

A Generalized Measurable Ignition Condition for Inertial Confinement Fusion

In inertial confinement fusion (ICF),¹ a shell of cryogenic deuterium and tritium (DT) thermonuclear fuel is accelerated inward by direct laser irradiation or by the x rays produced by heating a high-Z enclosure (hohlraum). At stagnation, the compressed fuel is ignited by a central hot spot surrounded by a cold, dense shell. Ignition occurs when the alpha-particle heating of the hot spot exceeds all the energy losses. To measure progress toward ignition, a metric is needed to assess how an implosion experiment performs with respect to the ignition condition. In a stationary plasma, the ignition condition is given by the Lawson criterion.² In ICF, the same ignition condition must be derived in terms of measurable parameters. Different forms of the 1-D ignition condition have been derived,^{1,3,4} but none of them can be accurately measured. Measurable parameters of the ICF fuel assembly are the areal density, the ion temperature, and the neutron yield. This article demonstrates that the ICF ignition condition can be written in terms of these measurable parameters. We start from the 1-D ignition model of Ref. 5 and generalize it to multidimensions through a single parameter: the yield-over-clean (YOC). The YOC is the ratio of the measured neutron yield to the predicted 1-D yield. The latter must be calculated consistently with the measured ρR and T_i . The generalized ignition criterion depends on the areal density, the ion temperature, and the YOC. Alternatively, the ignition condition can be written in terms of the areal density, the neutron yield, and the target mass.

This article first deals with the 3-D extension of the dynamic ignition model^{5,6} and an analytic ignition condition. The results of hydrodynamic simulations of imploding capsules forming the database used to generate a more-accurate ignition condition will also be shown. A measurable criterion requires the solution of a dynamic ignition model. The analysis starts by modifying the 1-D ignition model [Eq. (15) of Ref. 5] and the following considerations about multidimensional effects: The hot spot is enclosed by a surrounding shell that can be highly distorted by hydrodynamic instabilities. The hot-spot volume V_{hs} is bounded by Rayleigh–Taylor (RT) bubbles and spikes from the shell. The plasma in the bubbles is cold and does not contribute to the fusion yield. Following the analysis of Ref. 7,

we assume that only the “clean” hot-spot volume V_{clean} within the RT spikes (Fig. 121.15) is hot enough to induce fusion reactions, and the central temperature is unchanged by the RT evolution as long as the RT spikes do not reach the hot spot’s center. The 1-D ignition model can be extended to 3-D by integrating the alpha-particle energy deposition over the clean hot-spot volume, leading to

$$\frac{d}{d\tau}(\hat{P}\hat{R}^3) = -2\hat{P}\hat{R}^2 \frac{d\hat{R}}{d\tau} + \gamma_\alpha \hat{P}^2 \hat{T}\hat{R}_{clean}^3, \quad (1)$$

$$\frac{d}{d\tau} \left(\frac{\hat{P}\hat{R}^3}{\hat{T}} \right) = \hat{R}\hat{T}^{5/2}, \quad (2)$$

$$\frac{d^2\hat{R}}{d\tau^2} = \hat{P}\hat{R}^2. \quad (3)$$

With respect to the 1-D case, the alpha heating is reduced by the clean volume fraction R_{clean}^3/R^3 , where R_{clean} and R are

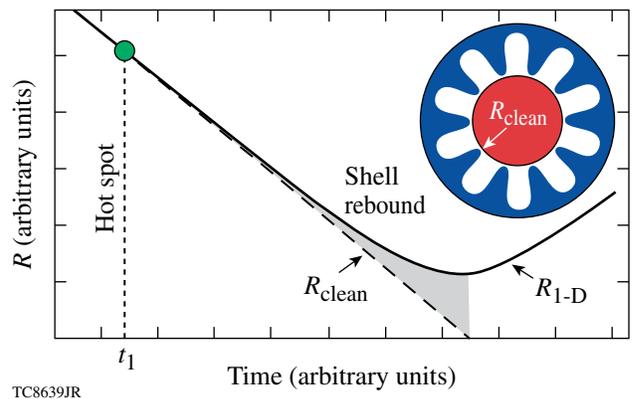


Figure 121.15 Schematic of the free-fall model. Fusion reactions occur only in the clean volume within the Rayleigh–Taylor spikes. The spikes “free-fall” after saturation of the linear growth.

