, which is described in detail in Ref. 19.

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Figure 70.25
Schematic of the diode-pumped, single-frequency, pulsed OMEGA master oscillator with amplitude and frequency feedback systems.
The laser is pumped by 700-µs square pulses at a 5-Hz repetition rate generated by an SDL-3490-P5 fiber-coupled laser diode (nominal 5-W output). The OMEGA front-end laser system operates at 5-Hz repetition rate that reduces thermal problems in the master oscillator and extends the lifetime of the diode. The image of the output 0.4-mm-diam fiber surface is relayed into the active element of the laser by using two 25-mm-focal-length spherical lenses AR coated for 797 nm. Both lenses are aligned and assembled together with the fiber port. The position of the pumped volume can be aligned to the TEM$_{00}$ cavity mode by adjusting the whole lens-fiber unit.

The low duty cycle of the oscillator obviates the need for a cooling system on the active element. The laser resonator is thermally uncoupled from the environment. The laser requires only two adjustments: alignment of the pumped volume in the active element and the A-O Q-switch position for unidirectional operation. The laser layout is shown in Fig. 70.26.

**Experimental Results**

We have found that a low rf power of ~5 mW$_{rf}$ is sufficient for unidirectional operation. We have achieved a very high contrast for the counter-propagating beams (>1500:1). As mentioned above, unidirectional operation is essential to maintain the single-frequency regime. In this operating mode the prelase stage exhibits regular, slowly decaying relaxation oscillations [Fig. 70.27(a)], which cause significant amplitude and temporal jitter of the subsequent Q-switched pulse. To stabilize the prelase phase we have developed a negative amplitude feedback with a constant offset. The offset provides the required rf power level to achieve unidirectional operation during the prelase phase. One of the beams diffracted by the A-O modulator is coupled into the 0.4-mm multimode fiber.
and sent to a diode that generates the feedback signal. Increased feedback increases the rf power to the A-O modulator, thus increasing the cavity losses and stabilizing the laser output. With amplitude feedback stabilization a very smooth prelase phase is observed [Fig. 70.27(b)], and the externally triggerable Q-switch leads to high amplitude stability and low temporal jitter of the output pulse.

At the lowest rf power required for unidirectional operation (~5 mW rf) the laser generates a ~300-ns pulse of ~5-µJ energy. The pulse width is defined by the removable Q-switch loss. To maintain unidirectional operation and obtain high stability and low jitter, the laser must work close to threshold. For a given resonator configuration the energy content of the Q-switched pulse is closely related to the pulse width. The self-feedback mechanism of the A-O enforced unidirectional operation is crucial for generating long single-frequency pulses because of the very low rf power required for the unidirectional prelase phase and hence low removable loss level. By increasing the offset in the amplitude feedback system and the pumping energy, we have been able to obtain stable single-frequency pulses with widths as short as 30 ns and energies of ~18 µJ. For use in the OMEGA laser chain the laser has been adjusted to generate an externally triggerable single-mode pulse of ~160-ns duration and ~10-µJ pulse energy. As a test of the laser stability and reproducibility, 100 laser pulses taken within 0.5 h with the laser operating at 5 Hz were recorded using a 1-GHz, 4-GS/s Hewlett-Packard 54720A digitizing oscilloscope. Figure 70.28(a) shows the average pulse shape (solid line) and its amplitude and temporal rms deviations (dashed lines). Figure 70.28(b) shows the same experimental data as Fig. 70.28(a), but the effect of the build-up jitter has been removed. By comparing Figs. 70.28(a) and 70.28(b) we conclude that the fluctuations seen in Fig. 70.28(a) are mostly due to the build-up time jitter (the long-term temporal jitter of the peak of the pulse is <7 ns rms). These data clearly show that the laser demonstrates excellent amplitude stability and pulse-shape reproducibility. The short-term (0.5-h) amplitude stability of the pulse has been measured to be ~0.3% rms. The long-term (8-h) stability is ~0.6% rms. The variation of the pulse width (which has an average FWHM of 159 ns) is ~0.7 ns rms. The achieved pulse duration and the remarkable stability of the pulse provide a constant pulse amplitude, with a variation of <1%, within the 10-ns pulse-shaping window. To maintain these excellent properties, the output beam must be handled very carefully. Even immeasurably small amounts of back reflections (from such sources as diagnostics, fibers, or fiber couplers) can reduce the stability significantly.

In all the experiments reported here, the laser was operated in the TEM₀₀ mode despite the large pump volume. This mode of operation, which involves operating close to threshold with an extended prelase phase, helps the laser maintain a single longitudinal and spatial cavity mode.

Figure 70.28
(a) The average pulse shape (solid line) and amplitude and temporal rms deviations (dashed lines) from the output Q-switched pulse for 100 shots taken within 0.5 h. (b) The data as in (a), but with the build-up jitter removed (all three lines, average and average ±rms fluctuations, virtually overlap). This indicates that all fluctuations in the left graph are mostly due to build-up time jitter of 7 ns rms, which is very small compared to the 159-ns pulse width (FWHM).
The optical efficiency in this Q-switched laser is ~5%. This relatively low optical efficiency is due to several factors: (1) the pump volume is large, exceeding the TEM\textsubscript{00} cavity-mode volume; (2) the output coupler has not been optimized; and (3) the pump beam is slightly vignette by the cavity mirror. However, for this application, optimal efficiency is not of major importance.

Long-term, single-frequency operation and stability are achieved by incorporating a frequency stabilization scheme. In this design 10% of the laser output is expanded and sent through a low-finesse, solid, temperature-controlled etalon to create fringes. Two fiber sensors straddle one of the fringes such that the difference between optical signals in the fibers is zero. Any fringe shift leads to a signed error signal that feeds into the (biased) PZT driver; this corrects the cavity length and drives the error signal to zero.

Conclusions

We have developed a diode-pumped, single-frequency, pulsed Nd:YLF master oscillator for the OMEGA laser system. Output pulses have been generated that have 30- to 300-ns duration and 5- to 18-\(\mu\)J energy with high amplitude stability (<0.6% rms), low timing jitter (<7 ns rms), and long-term frequency stability of <100 MHz over periods of many hours without observable dual-mode operation. The laser adjusted for 160-ns pulse width and 10-\(\mu\)J pulse energy satisfies all OMEGA requirements and is currently being incorporated into the OMEGA laser system.

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REFERENCES

Heat Transfer from Localized Absorbing Defects to the Host Coating Material in HfO$_2$/SiO$_2$ 351-nm High Reflectors

Recent atomic-force microscopy (AFM) studies of laser-induced damage morphology in HfO$_2$/SiO$_2$ UV multilayers, caused by 351-nm, 1-ns laser pulses, revealed submicron-sized craters as the dominant damage morphology in these films [see Fig. 70.29(a)]. The origin of such craters was attributed to nanoscale, localized absorbers in the film matrix, the smallest size of which was estimated to be <10 nm. However, at this time, both the exact physical nature of these absorbers and the mechanism of energy transfer to the host coating material in the promotion of damage remain speculative. Empirical evidence suggests that, at some time in the damage evolution, melting occurs; furthermore, near damage threshold, even the smallest absorbing defects are able to induce such melting to extend to about 50 nm inside the coating. For incident fluences 5%–20% above this threshold, the crater-depth distribution shifts dramatically, as measured by AFM (see Fig. 70.29), while for the lower fluences the melt processes and crater formation are largely confined to the top HfO$_2$ layer [Fig. 70.29(b)]—these processes penetrate into the next-from-the-top, SiO$_2$ layer at fluences ~20% above threshold [Fig. 70.29(d)].

In this work, by carrying out heat-transfer calculations for the same HfO$_2$/SiO$_2$ multilayer system, our goal was to answer the following questions:

a. How high a temperature must an absorbing defect reach to support film-crater formation of the type observed experimentally by AFM?

b. How does heat conduction affect the damage kinetics at these temperatures and for different defect and host characteristics?

c. May heat conduction be considered the dominant energy-transfer mechanism, or must other mechanisms be included for the process physics to remain plausible?

In the following, the model assumptions and simulation results will be presented. From these results, one concludes that, for realistically sized defects and absorption conditions for 351-nm laser light, a damage model commensurate with empirical, AFM evidence must account for energy-transfer mechanisms other than heat conduction alone.

**Methodology**

Heat-transfer modeling was accomplished by using the finite-element analysis code ANSYS in rigid-grid form. The equation of motion was treated in matrix form

$$[c] \{\dot{T}\} + [K] \{T\} = \{Q\}, \quad (1)$$

where $[c]$ represents the specific-heat matrix, $[K]$ the conductivity matrix, $\{T\}$ the nodal temperature vector, and $\{Q\}$ the nodal heat-flow vector. The model assumed *convective* heat transfer at the film/air interface and *conduction* inside both the defect and the host material. The model geometry, depicted in Fig. 70.30, contains alternating quarter-wave layers ($\lambda = 351$ nm) of HfO$_2$ and SiO$_2$ of cylindrical geometry with the $r$ axis along the film/air interface, and the $y$ axis oriented perpendicular to the layer stack. A single, cylindrical defect is placed at the thickness midpoint of the top HfO$_2$ layer, its size taking on values in accordance with data in Fig. 70.30.

Heat *generation* inside the defect is based on uniform volume absorption of the laser light at a *constant rate* throughout the 1-ns laser pulse. We assume that non-Beer’s law of absorption holds for these defects that are much smaller than a “skin depth.” For an absorbed fraction $\beta$ of the light normally incident on the defect of length $d$, the heat-generation rate inside the defect becomes

$$H_{gen} = \beta \Phi_{th} / d \tau, \quad (2)$$

where $\Phi_{th}$ is the damage-threshold fluence (5.6 J/cm$^2$) and $\tau$ is the 1-ns laser-pulse duration. As reliable absorption-coefficient data are absent for most nanoscale absorbers, $\beta$ was fixed at a value of 0.1. For a value of $d = 27$ nm, this yields a heat-generation rate $H_{gen} = 2 \times 10^{20}$ J/m$^3$ s. To evaluate the relative influence of various other parameters, such as the
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thermal-conductivity anisotropy and defect size and type, this $H_{gen}$ value was initially kept constant. Later, when agreement between empirically obtained AFM results and simulations was sought, $H_{gen}$ values were parametrically varied.

Material Properties

Two types of absorbing defects were considered:

1. Metallic Hf nanoclusters with bulk-metal thermal parameter values for $K$ (thermal conductivity), $H$ (enthalpy), and $T_m$ (melting point);

2. Off-stoichiometric HfO$_2$ film with the following parameters:
   
   $K$ – HfO$_2$ thin-film thermal conductivity,
   $H$ – HfO$_2$ bulk enthalpy, and
   $T_m$ – HfO$_2$ bulk melting point.

The absorbing-defect thermal parameter values are listed in Table 70.III.

Thin-film material property values are summarized in Table 70.IV, where $K_x$, $K_y$, and $K_z$ are the Cartesian-
coordinate components of the thermal conductivity and $\gamma$ is the anisotropy parameter for the thermal conductivity, i.e., $\gamma = 1$ for perfect isotropy. In these simulations, $\gamma = 0.1$ was chosen for the most anisotropic case. Also, in distinguishing metallic defects from HfO$_2$-type defects, thin-film anisotropy values were used for HfO$_2$-defect properties.

Latent heat of fusion was accounted for in these calculations by enthalpy $H$.

**Modeling Results and Discussion**

Instantaneous temperature contours in 2-D space (Fig. 70.31) show the temperature-field evolution within the
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film at various times after the beginning of the laser pulse. These contours represent the case of a “large” HfO$_2$ defect ($R = 20$ nm; $d = 26.7$ nm) located in the top HfO$_2$ layer. Note that in these contours the air/film interface is located at the bottom of each grid and the successive film layers stack upward. One finds [Fig. 70.31(a)] that at the end of the excitation pulse the heat generated is essentially confined to the defect itself, within which the temperature reaches a value of $2.7 \times 10^4$ °K. As time progresses, the locus of the peak temperature moves from the defect center toward the air/film interface [Fig. 70.31(b)]. As a consequence, 17 ns after the end of the pulse, the interface reaches a temperature of $1.5 \times 10^4$ °K. On the nanosecond time scale considered in Figs. 70.31(a)–70.31(d), convective heat transport at this interface remains physically irrelevant and, in effect, renders this interface an adiabatic boundary, fostering the modeled temperature buildup.

Critical to the comparison with empirical crater information are the lateral temperature contours, defining the lateral scale of the melting process. One can see that in the highly anisotropic ($\gamma = 0.1$) heat-conduction case represented in these figures, lateral melt-front propagation is fairly restricted—the melt radius remains <30 nm inside HfO$_2$, which is nearly a factor of 2 smaller than observed during AFM mapping of craters.

To determine the vertical-melt propagation through the film stack, Fig. 70.32 shows the vertical temperature around a “large” HfO$_2$ defect as a function of depth (here the air/film interface is located at the origin) at various times after the end of the laser pulse. From Fig. 70.32 it becomes apparent that within only 3 ns after the pulse, melting starts inside the SiO$_2$ layer (note the broken, vertical-layer-demarcation line between HfO$_2$ and SiO$_2$) and, by 10 ns after the pulse, reaches nearly halfway into the SiO$_2$ layer. Eventually the system starts to cool down, which sets the limit on the vertical-melt propagation. Similarly, Figs. 70.33 and 70.34 show the maximum temperature reached at any instant during the process at various depths below the defect as a function of conductivity anisotropy and defect type, respectively. For all anisotropy ratios chosen (Fig. 70.33), the SiO$_2$ layer experiences melting to some extent, up to ~75% of the entire layer. The same strong dependence of melting on anisotropy also holds for the “large” Hf-metal defect (Fig. 70.34), which at the fixed, identical heating rate is completely molten and itself isotropic ($T_m = 2506$ °K). In Figs. 70.33 and 70.34 there is a small, systematic error. The code recognizes and accounts for the change in conductivity anisotropy upon melting, but during the cool-down phase reinstates anisotropy as if the material had recovered initial crystallinity. Preliminary simulations show that this error in no way alters the seminal features or conclusions.
Ignoring the differences in absorption between a metallic and an off-stoichiometric defect and simply assuming that, over the laser pulse length, equal amounts of energy have been deposited in either one, the relative importance of defect heat capacity and internal heat conductivity for energy transfer to the surrounding film is outlined in Fig. 70.35. Due to its higher conductivity, the metallic defect attains a uniform temperature and delivers heat rapidly to its surface. This causes the surrounding HfO$_2$ film to reach higher temperatures than if the defect consisted of off-stoichiometric HfO$_2$. At the HfO$_2$/SiO$_2$ interface this difference has been mediated away by the poor conductivity of the dielectric film. The melting behavior of the SiO$_2$ layer is insensitive to the nature of the defect.

The issue now remains how, for equal energy volume density at the end of an excitation pulse, defects of various sizes (i.e., of various surface areas) affect the melting behavior of the host layer as well as that of the next-nearest neighboring layer. For the three sizes (small/medium/large) considered, the volumes scale as 1:6:37. Figures 70.36 and 70.37 plot the maximum temperatures reached inside the HfO$_2$ and SiO$_2$ layers for the three cases—Fig. 70.36 representing a dielectric defect and Fig. 70.37 a metallic defect. For the same reason as given in the discussion of Fig. 70.35 (i.e., the higher thermal conductivity of the metal), the metallic defects shed heat effectively during the laser pulse, providing for larger maximum-temperature differences between the defects with the various surface-to-volume ratios than for defects of dielectric composition. At threshold, neither dielectric nor metallic, small defects contain enough heat to melt the SiO$_2$ layer, indicating a critical defect size for melting to occur (at threshold) inside the SiO$_2$ layer. Tables 70.V and 70.VI list the melt-penetration depth $\ell_m$ normalized, for comparison convenience with AFM measurements, to the HfO$_2$/SiO$_2$ layer interface for both types of medium and large defects, as well as $\ell_m$ dependence upon a range of conductivity anisotropies. The emphasis here is on weak anisotropies: for medium defects, no melt events are recorded, and even for large defects the melt penetration into SiO$_2$ is very shallow.
By raising the value for $H_{\text{gen}}$ and simulating fluence conditions above threshold, one may address the question of how high a temperature a given defect must reach to generate damaging melt-penetration depths comparable to experimentally observed ones. For small- and medium-sized metallic defects the corresponding melt-penetration depths $\ell_m$ and defect peak temperatures are listed in Tables 70.VII and 70.VIII as a function of increasing $H_{\text{gen}}$. From these tables it becomes immediately apparent that experimentally measurable melt penetration occurs only for very high defect temperatures. For either defect size a temperature of $3 \times 10^4 \, ^oK$ is required. Such temperatures are alarming inasmuch as the physical mechanisms so far ignored in these simulations start to play a role in the overall laser-damage model. They also point toward the inability of the current model to simulate laser damage by thermal-conductivity-dominated energy transfer alone.

Table 70.V: Melt-penetration depth $\ell_m$ (nm) values, large-defect case, as a function of parameter $\gamma$.

<table>
<thead>
<tr>
<th>Defect Type</th>
<th>$\gamma =$ 0.1</th>
<th>$\gamma =$ 0.2</th>
<th>$\gamma =$ 0.5</th>
<th>$\gamma =$ 1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>HfO$_2$</td>
<td>47</td>
<td>35</td>
<td>18</td>
<td>9</td>
</tr>
<tr>
<td>Metallic</td>
<td>49</td>
<td>38</td>
<td>24</td>
<td>14</td>
</tr>
</tbody>
</table>

$T_{\text{max}}$ (HfO$_2$) = 27,000 K; $T_{\text{max}}$ (met) = 30,000 K.
Two mechanisms that spring immediately to mind have the potential for significantly altering the kinetics of laser damage by providing sources for energy absorption from the laser field at a distance from the original defect: thermoionically emitted electrons and blackbody radiation in both the IR and, more importantly, the UV portion of its spectrum. Still, during the excitation pulse, when the thermal energy is mostly bottled up inside the defect and its temperature is highest, free carriers directly emitted into or ionized by UV photons within the surrounding dielectric layer stack provide starting electrons for “avalanche-type” or other energy-transfer processes at locations that, in effect, constitute an electronic ballooning of the defect. Table 70.IX emphasizes this aspect by listing the fraction of integrated blackbody radiation with photon energy above the HfO$_2$ bandgap as a function of defect temperature, emitted by a heated defect into its surrounding. From Table 70.IX we see that 10% of the emitted blackbody spectrum lies above 5.6 eV for temperatures as low as $1 \times 10^4$ °K. At the temperatures predicted by the current simulations this fraction increases to nearly 90%. The potential significance of such a UV ionization mechanism was pointed out in 1978 by Manenkov and his group. Based on this earlier work, the Grenoble Group evaluated the role of such preionization in single-layer films on melting and mechanical breaking of the film matrix.

Such a “larger-effective-defect” mechanism is also a plausible answer to the earlier-mentioned discrepancy between the calculated lateral-melt penetration range and the empirical AFM data. While part of this discrepancy can be assuaged by choosing a less-severe conductivity anisotropy, the lateral seeding of heating sources by ionizing radiation is an equally provocative concept whose merit must be tested in expanded simulations.

<table>
<thead>
<tr>
<th>Defect Type</th>
<th>$\gamma = 0.1$</th>
<th>$\gamma = 0.2$</th>
<th>$\gamma = 0.5$</th>
<th>$\gamma = 1.0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>HfO$_2$</td>
<td>13</td>
<td>5</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Metallic</td>
<td>14</td>
<td>6</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

$T_{\text{max}}$ (HfO$_2$) = 25,000 K; $T_{\text{max}}$ (met) = 17,000 K.

<table>
<thead>
<tr>
<th>$H_{\text{gen}}$ (W/m$^3$)</th>
<th>$T_{\text{max}}$ (°K)</th>
<th>$\ell_m$ (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2 \times 10^{20}$</td>
<td>8551</td>
<td>0</td>
</tr>
<tr>
<td>4</td>
<td>18760</td>
<td>1</td>
</tr>
<tr>
<td>5</td>
<td>22110</td>
<td>4</td>
</tr>
<tr>
<td>6</td>
<td>24750</td>
<td>6</td>
</tr>
<tr>
<td>7</td>
<td>31890</td>
<td>9</td>
</tr>
<tr>
<td>8</td>
<td>37750</td>
<td>12</td>
</tr>
<tr>
<td>10</td>
<td>42990</td>
<td>15</td>
</tr>
</tbody>
</table>
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Table 70.IX: Fraction of thermal radiation from the absorbing defect with photon energy exceeding HfO2 bandgap (5.6 eV).