the clean and 1-D radii, respectively. We assume this to be the main effect of the implosion nonuniformities. In Eqs. (1)–(3), the hot-spot radius R , pressure P , and central temperature T are normalized with their stagnation values calculated without including the alpha-particle energy deposition $R_{\text{stag}}^{\text{no } \alpha}$, $P_{\text{stag}}^{\text{no } \alpha}$, and $T_*^{\text{no } \alpha}$ defined later. The dimensionless time $\tau = tV_i/R_{\text{stag}}^{\text{no } \alpha}$ is a function of the implosion velocity V_i . Equations (1)–(3) represent the hot-spot energy balance, the temperature equation from the hot-spot mass conservation, and the thin-shell Newton’s law, respectively. For simplicity, we have neglected the radiation losses (included in Ref. 5) in the derivation but retained in the simulation. The expansion [first term on the right-hand side of Eq. (1)] and the heat-conduction losses [right-hand side of Eq. (2)] are retained. This article focuses on the 3-D effects included in the term R_{clean} in Eq. (1). The term γ_α governs the ignition conditions and can be written as

$$\gamma_\alpha = \left(\varepsilon_\alpha C_0 P_{\text{stag}}^{\text{no } \alpha} R_{\text{stag}}^{\text{no } \alpha} T_*^{\text{no } \alpha} \right) / (8 V_i), \quad (4)$$

where ε_α is the alpha-particle energy (3.5 MeV) and $C_0 \simeq 2.5 \times 10^{-26} \text{ m}^3 \text{ keV}^{-3} \text{ s}^{-1}$ comes from approximating the volume integral of the fusion rate around a 4- to 15-keV central temperature with a power law $\sim T^3$. The initial conditions are defined at the time of peak implosion velocity V_i : $P(0) = P_0$, $R(0) = R_0$, $\dot{R}(0) = -V_i$, and $T(0) = T_0$. The stagnation values $R_{\text{stag}}^{\text{no } \alpha}$, $P_{\text{stag}}^{\text{no } \alpha}$, and $T_{\text{stag}}^{\text{no } \alpha}$ are obtained by solving the dimensional form of Eqs. (1)–(3) without alpha-particle–energy deposition ($\gamma_\alpha = 0$) and in the limit of large initial kinetic energy $\epsilon_0 = (M_{\text{shell}} V_i^2 / 4\pi P_0 R_0^3) \gg 1$. This leads to the following stagnation values without alphas:

$$P_{\text{stag}}^{\text{no } \alpha} \simeq P_0 \epsilon_0^{5/2}, \quad R_{\text{stag}}^{\text{no } \alpha} \simeq R_0 \epsilon_0^{-1/2}, \quad (5)$$

$$T_*^{\text{no } \alpha} \simeq \left(1.2 P_{\text{stag}}^{\text{no } \alpha} R_{\text{stag}}^{\text{no } \alpha} V_i / \kappa_0 \right)^{2/7}, \quad (6)$$

where $T_*^{\text{no } \alpha} \simeq 1.3 T_{\text{stag}}^{\text{no } \alpha}$ and $\kappa_0 \simeq 3.7 \times 10^{69} \text{ m}^{-1} \text{ s}^{-1} \text{ J}^{-5/2}$ is the coefficient of Spitzer thermal conductivity $\kappa_{\text{Sp}} \simeq \kappa_0 T^{5/2}$ for $\ln \Lambda \simeq 5$. Using the no- α stagnation values, the initial conditions of the dimensionless model are rewritten in the simple form $\hat{P}(0) = \epsilon_0^{-5/2}$, $\hat{T}(0) = \epsilon_0^{-1/2}$, $\hat{R}(0) = \epsilon_0^{-1/2}$, and $\hat{\dot{R}}(0) = -1$. The ignition model comprises Eqs. (1)–(3) and the initial conditions. Ignition is defined by the critical value of the parameter γ_α in Eq. (1), yielding an explosive singular solution. In the limit of $\epsilon_0 \rightarrow \infty$, the critical value of γ_α depends solely on the effect of nonuniformities entering through the clean radius R_{clean} . In the absence of nonuniformities (1-D), $R_{\text{clean}} = R$ and the critical value of γ_α is γ_α (1-D) $\simeq 1.1$. As the alpha heating raises the

hot-spot temperature, the RT spikes are ablated by the enhanced heat flux as well as by the alpha particles leaking from the hot spot and depositing their energy onto the spikes.⁸ This causes the ablative stabilization of the RT and an enhancement of the clean volume. This effect can be heuristically included by letting the clean radius increase up to the 1-D radius as the hot-spot temperature rises above the no- α value.