<table>
<thead>
<tr>
<th>$T$ (°K)</th>
<th>$F_{ion}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10,000</td>
<td>10</td>
</tr>
<tr>
<td>20,000</td>
<td>57</td>
</tr>
<tr>
<td>30,000</td>
<td>80</td>
</tr>
<tr>
<td>40,000</td>
<td>89</td>
</tr>
</tbody>
</table>

Table 70.VIII: Melt-penetration depth $\ell_m$, as a function of heat-generation rate $H_{gen}$, medium-defect case.

<table>
<thead>
<tr>
<th>$H_{gen}$ (W/m$^3$)</th>
<th>$T_{max}$ (°K)</th>
<th>$\ell_m$ (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1 \times 10^{20}$</td>
<td>8652</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>16600</td>
<td>14</td>
</tr>
<tr>
<td>3</td>
<td>27070</td>
<td>23</td>
</tr>
<tr>
<td>4</td>
<td>36970</td>
<td>30</td>
</tr>
<tr>
<td>5</td>
<td>44880</td>
<td>35</td>
</tr>
</tbody>
</table>

Summary

In considering thermal conduction as the only energy transport mechanism, the current simulations show that relevant comparison with empirical damage morphology necessitates such high defect temperatures ($T > 30,000$°K) that other physical mechanisms start to attain dominance. These calculations point toward a mechanism in which the thermally trapped defect (thermally trapped on a nanosecond time scale) emits ionizing radiation into the surrounding film matrix. In response to such ionization, a volume larger than the defect itself becomes absorptive to the laser field and mediates direct energy transfer to the film at locations distant from the defect.

ACKNOWLEDGMENT

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Signatures of Target Performance and Mixing in Titanium-Doped Target Implosions on OMEGA

In recently published work we discussed the signatures of mixing\(^1\) and of target performance\(^2\) provided by incorporating a titanium-doped layer within the shell of imploding targets. We report here on the results of an experiment on OMEGA using such targets. We observe the predicted absorption features formed by the titanium layer: absorption lines due to \(1s-2p\) transitions in titanium ions of incomplete \(L\) shell, as well as \(K\)-edge absorption in cold titanium. We also observe oscillations due to extended x-ray absorption fine structure (EXAFS) above the Ti \(K\) edge. The observed spectra are simulated by a radiative-transport model that uses \(LILAC\) profiles and OPLIB opacity values. The observed core temperature and shell areal density are found to fall short of the one-dimensional predicted values. We attribute this shortfall to a lack of irradiation symmetry, which leads to hydrodynamic instability and mixing [distributed phase plates (DPP’s) were not used in this experiment, although the SSD modulator was activated]. The introduction of a sharp density jump at the interfaces of the titanium layer introduces a Rayleigh-Taylor (RT) unstable layer, which makes the target more unstable. Signatures of mixing include the emission of the He-\(\alpha\) line of Ti\(^{20}\) due to titanium migrating to the core, as well as the EXAFS spectrum indicating cold titanium close to peak compression. The spectral signatures due to the titanium layer are shown to provide very useful signatures of target performance.

A titanium layer was placed within a polymer-shell target, between a mandrel and an overcoat layer. The overcoat is much thicker than the laser-ablated layer to prevent emission of titanium lines from laser heating. Likewise, the titanium layer was sufficiently far from the inner-shell interface to ensure that the titanium lines are not emitted in the absence of mixing.\(^1\) The titanium layer is thus cold for the most part and should give rise to absorption lines.\(^3\) The measured area enclosed within the absorption lines yields the areal density of the titanium and, by implication, of the total compressed shell. The intensity distribution of the absorption lines yields the temperature of the cold titanium layer. Additionally, the intensity slope of the continuum at higher photon energies yields the core temperature. These parameters are deduced from the measured spectra and compared with simulation predictions. Highly performing targets require only a low percentage (~1\%) of titanium doping to give significant absorption;\(^2\) the need to use a pure-titanium layer in this experiment is an indication of lower compression.

The sharp density jump at the interfaces of the titanium layer becomes unstable during acceleration and deceleration; however, a thin layer cannot support unstable modes of long wavelength. A reduction factor multiplying the RT growth rate, due to the finite thickness of an unstable layer, has been derived by Landau and Lifshitz.\(^4\) One-dimensional code simulations of shot 8207 (see below) show that during the acceleration phase (when the shell and Ti layer are still thin) the reduction factor ranges from ~0.2 to ~0.5 for modes \(\ell = 10\) to \(\ell = 50\). Thus, the contribution of the titanium interface to the overall RT growth should be small.

In this article we concentrate on a single shot on the OMEGA laser\(^5\)—shot No. 8207. The target was a polymer shell of 882-\(\mu\)m inner diameter and 4.6-\(\mu\)m thickness, coated with a 0.3-\(\mu\)m layer of titanium, a 15-\(\mu\)m layer of polymer, and finally a 0.1-\(\mu\)m layer of aluminum as a shinethrough barrier.\(^6\) The fill gas was atmospheric air. The 19.9-kJ laser pulse had a 1-ns flat top (to within \(\pm\)5\%) with 150-ps rise and fall times. SSD\(^7\) was used in this experiment, but not DPP’s.\(^8\)

**Experimental Results**

Spectrally dispersed images were obtained with a Kirkpatrick-Baez x-ray microscope of resolution \(\leq 5\ \mu\)m, fitted with a dispersing grating.\(^9\) The images show a highly nonuniform core of \(\sim 60-\mu\text{m FWHM}\), indicating an unstable implosion. This is further indicated by the spectral results discussed below.

The x-ray spectrum in the range of \(\sim 4\) to \(9\) keV was recorded by a Ge(111) crystal spectrometer fitted with a 100-\(\mu\)-wide spatially resolving slit. The slit acts to discriminate core radiation from coronal emission. The calibrated x-ray spectrum obtained with a Ge(111) diffracting crystal is shown in Fig. 70.38. Ti absorption lines are seen around 4.6 keV as well.
as absorption above the Ti $K$ edge at 4.966 keV. These absorption features take place when the radiation emitted by the hot, compressed core is absorbed by the colder Ti layer within the shell. The calibration procedure is explained in more detail in Ref. 10. For the calibration of the Kodak DEF film we relied on the measurements and modeling of Henke et al.;\textsuperscript{11} for the calibration of the Ge(111) crystal we relied on the measurements of Burek and Yaakobi,\textsuperscript{12} which agree well with the Darwin-Prins model calculations of Henke et al.\textsuperscript{13} Figure 70.39 shows the measured and calculated crystal reflectivity. It should be noted that the crystal sensitivity is a weak function of energy in the range of interest (4 to 8 keV). In Fig. 70.40 we magnify the part of the spectrum showing various absorption features that are of particular interest in this experiment. As explained below, the lines around 4.6 keV are absorbed within a cool titanium layer ($T_e \sim 200$ to 500 eV), whereas radiation above the Ti $K$ edge at 4.966 keV is absorbed by much colder titanium. The EXAFS oscillations also indicate cold titanium. On the other hand, the Ti He-$\alpha$ line is emitted in a high-temperature region ($\sim 1$ keV).

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7038.png}
\caption{Calibrated, time-integrated x-ray spectrum obtained on shot 8207. Ti absorption lines are seen around 4.6 keV and the Ti $K$ edge at 4.966 keV. These absorptions take place when the radiation emitted by the hot, compressed core is absorbed by the colder Ti layer within the shell.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7039.png}
\caption{Measured\textsuperscript{12} and calculated\textsuperscript{13} integrated reflectivity of Ge(111) crystal.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure7040.png}
\caption{Part of the spectrum of Fig. 70.38, where absorption features appear. The lines around 4.6 keV are absorbed within a cool titanium layer ($T_e \sim 200$ to 500 eV), whereas radiation above the Ti $K$ edge at 4.966 keV is absorbed by much colder titanium. The EXAFS oscillations also indicate cold titanium. On the other hand, the Ti He-$\alpha$ line is emitted in a high-temperature region ($\sim 1$ keV).}
\end{figure}

\textbf{K-Edge Absorption}

The spectrum shows a drop in intensity at the $K$ edge of cold titanium at 4.966 keV. This indicates the existence of cold titanium around the time of peak compression, when the observed core emission of continuum radiation is significant. To estimate the temperature of the absorbing titanium we note that for each electron ionized from a titanium atom, the $K$ edge shifts to higher energies. A simple method for estimating the energy of these edges is discussed in Ref. 14. When the 12 $M$-shell electrons in Ti are removed, the edge shifts progressively from 4.966 keV up to about 5.2 keV; when the eight $L$-shell electrons are removed, the edge shifts progressively from $\sim 5.2$ to $\sim 6.2$ keV. The sharpness of the $K$-edge absorption indicates that no more than a few $M$-shell electrons are ionized, indicating a temperature lower than $\sim 10$ to 20 eV. The EXAFS spectrum discussed below indicates a still lower temperature.

The drop above the $K$ edge corresponds to an absorption by a cold titanium layer of an areal density of 1.3 mg/cm$^2$
This is 9.3 times higher than the original areal density of the titanium layer, 0.135 mg/cm$^2$. Using this value of areal density we can derive the spectrum emitted by the core before being attenuated by the cold titanium layer. This is simply given by $I(E) = I(E) \exp[-\rho R \Delta \tau(E)]$, where $I(E)$ is the observed spectrum and $\tau(E)$ is the absorption (or opacity) of cold titanium; the result is shown in Fig. 70.41. The continuum is indeed seen to fall along a smooth exponential curve whose slope indicates a core electron temperature of 0.94 keV. This could have also been deduced from the high-energy part of the continuum in Fig. 70.38, where the attenuation by the cold titanium is negligible.