The aim of the new ignition model is to identify a measurable parameter describing the effects of hot-spot nonuniformities entering through the time history of the clean radius $R_{\text{clean}}(\tau)$. The RT spikes first grow exponentially until reaching a saturation amplitude. After saturation, the spikes free-fall into the hot spot as shown in Fig. 12.15; the acceleration $g(t) = R''(t)$ determines the linear growth rates $\gamma_{\text{RT}} = \sqrt{k g(t)}$, where $k \sim \ell/R(t)$ is the perturbation wave number. The number of e foldings of linear growth is

$$n_e = \sqrt{\ell} \hat{n}_e = \int_0^{t_{\text{lin}}} \gamma_{\text{RT}}(t) dt,$$

where t_{lin} is the interval of linear growth up to saturation. In the nonlinear free-fall stage, the spikes’ amplitude grows as

$$\Delta R \approx \eta(t_{\text{lin}}) + \int_{t_{\text{lin}}}^t dt' \int_{t_{\text{lin}}}^{t'} g(t'') dt'',$$

where $\eta(t_{\text{lin}})$ is the linear amplitude at saturation. For simplicity, we assume that the linear growth can be neglected [small $\eta(t_{\text{lin}})$] with respect to the nonlinear growth so that the spike amplitude ΔR depends only on t_{lin} and t . This leads to a clean radius $R_{\text{clean}} = R - \Delta R = R(t_{\text{lin}}) + R'(t_{\text{lin}})(t - t_{\text{lin}})$ for $t > t_{\text{lin}}$. Before t_{lin} , the clean radius equals the 1-D radius, $R_{\text{clean}} \simeq R$. The time t_{lin} depends on the amplitude of the inner DT-ice roughness at the end of the acceleration phase. The larger the initial nonuniformity level, the smaller the time t_{lin} . We first solve Eqs. (1)–(3) without alpha-particle–energy deposition and compute $\hat{R}^{\text{no } \alpha}(\tau)$. Then we use $\hat{R}^{\text{no } \alpha}$ to determine \hat{R}_{clean} using the free-fall model. The most-severe reduction of the clean volume corresponds to $\tau_{\text{lin}} = 0$, when the nonlinear RT growth starts from the beginning of the deceleration phase. The number of e foldings of linear growth is directly proportional to

$$\hat{n}_e^{\text{no } \alpha} \simeq \frac{\pi}{2} + \arctan \left(\sqrt{\epsilon_0} - \frac{\epsilon_0}{\tau_{\text{lin}}} \right). \quad (7)$$

For a given τ_{lin} , we compute $\hat{n}_e^{\text{no } \alpha}$, $R_{\text{clean}}(\tau, \tau_{\text{lin}})$, and the yield-over-clean without alphas (YOC^{no } \alpha}):

$$\text{YOC}^{\text{no } \alpha} = \frac{\int_0^\infty \hat{p}^2 \hat{T} \hat{R}_{\text{clean}}^3 d\tau}{\int_0^\infty \hat{p}^2 \hat{T} \hat{R}^3 d\tau}, \quad (8)$$

where \hat{p} , \hat{T} , and \hat{R} are the solutions of Eqs. (1)–(3) without alpha-particle–energy deposition (i.e., $\gamma_\alpha = 0$). The $\text{YOC}^{\text{no } \alpha}$ is the ratio of the neutron yield for a reduced clean volume to the 1-D neutron yield for the case without alphas. Both $\text{YOC}^{\text{no } \alpha}$ and $\hat{n}_e^{\text{no } \alpha}$ depend on τ_{lin} , and a relation can be numerically derived, yielding the functional relation $\hat{n}_e^{\text{no } \alpha} = \hat{n}_e^{\text{no } \alpha}(\text{YOC}^{\text{no } \alpha})$. Since $\hat{n}_e^{\text{no } \alpha}$ is a measure of the initial nonuniformities, $\text{YOC}^{\text{no } \alpha}$ can also be used to define the initial nonuniformities' level. For a given value of $\text{YOC}^{\text{no } \alpha}$, it is possible to determine the ignition condition, including the effects of nonuniformities, by solving Eqs. (1)–(3) with alpha deposition for the corresponding clean radius \hat{R}_{clean} and by varying γ_α to find the critical value for a singular solution. We start by determining the transition time τ_{lin} from linear to nonlinear growth by solving Eqs. (1)–(3) with $\hat{R}_{\text{clean}} \approx \hat{R}$ (valid in the linear regime) and a given value of γ_α . The resulting radius $R^\alpha(\tau)$ is used to compute the linear e foldings:

$$\hat{n}_e^\alpha(\tau_{\text{lin}}) = \int_0^{\tau_{\text{lin}}} \sqrt{R^{\alpha''}/R^\alpha} d\tau. \quad (9)$$