$E$ is the absorbed photon energy and $E_K$ is the energy of the $K$ edge. The expression for $\chi(k)$ is

$$\chi(k) = \sum_j N_j F_j(k) \exp[-2\sigma^2 k^2 - 2R_j/\lambda(k)] \times \sin[2kR_j + \phi_j(k)]/kR_j^2,$$

where $N_j$ is the number of atoms surrounding the absorbing atom at a distance $R_j$. The backscattering amplitude $F_j(k)$ and phase shift factor $\phi_j(k)$ for titanium were taken from the detailed calculations by Teo and Lee, and the mean free path of the ejected electron in titanium, $\lambda(k)$, was taken from calculations of Blanche et al. The vibration amplitude $\sigma^2$ in the Debye-Waller factor and the interparticle distance $R_j$ will be adjustable parameters in fitting the experimental EXAFS spectrum to Eq. (1).

Figure 70.42 shows the calculated absorption $\mu(k)$ of the cold titanium layer in shot 8207 (shown above to have an areal density of 1.3 mg/cm$^2$), compared with an EXAFS spectrum of a 6-µm titanium foil absorber, obtained with synchrotron irradiation. The latter curve was multiplied by the ratio of thicknesses (2.9/6) in order to normalize it to the effective thickness (2.9 µm) of the absorbing layer in shot 8207. For both curves, the absorption was reduced by the much smaller absorption due to $L$-shell electrons, given by the absorption below the $K$ edge (thus the absorption curves equal zero below the edge). The oscillations in the present result have a slightly larger period (thus a smaller $R_j$) and larger amplitude than the solid-titanium oscillations; both are consistent with slightly

EXAFS Spectrum

Above the $K$ edge the spectrum shows oscillations due to EXAFS. EXAFS$^{15}$ is observed in solids (even amorphous ones) and is due to the interference of the photoelectron waves emitted from the absorbing ion and those reflected from the neighboring ions. It was previously observed in laser-heated flat targets$^{16}$ but not in imploded targets. The analysis of the EXAFS oscillations yields the interparticle distance and, hence, the density. EXAFS data for solid titanium have been published$^{17-19}$ and can be used for comparison.

The theory of EXAFS$^{15}$ yields an expression for $\chi(k) = \mu(k)/\mu_0(k) - 1$, where $\mu(k)$ is the absorption (or opacity) and $\mu_0(k)$ is the absorption of the isolated atom (i.e., without the EXAFS oscillations). The wave number of the ejected photoelectron $k$ is given by $h^2 k^2/2m = E - E_K$, where
higher than solid density in our case. The more gradual rise above the \( K \) edge in the curve obtained here is partly the result of finite spectral resolution and partly due to the ionization of a few \( M \)-shell electrons.

The isolated-atom absorption curve \( \mu_0(k) \) is given by a smooth average through the EXAFS oscillations; thus, the ratio \( \chi(k) = \mu(k)/\mu_0(k) - 1 \) retains the changes in the absorption due only to the EXAFS oscillations. Before fitting the experimental EXAFS spectrum to Eq. (1), a Fourier transformation is applied (yielding the radial charge distribution around the absorbing atom) to single out the contribution of only the first term in Eq. (1), that of the closest shell of atoms around the absorbing atom. Also, rather than transforming \( \chi(k) \), the quantity \( k^3 \chi(k) \) is normally chosen, putting more weight on the part of the spectrum away from the \( K \) edge (i.e., on higher \( k \) values). This choice is advantageous because Eq. (1) is precise at small \( k \) values; also, the effect of uncertainty in the value of \( E_k \) (due to valence-band energy structure) diminishes with increasing \( k \) values. The range of 2 to 10 Å\(^{-1} \) was used for the analysis of \( k^3 \chi(k) \). Below 2 Å\(^{-1} \) the curve is negligibly small; above \( k \sim 10 \) Å\(^{-1} \) the EXAFS spectrum is obscured by the rise of the Ti He-\( \beta \) line (albeit weak) at 5.582 keV and its dielectronic satellites.

The result of Fourier transforming the quantity \( k^3 \chi(k) \) (using a Hanning window\(^{22} \) to avoid spurious oscillations) is seen in Fig. 70.43. Only one peak, at 2.2 Å, has a significant contribution. This distance is not exactly equal to the interparticle distance because of the effect of the phase factor \( \phi_j(k) \) in Eq. (1). We next filter out this peak (extending from \(-1 \) to \(-3 \) Å) by multiplying the curve of Fig. 70.43 by an appropriate super-Gaussian curve, and finally apply an inverse Fourier transformation back to the \( k \) space. The resulting curve (Fig. 70.44) was fitted by the first term of Eq. (1), multiplied by \( k^3 \). As mentioned above, the functions \( F(k), \lambda(k), \) and \( \phi_j(k) \) for titanium have been calculated in great detail, and thus the two remaining parameters, \( \sigma^2 \) and \( R \), serve as adjustable parameters in the fit; no additional normalization was applied. Figure 70.44 shows the best fit, with \( \sigma^2 = 0.013 \) Å\(^2 \) and \( R = 2.6 \) Å. The parameter \( R \) depends primarily on the oscillation frequency of \( k^3 \chi(k) \), whereas \( \sigma^2 \) depends primarily on the amplitude decay rate at large \( k \) values (the amplitude rises at small \( k \) values because of the \( k^3 \) factor). Additionally, \( \sigma^2 \) determines the location and magnitude of the maximum in the \( k^3 \chi(k) \) curve. It should be emphasized that no amplitude normalization was applied to obtain this fit.

In solid titanium each atom is surrounded by two sub-shells of six atoms each, at distances of 2.889 Å and 2.940 Å. The unresolved peak in Fig. 70.43 thus corresponds to \( N = 12 \) backscattering atoms at an average distance of 2.6 Å [hence the choice \( N = 12 \) in Eq. (1)]. This indicates a titanium layer of density \( \sim 1.4 \) higher than that of solid titanium, i.e., a density of 6.4 g/cm\(^3 \). The Debye-Waller parameter \( \sigma \) (the amplitude of ion thermal oscillations) is proportional to \( T^{1/2} \). By comparison with room-temperature EXAFS spectra of titanium, the spectrum of Fig. 70.44 corresponds to an ion temperature below \(-1 \) eV. The values of density and temperature deduced here from the EXAFS spectrum are similar to those found with
an EXAFS measurement of laser-compressed foils. However, the ion temperature deduced here is lower than the electron temperature estimated above ($T_e < 10$ to $20$ eV) from the sharpness of the $K$-edge absorption.

Absorption Lines

The absorption lines seen in Fig. 70.40 indicate that part of the titanium shell is ionized, in addition to the cold part giving rise to the $K$-edge and EXAFS absorptions. The application of absorption lines to determine the properties of the compressed shell was discussed in detail in Ref. 1. We show in Fig. 70.45 an expanded view of the absorption-line manifold obtained on shot 8207, compared with opacity calculations for $T = 300$ eV and $\rho = 6.4$ g/cm$^3$. The calculations were taken from the LTE opacity library OPLIB, which was also used in the simulations described in the next section. The validity of assuming LTE populations in the calculation of absorption lines has been discussed in Ref. 1. The absorption lines around 4.6 keV correspond to transitions of the type $1s^22p^2$ in titanium ions of an incomplete $L$ shell: $\text{Ti}^{+13}$ to $\text{Ti}^{+20}$, formed when core-emitted continuum traverses the cold titanium layer. The designation $\text{Li}$ in Fig. 70.45 stands for lithium-like titanium ion, and likewise for the other designations. Each peak contains several lines that are unresolved mostly due to broadening due to the finite source size. For example, the peak marked C (carbon-like) consists of 35 transitions of the type $1s^22s^22p^2-1s^22p^3$. The intensity distribution of the absorption peaks depends mostly on the temperature but also on the density. For example, the cases where the dominant peaks are the C-like or the N-like peaks (as in shot 8207) correspond to a temperature that changes from ~200 to ~500 eV for an assumed density in the range of 1 to 50 g/cm$^3$. Thus, with no knowledge of the density, a comparison as in Fig. 70.45 can be used to obtain only a rough estimate of the temperature in the cold shell. The energies calculated by OPLIB are approximate, and Fig. 70.45 shows them to be slightly different than the measured values.

In addition to absorption lines, Fig. 70.45 shows the emission of the He-$\alpha$ line of $\text{Ti}^{+20}$. The emission of He-like lines from a doped layer that is sufficiently removed from the interface was shown to be a signature of mixing. Indeed, code simulations described in the next section show that these lines should not have been seen in the spectrum, in the absence of mixing.

Next we deduce the shell areal density from the absorption lines, using the relation

$$\int \ln[I_0(E)/I(E)]dE = \rho \Delta r \int k(E)dE.$$  \hspace{1cm} (2)

The left-hand term is an integral over the measured absorption-line manifold [if film density is proportional to $\ln(I)$, this term equals the area enclosed within the absorption lines in a film-density plot]. Although the opacity integral depends on the temperature and density of the absorbing region, it has been shown that using the observed intensity distribution of the absorption peaks enables us to deduce the areal density without having to know these parameters. We calculate the opacity integral $\int k(E)dE$ for titanium, using the OPLIB opacity library, for a wide range of temperatures and densities. When the results are grouped by the peak of highest opacity, the integral values fall within relatively narrow ranges, which can be understood as follows: Ionization increases with increasing

![Figure 70.45](image_url)

Comparison between the measured Ti absorption lines from shot 8207 and the opacity calculated by OPLIB. The OPLIB calculation is for $T = 300$ eV and $\rho = 6.4$ g/cm$^3$. The designation $\text{Li}$ stands for $1s^22p$ transitions in Li-like Ti, and likewise for the other designations.
temperature but decreases with increasing density (because the three-body recombination rises faster with density than other, two-body processes). Thus, a given ionization level is obtained for pairs of \((T, \rho)\) values where both increase simultaneously. Since opacity increases with density but decreases with temperature, the integrated opacity for such pairs tends to be reasonably constant. We show in Fig. 70.46 the calculated opacity integral, arranged according to the strongest opacity peak (marked Li for cases where the lithium-like peak is the strongest, etc.). Thus, simply knowing the strongest absorption peak narrows down the uncertainty in the integrated opacity and, hence, in the deduced areal density. For example, for cases where the C-like peak is the strongest, the uncertainty in the integrated opacity is \(\pm 25\%\). Applying Fig. 70.46 and Eq. (2) to the spectrum of shot 8207, we find \(\Delta \rho r \sim 0.4 \text{ mg/cm}^2\) for the titanium layer with a temperature in the range of ~200 to 500 eV. Adding the areal density found above for the cold titanium \(1.3 \text{ mg/cm}^2\), we find a total \(\Delta \rho r\) for the titanium layer of \(1.7 \text{ mg/cm}^2\). In adding the areal densities we have assumed that the line- and \(K\)-edge absorptions occur at the same time, signifying a temperature gradient within the titanium layer. This is indeed indicated by Fig. 70.40. Suppose the two absorptions take place at two different times: the \(K\) edge is absorbed at time \(t_1\) and the lines are absorbed at a time \(t_2\). The observed fluence above the \(K\) edge \((1.2 \times 10^{16} \text{ keV/keV})\) consists then of three parts: (a) the fluence that was emitted at \(t_1\) but survived the \(K\)-edge absorption, (b) the fluence emitted at \(t_2\), and (c) the fluence emitted at other times. Thus, the fluence at \(t_2\) must be smaller than the observed fluence above the \(K\) edge. However, this level of fluence is much smaller than the depth of the absorption lines \((\sim 4 \times 10^{16} \text{ keV/keV})\), indicating insufficient fluence to absorb the lines in those times.

Using the measured \(\Delta \rho r\) of the titanium layer we can estimate the \(\Delta \rho r\) of the entire compressed shell. Figure 70.47 shows the ratio \(Q = (\Delta \rho r)_{\text{total}} / (\Delta \rho r)_{\text{Ti}}\) calculated by the one-dimensional hydrodynamic code \textsc{Lilac} for shot 8207 as a function of the compression ratio (defined as \(r_0/r\), where \(r\) is the radius of the gas-shell interface and \(r_0\) is its initial value). Also shown is the result of a simple geometrical model where the unablated part of the shell is assumed to be incompressible as it implodes inward. Since charge-collector measurements (and simulations) indicate that an overcoat thickness of \(\sim 9 \mu\text{m}\) is ablated, the model uses the inner \(10.9 \mu\text{m}\) as the unablated part of the shell. Thus, a lower bound \(Q \sim 10\) can be used, giving \(\Delta \rho r > 17 \text{ mg/cm}^2\) for the compressed shell.

It should be pointed out that the use of time-integrated spectra yields an underestimate of the areal density because emission during times when absorption is insignificant diminishes the absorption contrast (typically by a factor of \(\sim 2\)).

**Comparison with Simulations**

In this section we compare the observed spectrum with that predicted by \textsc{Lilac}. The Ti spectral signatures are shown to reflect the reduced target performance that was a consequence of the poor irradiation uniformity in this experiment.

![Figure 70.46](image)

Area under the opacity-spectrum peaks of titanium (corresponding to the absorption-line manifold around 4.6 keV). For temperatures in the range of 300 to 1000 eV and densities in the range of 1 to 50 g/cm³, the points are grouped according to the strongest absorption peak in the opacity spectrum (\(\text{Li}\) stands for cases where the lithium-like peak is the strongest, and likewise for the other designations).

![Figure 70.47](image)

The ratio of \(\Delta \rho r\) for the total shell and for the titanium layer. The model assumes that the unablated shell implodes incompressibly. The compression ratio is defined as \(r_0/r\), where \(r\) is the radius of the gas-shell interface and \(r_0\) is its initial value.

**Figure 70.47**

The ratio of \(\Delta \rho r\) for the total shell and for the titanium layer. The model assumes that the unablated shell implodes incompressibly. The compression ratio is defined as \(r_0/r\), where \(r\) is the radius of the gas-shell interface and \(r_0\) is its initial value.
The simulated spectra were computed by applying a radiation-transport model\textsuperscript{1} to \textit{LILAC}-generated profiles, using the OPLIB opacity library. As discussed elsewhere,\textsuperscript{1,2} using the LTE opacity library is adequate for simulating the continuum radiation and the absorption lines. However, this would not be true for simulating the emission of helium-like and hydrogen-like titanium lines.

Figure 70.48 shows the comparison for the higher-energy part of the spectrum, and Fig. 70.49 the lower-energy part, where the absorption features appear. In both cases the simulated spectra are integrated in time up to the time marked in Figs. 70.48 and 70.49. The integration up to 2 ns is essentially an integration over the whole implosion. The simulated curves show some flattening below \( \sim 7 \) keV due to shell attenuation,\textsuperscript{25,9} and only higher-energy radiation is unattenuated and can be used to determine the core temperature. However, the experimental curve does not show this flattening, indicating a less-compressed shell. It also shows a cooler core than predicted: \( T = 0.94 \) as compared with \( T = 1.8 \) keV. The maximum temperature in the simulation \( (T \sim 3 \) keV\) was higher than that indicated by the time-integrated continuum slope \((T = 1.8 \) keV\), and thus it can be expected that the peak temperature in this experiment is \( \approx 1 \) keV. The lower tempera-

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure70_48.png}
\caption{Comparison of the measured and simulated x-ray continuum spectra for shot 8207. The simulated curves are integrated up to the marked times. The slopes yield the core electron temperature.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure70_49.png}
\caption{Comparison of measured and simulated x-ray spectra for shot 8207, in the region showing absorption features. The simulated curves are integrated up to the marked times.}
\end{figure}
ture and compression result in a much lower core-radiation fluence than predicted. Figure 70.48 shows that the implosion in this experiment falls short of the 1-D code predictions; in particular, the target fails to undergo the final compression stage that is predicted to occur between ~1.86 ns and peak compression at ~1.9 ns.

Similar conclusions can be drawn from the comparison in Fig. 70.49. The simulated time-integrated spectrum (<2 ns) shows much deeper absorption lines than observed, indicating a higher areal density, and little K-edge absorption, indicating a higher shell temperature. In fact, the saturated absorption of the simulated absorption lines shows that almost all radiation emitted after ~1.84 ns at the wavelengths of these lines is absorbed. As time progresses, the simulated spectra show a gradual shift from K-edge absorption to line absorption, indicating heating of the titanium layer by the core. Also, the absorption-line manifold is seen to shift toward higher ionizations, again indicating an increase in shell temperature. By contrast, the experimental curve shows (a) a lower total absorption, indicating a lower areal density [see Eq. (2)], and (b) prominence of K-edge absorption over line absorption, indicating a cooler shell. As in Fig. 70.48, the results show that the implosion is effectively aborted after ~1.86 ns. At intermediate times (~1.84 to 1.86 ns) K-edge and line absorptions occur simultaneously, which was shown above to be the case in the experiment.

We also note absorption features above ~5 keV in the simulated spectra but not in the measured spectrum. These are K-edge absorption in ionized Ti, as well as transitions of the type 1s–3l (K-shell to M-shell transitions) in various titanium ions.

The measured $\rho \Delta r$ of the titanium layer was found above to be ~1.7 mg/cm$^2$. The same $\rho \Delta r$ value in the simulation occurs at 1.7 ns, consistent with the conclusion of incomplete compression suggested above. At 1.7 ns the predicted titanium density is 11 g/cm$^3$, compared with the value 6.4 g/cm$^3$ deduced from the EXAFS spectrum. The predicted electron temperature is ~50 eV, compared with the estimate $T < 10$ to 20 eV from the sharpness of the K-edge absorption. The simulated spectra also predict no emission of helium-like Ti lines (even though LTE opacity modeling tends to overestimate their intensity).

The appearance of the He-\(\alpha\) line in the experiment (see Fig. 70.45) is clear evidence of shell-core mixing,\(^1\) which transports titanium into high-temperature regions. Titanium can be driven out to the ablation region (during acceleration) or into the compressed core (during deceleration). To determine which is the case in this experiment, we examine the spatial profile of the He-\(\alpha\) line, as measured by the crystal spectrometer. Figure 70.50 shows the profiles (in the target plane) at the wavelength of the He-\(\alpha\) line, as well as at a nearby wavelength; the net He-\(\alpha\) emission is given by their difference. The sharpness of the core emission profile indicates a smaller core than the slit width (100 $\mu$m), consistent with the 60-$\mu$m width measured by the x-ray microscope. Figure 70.50 clearly shows that most of the He-\(\alpha\) emission comes from the core, indicating mixing during the deceleration phase. The peak core temperature ($\approx 1$ keV) is sufficiently high to excite the He-\(\alpha\) line. The observed intensity of the He-\(\alpha\) line can be used to obtain a rough estimate of the amount of titanium reaching the core due to mixing. To that end, we repeat the simulations of Fig. 70.49 while assuming that a small fraction of the titanium mass is uniformly spread throughout the shell layers lying inward of the original titanium layer. Figure 70.51 shows the result for the case of mixing 3% of the total titanium mass into the core. The He-\(\alpha\) line (as well as its adjacent satellite line) now appears in the calculated spectrum. A comparison is made between the experimental spectrum and the simulated spectrum integrated up to 1.86 ns, as suggested by Figs. 70.48 and 70.49. In calculating the spectrum of Fig. 70.51, a correction was made to account for the LTE calculations’ overestimate of the intensity of the emission lines. A steady-state, non-LTE model was used to calculate the relative populations of the lithium-like, helium-like, and hydrogen-like Ti species, from which the intensity of the major

\(\begin{figure*}[h]
\centering
\includegraphics[width=\textwidth]{figure70.50.png}
\caption{Spatial profile of emission at the wavelength of the Ti He-\(\alpha\) line (4.75 keV), and at a nearby wavelength. The difference (i.e., the net He-\(\alpha\) emission) indicates mixing of titanium into the compressed core.}
\end{figure*}
Signatures of Target Performance and Mixing in Titanium-Doped Target Implosions on OMEGA

The reduced target performance evidenced in Figs. 70.48 and 70.49 as well as the presence of mixing is the result of inadequate irradiation uniformity when not using phase plates to smooth the laser irradiation, as well as the result of the density jump at the titanium layer interfaces. The titanium spectral signatures studied in this work should prove very useful in tracking the improved target performance with improved laser uniformity.