This is used to determine the time τ_{lin} by setting

$$\hat{n}_e^\alpha(\tau_{\text{lin}}) = \hat{n}_e^{\text{no } \alpha}(\text{YOC}^{\text{no } \alpha}),$$

leading to a functional relation $\tau_{\text{lin}} = \tau_{\text{lin}}(\text{YOC}^{\text{no } \alpha})$. Using τ_{lin} , the clean radius history follows from

$$\hat{R}_{\text{clean}}^\alpha = \hat{R}^\alpha(\tau_{\text{lin}}) + \hat{R}^{\alpha'}(\tau_{\text{lin}})(\tau - \tau_{\text{lin}}). \quad (10)$$

The effect of nonuniformities on ignition is studied by varying the initial level of nonuniformities through $\text{YOC}^{\text{no } \alpha}$, computing τ_{lin} , and finding the critical γ_α in Eq. (1), yielding a singular explosive solution. This leads to the 3-D ignition condition shown in Fig. 121.16, which can be approximated by $\gamma_\alpha(\text{YOC}^{\text{no } \alpha})^{4/5} > 1.2$. Using the definition γ_α in Eq. (4) and substituting the energy conservation and the shell mass at stagnation (modified to include the finite shell-thickness effects⁵), one finds that $\gamma_\alpha \sim (\rho R)^{3/4} T_*^{15/8}$, leading to the following analytic ignition condition:

$$\chi^{\text{an}} \approx \rho R_{\text{tot}}^{\text{no } \alpha} (T^{\text{no } \alpha} / 4.5)^{5/2} (\text{YOC}^{\text{no } \alpha})^\mu \approx 1, \quad (11)$$

where $\rho R_{\text{tot}}^{\text{no } \alpha}$ is the total areal density (approximately equal to the shell areal density) in g/cm^2 , $T^{\text{no } \alpha}$ is the peak hot-spot

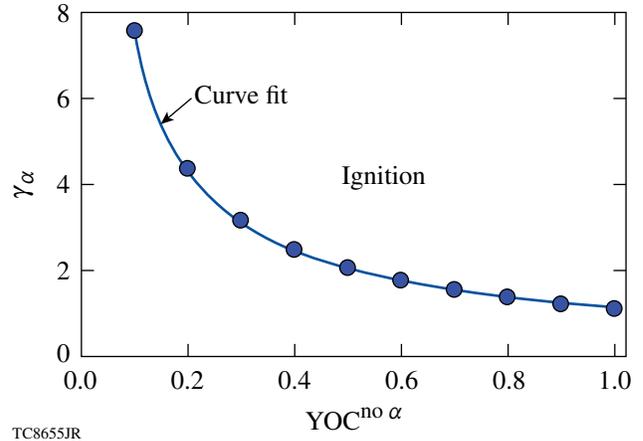
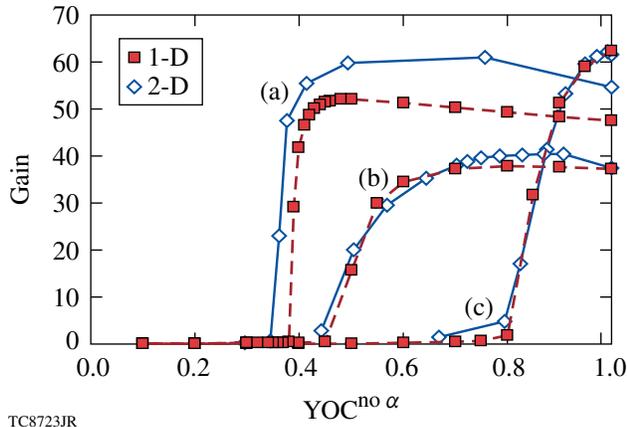


Figure 121.16

The critical parameter γ_α required for a singular solution of Eqs. (1)–(3) versus the YOC. The numerical solution can be fitted by a simple power law $\gamma_\alpha \approx 1.2/(\text{YOC}^{\text{no } \alpha})^{4/5}$.