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REFERENCES

Dehasing Time of an Electron Accelerated by a Laser Pulse

In a recent paper\(^1\) we described the motion of electrons in the electromagnetic field of a circularly polarized laser pulse propagating through a plasma. Electrons that are in front of the pulse initially can be accelerated to high energies and extracted easily. Although this direct acceleration scheme is less than ideal because the pulse can generate a parasitic wake, its simplicity is noteworthy. The wake fields produced by short pulses have been observed recently,\(^2,3\) and future experiments will study the interaction of electron bunches with these wake fields. One would only need to change the timing of an electron bunch in these experiments to test the scientific feasibility of direct acceleration. In this article we study the dehasing time of an electron accelerated by a pulse of infinite width to determine the propagation time and plasma length required to observe direct acceleration.

In the following sections, the trajectory of a charged particle is determined analytically for a representative pulse profile; the dehasing time of an accelerated particle is determined; its dependence on the speed, length, and intensity of the pulse along with the injection energy of the particle is studied in detail; and finally, the main results are summarized.

**Particle Motion in a Planar Field**

The motion of a particle, of charge \(q\) and mass \(m\), in an electromagnetic field is governed by the equation\(^4\)

\[
d_{\tau} \left( u_{\mu} + a_{\mu} \right) = u^\nu \partial_{\mu} a_{\nu},
\]

where \(u^{\mu}\) is the four-velocity of the particle divided by \(c\), \(\tau\) is the proper time of the particle multiplied by \(c\), and \(a^{\mu}\) is the four-potential of the field multiplied by \(q/mc^2\). The metric four-tensor \(g^{\mu
u} = \text{diag}(1,-1,-1,-1)\).

For a planar field \(a^{\mu}\) has \(y\) and \(z\) components that are functions of \(t\) and \(x\). It is convenient to denote the transverse (two-vector) component of \(a^{\mu}\) by \(a\), the transverse component of \(u^{\mu}\) by \(v\), and the longitudinal components of \(u^{\mu}\) by \(\gamma\) and \(u\).

In this notation, the transverse component of Eq. (1) is

\[
d_{\tau} (v + a) = 0.
\]

For a particle that is in front of the pulse initially, and is not moving transversely,

\[
v = -a.
\]

By using Eq. (3), one can rewrite the longitudinal components of Eq. (1) as

\[
d_{\tau} \gamma = \partial_{x} \left( v^2 / 2 \right), \quad d_{\tau} u = -\partial_{x} \left( v^2 / 2 \right).
\]

For a circularly polarized field

\[
a^{\mu} = (0, 0, a \cos \phi, a \sin \phi) / \sqrt{2}.
\]

We assume that the phase \(\phi = t - sx\), where \(s < 1\) is the inverse phase speed of the pulse, and the amplitude \(a\) is a function of \(\psi = t - rx\), where \(r > 1\) is the inverse group speed of the pulse. Equations (3)–(5) were solved in Ref. 1 for a particle that is at rest initially. The solution of these equations for a particle that is moving initially is similar. Since the ponderomotive potential \(v^2 / 2\) is independent of \(\phi\), it follows from Eqs. (4) that

\[
d_{\tau} (r \gamma - u) = 0.
\]

By combining Eq. (6) with the definition of \(\gamma\), one can show that

\[
\gamma = \frac{\left( r \gamma_0 - u_0 \right) \mp r \omega}{r^2 - 1},
\]

\[
u = \frac{\left( r \gamma_0 - u_0 \right) \mp r \omega}{r^2 - 1},
\]

where

\[
\gamma = \frac{(r \gamma_0 - u_0) \mp r \omega}{r^2 - 1},
\]

\[
u = \frac{(r \gamma_0 - u_0) \mp r \omega}{r^2 - 1},
\]

\[
\gamma = \frac{(r \gamma_0 - u_0) \mp r \omega}{r^2 - 1},
\]
ω = \left[ (γ_0 - u_0)^2 - (r^2 - 1) \right]^{1/2}. \quad (8)

In Eqs. (7) the − sign applies to the case in which γ > ru, which corresponds to a particle that is moving more slowly than the pulse, and the + sign applies to the case in which γ < ru, which corresponds to a particle that is moving more quickly than the pulse. By using the fact that 1 = γ^2_0 - u_0^2, one can rewrite Eq. (8) in the convenient form

ω = \left[ (γ_0 - u_0)^2 - (r^2 - 1)v^2 \right]^{1/2}. \quad (9)

For the case in which γ_0 = 1 and u_0 = 0, Eqs. (7) and (9) reduce to the corresponding equations of Ref. 1. A particle that is moving more slowly than the pulse initially will be repelled by the pulse if ω = 0. For this to happen the pulse intensity must equal the repelling intensity

\[ a^2 = 2(γ_0 - u_0)^2 / (r^2 - 1), \quad (10) \]

in which case the gain in particle energy

\[ δγ = 2(γ_0 - u_0) / (r^2 - 1). \quad (11) \]

For completeness, a covariant analysis of particle motion in a circularly polarized field is given in Appendix A, and a brief description of particle motion in an elliptically polarized field is given in Appendix B.

Equations (3), (7), and (9) define \( dμ \) as a function of \( ψ \). By combining the equation \( d_ψ = γ - ru \) with Eqs. (7), one can show that

\[ dτ/dψ = ±1/ω(ψ), \quad (12) \]

where the + sign applies to the case in which γ < ru and the − sign applies to the case in which γ > ru. If the solution of Eq. (12) can be inverted, \( μ(γ) \) can be expressed as an explicit function of τ.

To illustrate the particle motion we consider the simple profile

\[ a(ψ) = e \sin(πψ/2lr), \quad (13) \]

where \( e^2 \) is the peak intensity of the pulse and \( l \) is its full-width at half-maximum. For this profile

\[ ω(ψ) = (γ_0 - ru) \left[ 1 - m^2 \sin^2(πψ/2lr) \right]^{1/2}, \quad (14) \]

where

\[ m^2 = (r^2 - 1)e^2 / 2(γ_0 - ru)^2 \quad (15) \]

is the ratio of the pulse intensity to the repelling intensity.

When \( m < 1 \), the pulse overtakes the particle completely. In this case \( ψ \) varies between 0 and 2lr, and the solution of Eq. (12) is

\[ τ(ψ) = \frac{2lr/π (γ_0 - ru)}{F(πψ/2lr, m)}, \quad (16) \]

where \( F \) denotes the incomplete elliptic integral of the first kind, of modulus \( m \). It follows from Eqs. (7) and (9) that

\[ t(ψ) = \frac{r(γ_0 - u_0) τ(ψ) - ψ}{r^2 - 1}, \quad (17) \]

\[ x(ψ) = \frac{r(γ_0 - u_0) τ(ψ) - rψ}{r^2 - 1}. \]

The particle motion is illustrated in Fig. 70.52 for the case in which \( γ_p = 30, γ_0 = 7, \) and \( e^2 = 7 \) [The Lorentz factor \( γ_p \) is defined in the first of Eqs. (22)]. In Fig. 70.52(a) the phase, normalized to \( lr \), is plotted as a function of time, normalized to \( γ_0 \). As the particle is accelerated by the front of the pulse, the rate of phase slippage decreases. However, since the peak intensity of the pulse is lower than the repelling intensity, the particle speed never equals the pulse speed and the pulse overtakes the particle. As the particle is decelerated by the back of the pulse, the rate of phase slippage increases. It is evident from Fig. 70.52(a) that the deceleration time equals the acceleration time. In Fig. 70.52(b) the longitudinal momentum is plotted as a function of the normalized time. Although the particle speed never exceeds the pulse speed, the energy...
associated with the transverse particle motion allows the particle momentum to exceed the pulse momentum. Because the longitudinal momentum is a symmetric function of time, the deceleration distance equals the acceleration distance.

When \( m > 1 \), the particle is repelled by the pulse. In this case \( \psi \) increases from 0 to \( (2lr/\pi)\sin^{-1}(1/m) \) as the particle ascends the ponderomotive potential and decreases from \( (2lr/\pi)\sin^{-1}(1/m) \) to 0 as the particle descends the ponderomotive potential. The solution of Eq. (12) is

\[
\tau(\psi) = \left[\frac{2lr}{\pi m(\gamma_0 - ru_0)}\right]F(\theta, 1/m), \\
\left[\frac{2lr}{\pi m(\gamma_0 - ru_0)}\right][2K(1/m) - F(\theta, 1/m)],
\]

where

\[
\theta(\psi) = \sin^{-1}\left[m \sin\left(\frac{\pi \psi}{2lr}\right)\right]
\]

and \( K \) denotes the complete elliptic integral of the first kind, of modulus \( m \). The first form of Eq. (18) applies to the ascent and the second form applies to the descent. Equations (17) apply to both the ascent and descent, provided that \( \tau \) is defined by Eqs. (18) and (19). The particle motion is illustrated in Fig. 70.53 for the case in which \( \gamma_P = 30 \), \( \gamma_0 = 7 \), and \( e^2 = 10 \). In Fig. 70.53(a) the normalized phase is plotted as a function of the normalized time. Initially, the pulse overtakes the particle and the rate of phase slippage is positive. Since the peak intensity of the pulse is higher than the critical intensity, the particle is accelerated until its speed equals the pulse speed and the rate of phase slippage is zero. Subsequently, the particle overtakes the pulse and the rate of phase slippage is negative. The descent time is longer than the ascent time because the time dilation associated with a particle moving faster than the pulse is larger than that associated with a particle moving slower than the pulse. In Fig. 70.53(b) the longitudinal momentum is plotted as a function of the normalized time.
ized time. Since the particle does not reach the peak of the pulse, the $x$ component of the ponderomotive force is always positive and the longitudinal momentum of the particle increases monotonically. Because the longitudinal momentum is an asymmetric function of time, the descent distance is longer than the ascent distance.

**Dephasing Time of an Accelerated Particle**

The previous analysis shows how an intense pulse repels a charged particle that is in front of the pulse. The relation between the pulse intensity, the particle injection energy, and the gain in particle energy was studied in Ref. 1. In this section the time required for the pulse to catch and repel the particle, and, subsequently, for the particle to outrun the pulse, is studied. This time is referred to as the dephasing time and is denoted by $T$. The distance traveled by the particle during the dephasing time is referred to as the dephasing distance and is denoted by $X$. It follows from Eqs. (17) and (18) that

$$T = \frac{4l^2(r\gamma_0 - u_0)K(1/m)}{\pi m(r^2 - 1)(\gamma_0 - ru_0)} \tag{20}$$

and $X = Ti/r$. For future reference, notice that $K(1/m) \to \log [4/(m^2 - 1)^{1/2}]$ as $m \to 1$ and $K(1/m) \to \pi 2$ as $m \to \infty$. \(^5\)

Formula (20) for the dephasing time exhibits a complicated dependence on the pulse intensity and speed and the initial particle momentum. One can gain insight into the underlying physics by performing a pulse-frame analysis of the acceleration process. In the notation of Ref. 1, ' denotes a pulse-frame quantity, the subscript $A$ denotes the initial position of the particle, and $B$ denotes the position at which the particle is repelled.

The pulse-frame energy and momentum of the particle are related to the laboratory-frame energy and momentum by the equations

$$\gamma' = \gamma_p \gamma - u_p u, \quad u' = \gamma_p u - u_p \gamma, \tag{21}$$

where

$$\gamma_p = r^{1/2}(r^2 - 1)^{1/2}, \quad u_p = 1/(r^2 - 1)^{1/2}. \tag{22}$$

In these equations $\gamma_p$ is the Lorentz factor associated with the pulse speed $1/r$ and $u_p = (\gamma_p^2 - 1)^{1/2}$. If one uses the linear group speed of the pulse to estimate the Lorentz factor, $\gamma_p = \omega_0 / \omega_e$, where $\omega_0$ is the carrier frequency of the pulse and $\omega_e$ is the electron-plasma frequency. \(^6\)

In the pulse frame $v^2$ is time-independent. It follows from the first of Eqs. (4) that $\gamma'$ is constant and, hence, that $(u')^2 + v^2 = (u'_A)^2$. Since $dx'/dt' = u'/\gamma_A'$, it follows that

$$T' = 2\gamma_A' \int_{x_0}^{x_A} \frac{dx'}{[(u'_A)^2 - v^2(x')]^{1/2}}. \tag{23}$$

In Eq. (23) the factor of 2 arises because the pulse-frame descent time equals the pulse-frame ascent time. The factor of $\gamma_A'$ arises because of the difference between proper time and pulse-frame time. Provided one ignores the distinction between momentum and velocity, the integral in Eq. (23) represents the ascent time of a nonrelativistic particle in the potential well $v^2(x')/2$. In the pulse frame $a = e\sin(-\pi x/2l')$, where $l' = \gamma_p l$. For this profile

$$T' = 2\gamma_A'(2l'/\pi)\left[\sqrt{2}/e\right]K\left(\sqrt{2}u'_A/e\right). \tag{24}$$

The factor of $2l'/\pi$ arises because the ponderomotive force associated with the pulse is inversely proportional to the pulse length. Although Eq. (24) is complicated, the origin of each factor is well understood.

In the pulse frame the particle begins and ends its interaction with the pulse at point A. Since $X' = 0$, it follows that

$$T = \gamma_p T', \quad X = u_p T'. \tag{25}$$

Notice that $X = Ti/r$, as stated after Eq. (20). It follows from Eqs. (21) and (22) that $r(r\gamma_0 - u_0)/[r^2 - 1] = \gamma_p \gamma_A'$ and $4l/r\pi m(\gamma_0 - ru_0) = 2(2l'/\pi)\left[\sqrt{2}/e\right]$. Thus, Eq. (24) and the first of Eqs. (25) agree with Eq. (20).

It is convenient to define the normalized dephasing time

$$\bar{T} = \left(4\sqrt{2} \gamma_A'/\pi e\right)K\left(\sqrt{2} u'_A/e\right), \tag{26}$$

which is the dephasing time divided by $\gamma_p^2 l$. The factor of $l$ was due to the inverse dependence of the ponderomotive force on the pulse length. One factor of $\gamma_p$ was due to the Lorentz
transformation of the pulse length from the laboratory frame to
the pulse frame; the other factor was due to the Lorentz
transformation of the dephasing time from the pulse frame to
the laboratory frame. These factors do not depend on the
physical origin or shape of the potential well in which the
particle moves. Thus, it was inevitable that they should be the
same as the factors that control the dephasing time of an
electron in the laser beat-wave accelerator\(^7\) or the laser wake-
field accelerator.\(^7,8\) For completeness, a brief analysis of the
particle motion and dephasing time associated with these
indirect acceleration schemes is given in Appendix C.

Just as a pulse-frame analysis of the acceleration process
fosters insight into the dephasing time, so also does it foster
insight into the energy gain. In the pulse frame the particle
energy is constant, and the final particle momentum has the
same magnitude as the initial particle momentum and the
opposite sign: \(\delta \gamma' = 0\) and \(\delta u' = 2|\mu_A'|\). It follows from these
results and Eqs. (21) that

\[
\delta \gamma = 2u_P|\mu_A'|, \tag{27}
\]
in agreement with Eq. (11).

The normalized dephasing time is plotted as a function of
pulse intensity in Fig. 70.54 for the case in which \(\gamma_P = 30\). In
Fig. 70.54(a) the injection energy \(\gamma_A = 7\). The solid line denotes
the exact dephasing time [Eq. (26)], and the broken line
denotes the approximate dephasing time \(2\sqrt{2} \gamma_A'/e\). For the
chosen values of \(\gamma_P\) and \(\gamma_A\) the approximate dephasing time is
6.4/e. When the pulse intensity is close to the repelling inten-
sity, the particle lingers near the peak of the pulse and the
dephasing time is long. As the pulse intensity increases, point
B moves toward the front of the pulse and the dephasing time
decreases. In the high-intensity regime this decrease is gradual.
Since the pulse energy located behind point B is wasted, there
is little to be gained by using pulse intensities that exceed the
critical intensity by more than a factor of 2. Since the injection
energy is constant, so also is the energy gain [Eq. (27)]. In
Fig. 70.54(b) the injection energy

\[
\gamma_A = \gamma_P \mu - \left[\left(\gamma_P - 1\right)\left(\mu^2 - 1\right)\right]^{1/2}, \tag{28}
\]
where \(\mu = \left(1 + e^2/4\right)^{1/2}\) is a measure of the pulse intensity.
This choice of injection energy ensures that the repelling
intensity is one-half of the pulse intensity. For this injection
energy \(u_A' = -e/2, \gamma_A' = \left(1 + e^2/4\right)^{1/2}\), and the saturation time
is \(1.7(1 + 4/e^2)^{1/2}\), independent of \(\gamma_P\). In the low-intensity
regime the dephasing time is long because the pondero-
motive force is weak. In the high-intensity regime the dephasing
time is almost independent of pulse intensity because the
increase in ponderomotive force that accompanies an increase
in pulse intensity is offset by the corresponding decrease in
injection energy. It follows from Eq. (27) and the preceding
discussion that the energy gain equals \(u_P e\). As the pulse
intensity increases, the energy gain increases and the required
injection energy decreases.

The normalized dephasing time is plotted as a function of
injection energy in Fig. 70.55 for the case in which \(\gamma_P = 30\). In
Fig. 70.55(a) the pulse intensity \(e^2 = 10\). The solid line denotes
the exact dephasing time [Eq. (26)], and the broken line
denotes the approximate dephasing time \(2\sqrt{2} \gamma_A'/e\). For the
chosen values of \(\gamma_P\) and \(e\) the approximate dephasing time is

\[\text{Figure 70.54}\]

Normalized dephasing time [Eq. (26)] plotted as a function of pulse intensity
for the case in which \(\gamma_P = 30\). (a) The particle injection energy \(\gamma_A = 7\).
(b) The particle injection energy [Eq. (28)] ensures that the repelling
intensity [Eq. (10)] is one-half of the pulse intensity.
When the injection energy is close to the repelling energy, the particle lingers near the peak of the pulse and the dephasing time is long. As the injection energy increases, point B moves toward the front of the pulse and the dephasing time decreases. In the high-energy regime the dephasing time is almost independent of the injection energy because \( \gamma' \approx \gamma \). The energy gain decreases as the injection energy increases. In Fig. 70.55(b) the pulse intensity \( e^2 \) is twice the repelling intensity [Eq. (10)]. In the low-energy regime the dephasing time is almost independent of the injection energy because \( \gamma'_A = \gamma_p \) and \( u'_A = -\gamma_p \). The ratio \( \gamma'_A/u'_A \) is almost independent of \( \gamma_p \). In the high-energy regime the dephasing time is long and the energy gain is small because \( \gamma'_A = 1 \) and \( |u'_A| \ll 1 \).

**Summary**

The motion of an electron in the electromagnetic field associated with a circularly polarized laser pulse of infinite width was studied analytically. When the pulse intensity is lower than the repelling intensity [Eq. (10)], the pulse overtakes the electron completely. When the pulse intensity is higher than the repelling intensity, the electron is repelled by the pulse and eventually outruns it. The time taken for the electron to outrun the pulse is called the dephasing time and is the product of two terms. The first term is \( \gamma_p l \), where \( \gamma_p \) is the Lorentz factor associated with the pulse speed and \( l \) is the pulse length. The second term [Eq. (26)] depends on the pulse intensity, the pulse shape, and the electron injection energy. As a rough guideline, the second term is of order unity unless the pulse intensity is close to the repelling intensity. For a pulse of finite width, an electron that is not close to the pulse axis initially will be expelled from the pulse by the radial component of the ponderomotive force. Further work is needed to quantify this snowplow effect.

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**Appendix A: Covariant Analysis of the Particle Motion in a Planar Field**

The resolution of Eq. (1) into longitudinal and transverse components is facilitated by the introduction of the four-vector \( k^\mu \), which is defined by the equation \( \psi = k^\nu x_\nu \), and the four-vector \( l^\nu \), which is defined by the equations \( l^\nu l_\nu = -k^\nu k_\nu \), \( l^\nu k_\nu = 0 \), and \( l^\nu a_\nu = 0 \), where \( a^\mu \) is the transverse four-potential of a planar field of arbitrary polarization. In the laboratory frame \( k^\mu = (1,r,0,0) \) and \( l^\mu = (r,1,0,0) \). By using these four-vectors, one can write

\[
x_\mu = y_\mu + \psi k_\mu/k^\nu k_\nu + \theta l_\mu/l^\nu l_\nu .
\]

where \( y_\mu \) is transverse and \( \theta = l^\nu x_\nu \). In a similar way, one can write

\[
u_\mu = v_\mu + (k^\nu u_\nu)k_\mu/k^\nu k_\nu + (l^\nu u_\nu)l_\mu/l^\nu l_\nu .
\]

where \( v_\mu = dy_\mu/d\tau \) is transverse, \( k^\nu u_\nu = d\psi, \) and \( l^\nu u_\nu = d\theta \).
The transverse component of Eq. (1) is
\[ d_\tau (v_\mu + a_\mu) = 0, \]  \hspace{1cm} (A3)
from which it follows that
\[ v_\mu (\tau) = v_\mu (0) + a_\mu (0) - a_\mu (\tau). \]  \hspace{1cm} (A4)
Equation (A4) is the analog of Eq. (3).