temperature in keV, and $\mu \approx 1$. Equation (11) represents a measurable criterion that can be used to assess the 3-D implosion performance, provided the alpha particles do not significantly change the hydrodynamics. This is the case with surrogate deuterium D_2 and tritium–hydrogen–deuterium (THD) [with a few % of D (Ref. 9)] as well as low-gain (<10%) DT capsules. Obviously, ignited DT capsules do not require an ignition criterion. The effect of nonuniformities enters the ignition condition through a single parameter: the YOC. The accuracy of the generalized ignition condition can be improved by including the effect of the ablative stabilization of the deceleration RT and by tuning the power indices in Eq. (11) through a set of numerical simulations. We have carried out a set of 2-D simulations of ignition targets with varying inner-ice-surface roughness using the code *DRACO*.¹⁰ The initial ice roughness is increased until ignition fails. Each run is repeated without the alpha-particle–energy deposition to determine the no- α neutron yield and the $\text{YOC}^{\text{no } \alpha}$. A gain curve is generated by plotting the energy gain (fusion energy yield/laser energy on target) versus the $\text{YOC}^{\text{no } \alpha}$. Figure 121.17 shows the gain curves for (a) a 420-kJ direct-drive–ignition target designed to simulate the 1-MJ indirect-drive point design¹¹ for the National Ignition Facility (NIF),¹² (b) the 1.5-MJ, all-DT direct-drive point design,¹³ and (c) the 1-MJ direct-drive wetted-foam design.¹⁴

To validate the clean volume analysis used in the analytic ignition model, we compare the result of 2-D simulations with the same gain curve obtained from 1-D simulations, where the fusion rate $\langle \sigma v \rangle$ is reduced by a factor ξ equal to the $\text{YOC}^{\text{no } \alpha}$. Since the alpha-energy deposition depends on the product



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Figure 121.17

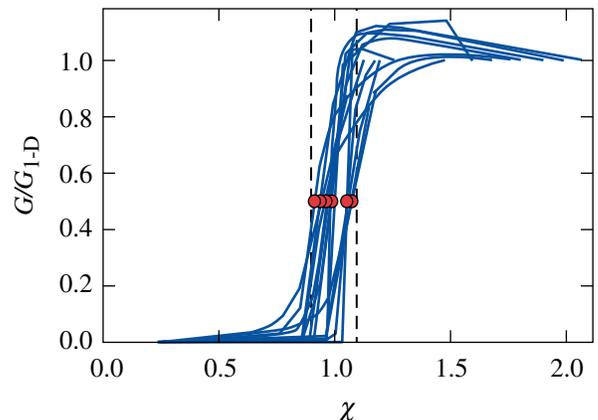
Energy gain versus $YOC^{no \alpha}$ computed with 1-D (squares) and 2-D (diamonds) simulations. The 2-D simulations use a varying initial ice roughness. The 1-D simulations use a fusion rate reduced by the YOC to mimic the reduction of the clean hot-spot volume. The gain curves are for (a) a 420-kJ direct-drive surrogate of the 1-MJ indirect-drive NIF point design, (b) the 1.5-MJ, all-DT direct-drive point design, and (c) the 1-MJ direct-drive wetted-foam design.

$\langle \sigma v \rangle V_{\text{clean}}$, reducing $\langle \sigma v \rangle$ in the 1-D code by the factor $\xi = YOC^{no \alpha}$ is approximately equivalent to reducing the hot-spot volume by the clean volume fraction. In the 1-D code, the reduction of $\langle \sigma v \rangle$ takes effect as long as the central hot-spot temperature is below 10 keV. For temperatures above 10 keV, the hot spot is robustly ignited, the RT becomes ablatively stabilized, and ξ is increased linearly with the temperature until $\xi = 1$ for $T > 15$ keV. This effect can also be included in the analytic model by letting R_{clean} approach R_{1-D} [in Eq. (1)] as the temperature exceeds its no- α value. This leads to a reduction of the YOC exponent in Eq. (11) ($\mu \approx 0.8$) and an analytic ignition condition $\chi^{\text{an}} \approx \rho R_{\text{tot}}^{no \alpha} (T_n^{no \alpha} / 4.5)^{5/2} (YOC^{no \alpha})^{0.8} \approx 1$. Phasing out the reduction factor ξ after ignition makes it possible for the 1-D code to correctly predict the burn-wave propagation through the cold shell and the final gain. The results from the modified 1-D code are compared with the 2-D simulations for the three targets above. As shown in Fig. 121.17, the modified 1-D code predicts the “ignition cliff” for critical values of the $YOC^{no \alpha}$ in agreement with the 2-D simulations. The ignition cliff represents the sharp decrease in gain occurring for a critical value of the YOC. After validating the modified 1-D code with the 2-D simulations, we used the fast 1-D code to generate a database of $\rho R_n^{no \alpha}$, $T_n^{no \alpha}$, and $YOC^{no \alpha}$ for marginally ignited capsules with the ignition YOC varying between 0.3 and 0.8. Marginal ignition is defined as the gain corresponding to the middle point of the ignition cliff (~half the 1-D gain). This is a physical definition of ignition describing the onset of the burn-wave propagation. The 3-D ignition criterion based on a

power law of the three measurable parameters has been derived through the best fit of the simulation results. Figure 121.18 shows the normalized gain curves ($G/G_{1-D} = \text{gain}/1\text{-D gain}$) from the database versus the ignition parameter χ representing the “best fit.” The best fit of the ignition criterion $\chi \approx 1$ yields

$$\chi^{\text{fit}} \equiv \rho R_{\text{tot}(n)}^{no \alpha} (T_n^{no \alpha} / 4.7)^{2.1} (YOC^{no \alpha})^{\mu} \quad (12)$$

with $\mu \approx 0.63$. This fit predicts the ignition cliff with a $\pm 10\%$ error. The subscript n indicates the spatial and temporal average with the fusion rate (i.e., neutron average) used to approximate the experimental observables. Note that $T_n^{no \alpha}$ in Eq. (12) is the 1-D temperature. Since the central temperature decreases slightly with increasing nonuniformities (lower YOC), one would expect a weaker dependence on the YOC in Eq. (12) when the 2-D (or the measured) temperature is used. This is shown by the fit from a LASNEX¹⁵ 2-D simulation database of DT and surrogate THD⁹ NIF-point-design targets. A fit of the gain curves using the LASNEX database yields an ignition condition like Eq. (12) with $\mu \approx 0.47$. The best-performing DT cryogenic implosion on OMEGA¹⁶ to date has achieved an areal density of ≈ 0.2 g/cm² and a temperature of ≈ 2 keV with a YOC of $\approx 10\%$ (Ref. 17), leading to an ignition parameter $\chi \sim 10^{-2}$. Notice that the $YOC^{no \alpha} \equiv (Y^{\text{ex}} / Y^{1-D})$ requires the 1-D yield (Y^{1-D}) as normalization of the experimental yield (Y^{ex}). Since the 1-D yield is a strong function of the temperature, one expects a severe reduction of the temperature dependence in Eq. (12). A fit of the simulation database used in Fig. 121.18



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Figure 121.18

Gain curves from the simulation database. The normalized gain G/G_{1-D} is plotted versus the ignition parameter χ . The ignition cliff is predicted by $\chi = 1$ with a $\pm 10\%$ error.

shows that an approximate ignition condition ($\pm 20\%$ error) for DT targets can be written without the temperature as

$$\rho R_{\text{tot(n)}}^{\text{no } \alpha} \left[0.1 Y_{16(\text{no } \alpha)}^{\text{ex}} / M_{\text{sh}}^{\text{mg}} \right]^{0.58} \approx 1, \quad (13)$$

where Y_{16}^{ex} is in units of 10^{16} neutrons and M_{sh} (in mg) is the portion of the shell mass stagnating at the time of peak neutron rate (bang time). For typical ICF implosions, M_{sh} is about half of the unablated shell mass. The latter can be measured or estimated from the simulations with reasonable accuracy. This result is in reasonable agreement with the analysis of Spears *et al.*⁹ of the simulated down-scattered neutron spectrum database for the NIF point-design target (fixed M_{sh}). An ignition condition similar to Eq. (12) can be recovered from Eq. (13) by setting $Y^{\text{ex}} = \text{YOC} \cdot Y^{1\text{-D}}$ and by using the following fit for $Y^{1\text{-D}}$ of DT targets from a 1-D simulation database:

$$Y_{16(\text{no } \alpha)}^{1\text{-D}} \approx \left(\frac{T_n^{\text{no } \alpha}}{4.7} \right)^{4.7} \left[\rho R_{\text{tot(n)}}^{\text{no } \alpha} \right]^{0.6} \left(\frac{M_{\text{sh}}^{\text{mg}}}{0.1} \right). \quad (14)$$

The criteria of Eqs. (12) or (13) can be used to assess the performance of cryogenic implosions on the NIF and OMEGA.

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