By using Eq. (A4), one can rewrite the right side of Eq. (1) as \(-\partial_\mu (v^r v_\nu / 2)\). Since \(v^r v_\nu\) was assumed to be a function of \(\psi\), \(\partial_\mu = k_\mu d_\phi\). It follows from these results that the longitudinal components of Eq. (1) are
\[ d_\tau (k^\mu u_\mu) = -k^\mu k_\nu d_\phi (v^r v_\nu / 2), \quad d_\tau (l^\mu u_\mu) = 0. \]  \hspace{1cm} (A5)
It follows from the second of Eqs. (A5) that
\[ l^\mu u_\mu (\tau) = l^\mu u_\mu (0). \]  \hspace{1cm} (A6)
One way to obtain an expression for \(k^\nu u_\nu\) is to use the identity \(u^\nu u_\nu = 1\), which can be rewritten as
\[ v^r v_\nu + (k^\nu u_\nu)^2 / k^\nu k_\nu + (l^\nu u_\nu)^2 / l^\nu l_\nu = 1. \]  \hspace{1cm} (A7)
It follows from Eq. (A7) that
\[ (k^\nu u_\nu (\tau))^2 = [l^\nu u_\nu (\tau)]^2 + k^\nu k_\nu [1 - v^r v_\nu (\tau)]. \]  \hspace{1cm} (A8)
Equations (A6) and (A8) are the analogs of Eqs. (7) and (8). By using the expression for \(k^\nu u_\nu (0)\) that follows from Eq. (A8), and Eq. (A6), one can show that
\[ (k^\nu u_\nu (\tau))^2 = (k^\nu u_\nu (0))^2 + k^\nu k_\nu [v^r v_\nu (0) - v^r v_\nu (\tau)]. \]  \hspace{1cm} (A9)
Equation (A9) is the analog of Eq. (9). Another way to obtain an expression for \(k^\nu u_\nu\) is to change the independent variable in the first of Eqs. (A5) from \(\tau\) to \(\psi\). Since \(d_\tau \psi = k^\nu u_\nu\), the first of Eqs. (A5) becomes
\[ d_\phi \left[ (k^\nu u_\nu)^2 / 2 \right] = -k^\mu k_\nu d_\phi \left( v^r v_\nu / 2 \right). \]  \hspace{1cm} (A10)
from which Eq. (A9) follows.

Finally, since \(v^r v_\nu\) is a function of \(\psi\), Eqs. (A4), (A6), and (A9) express \(u_\mu\) as a function of \(\psi\). To express \(u_\mu\) as a function of \(\tau\) one must invert the solution of the phase equation
\[ d\tau / d_\psi = \pm 1/\omega (\psi), \]  \hspace{1cm} (A11)
where \(\omega\) is the square root of the terms on the right side of Eq. (A9).

**Appendix B: Guiding-Center Motion in a Planar Field**

Equation (6) is valid when the \(v^2\) terms in Eqs. (4) are independent of \(\phi\). To satisfy this condition we assumed that the field is circularly polarized and that the particle is in front of the pulse initially and not moving transversely. Equations (7), (9), and (10) follow from Eq. (6) and the definition of \(\gamma\), which requires that
\[ d_\tau (\gamma^2 - u^2 - v^2) = 0. \]  \hspace{1cm} (B1)
For the elliptically polarized field
\[ a^\mu = (0, 0, a_y \cos \phi, a_z \cos \phi), \]  \hspace{1cm} (B2)
where \(a_y = a \delta\) and \(a_z = a (1 - \delta^2) / 2\), the \(v^2\) terms in Eqs. (4) are not independent of \(\phi\), and Eq. (6) is not valid. However, the particle motion is known to consist of a fast oscillation about a guiding center and a guiding-center drift that varies slowly. In a vacuum, the guiding-center motion is governed by the equation
\[ d_\tau \langle u_\mu \rangle = -\partial_\mu \langle a^r a_\nu \rangle / 2, \]  \hspace{1cm} (B3)
where \(\langle \rangle\) denotes a \(\phi\)-average and \(\langle a^r a_\nu \rangle = -a^2 / 2\). We expect Eq. (B3) to provide a reasonable description of the guiding-center motion in a rarefied plasma, in which the phase speed of the field is slightly higher than the speed of light. Equation (B3) has associated with it the conservation equation
\[ d_\tau \left( \langle u^r \rangle + \langle a^r a_\nu \rangle \right) = 0. \]  \hspace{1cm} (B4)
Since the ponderomotive potential \( a^2/4 \) is independent of \( \phi \), it follows from Eq. (B3) that
\[
d_\tau (\langle \gamma \rangle - \langle u \rangle) = 0. \tag{B5}
\]

Equation (B5) is the analog of Eq. (6). Since \( \langle \gamma \rangle \) is constant, Eq. (B4) reduces to
\[
d_\tau (\langle \gamma \rangle^2 - \langle u \rangle^2 - a^2/2) = 0. \tag{B6}
\]

Equation (B6) is the analog of Eq. (B1). Thus, for a particle that is in front of the pulse initially, \( \gamma \) and \( u \) are given by Eqs. (7) and (9), in which \( v^2 \) is replaced by \( a^2/2 \), and the repelling conditions are described by Eq. (10).

**Appendix C: Particle Motion in a Planar Electrostatic Field**

The four-potential of an electrostatic field can be written as
\[
a_\mu = pk_\mu/k^\nu k_\nu + ql_\mu/l^\nu l_\nu, \tag{C1}
\]
where \( k^\mu \) and \( l^\mu \) were defined in Appendix A. We assume that \( a_\mu \) is a function of \( \psi \), from which it follows that \( \partial_\mu = k_\mu \partial_\phi \). Since the electrostatic field is unaffected by the gauge transformation \( a_\mu \rightarrow a_\mu + \partial_\mu b \), where \( b \) is an arbitrary function of \( \psi \), \( p \) is redundant. In the Lorentz gauge \( p = 0 \).

By substituting decomposition (C1) in Eq. (1) and contracting the resulting equation with \( k^\mu \), one can show that
\[
d_\tau (k^\mu u_\mu + p) = (k^\nu u_\nu) d_\phi p - (l^\nu u_\nu) d_\phi q. \tag{C2}
\]

Since \( k^\nu u_\nu = d_\phi \psi \), the \( p \) terms in Eq. (C2) cancel, as they must do. By substituting decomposition (C1) in Eq. (1) and contracting the resulting equation with \( l^\mu \), one can show that
\[
d_\tau (l^\mu u_\mu + q) = 0. \tag{C3}
\]

It follows from Eq. (C3) that
\[
l^\mu u_\mu (\tau) = l^\mu u_\mu (0) + q(0) - q(\tau). \tag{C4}
\]

One way to obtain an expression for \( k^\nu u_\nu \) is to use the identity \( u^\nu u_\nu = 1 \), which can be rewritten as
\[
\left[ k^\nu u_\nu (\tau) \right]^2 = \left[ l^\nu u_\nu (\tau) \right]^2 - l^\nu l_\nu. \tag{C5}
\]

Another way to obtain an expression for \( k^\nu u_\nu \) is to solve Eq. (C2) directly. By changing the independent variable from \( \tau \) to \( \psi \), one can rewrite Eq. (C2) as
\[
d_\phi \left[ (k^\nu u_\nu)^2 / 2 \right] = d_\phi \left[ (l^\nu u_\nu)^2 / 2 \right], \tag{C6}
\]
from which Eq. (C5) follows.

Since \( q \) is a function of \( \psi \), Eqs. (C4) and (C5) express \( u_\mu \) as a function of \( \psi \). To express \( u_\mu \) as a function of \( \tau \), one must invert the solution of the phase equation
\[
d_\tau /d_\psi = \pm 1/\omega(\psi), \tag{C7}
\]
where \( \omega \) is the square root of the terms on the right side of Eq. (C5).

In the wave frame \( k^\mu_\mu = (0, l, 0, 0) \) and \( l^\mu_\mu = (l, 0, 0, 0) \), where \( l = (r^2 - 1)^{1/2} \). It follows from these results that \( \psi = -k^\nu x^\nu \), \( k^\nu u_\nu = -lu_\nu \), \( l^\nu u_\nu = l \phi \), and \( q = l \phi \), where \( \phi \) is the electrostatic potential. Thus, Eq. (C4) can be rewritten as
\[
\gamma'(\tau) = \gamma'(0) + \phi'(0) - \phi'(\tau) = 0, \tag{C8}
\]
Eq. (C5) can be rewritten as
\[
\left[ u'(\tau) \right]^2 = \left[ \gamma'(\tau) \right]^2 - 1, \tag{C9}
\]
and Eq. (C7) can be rewritten as
\[
d_\tau /d\lambda = \mp 1/\omega(\lambda), \tag{C10}
\]
where \( \omega \) is the square root of the terms on the right side of Eq. (C9). The dephasing time of an accelerated particle can be determined from Eq. (C10) in a manner similar to that described previously. In particular, by considering the relations between laboratory-frame and wave-frame quantities, one can show that the dephasing time is proportional to \( \gamma_W^2 \lambda \), where \( \gamma_W \) is the Lorentz factor associated with the phase speed of the wave and \( \lambda \) is the wavelength.

**DEPHASING TIME OF AN ELECTRON ACCELERATED BY A LASER PULSE**

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DEPHASING TIME OF AN ELECTRON ACCELERATED BY A LASER PULSE

The potential associated with a large-amplitude plasma wave is described by elliptic functions. Simple formulas for the injection energy and energy gain associated with this potential were determined by Esarey and Piloff. The dephasing times associated with this and other potentials were studied by Teychenné, Bonnaud, and Bobin.

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