

Polychromatic Tomography of High Energy Density Plasmas

**T. Nagayama¹, R. Mancini¹, R. Florido¹,
R. Tommasini², J. Koch²,
J. Delettrez³, S. Regan³, V. Smalyuk³**

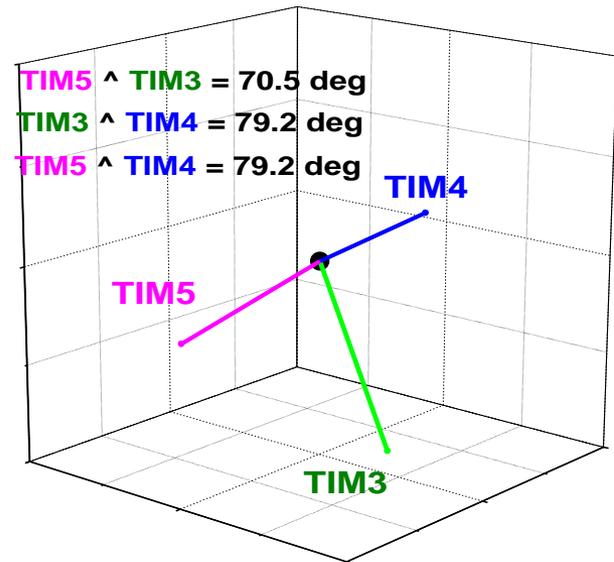
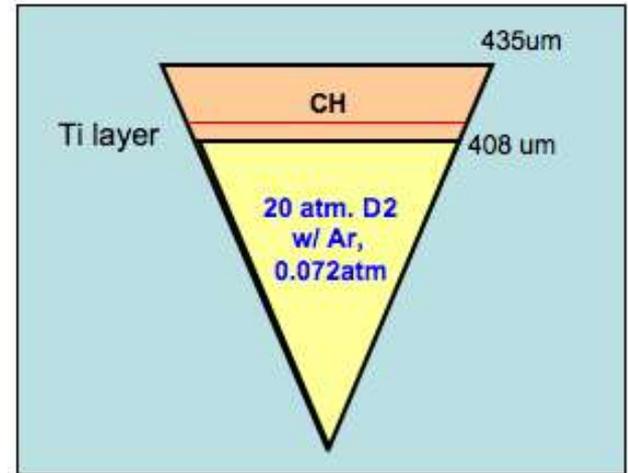
¹Physics Department, University of Nevada, Reno

²Lawrence Livermore National Laboratory

³Laboratory for Laser Energetics, University of Rochester

OMEGA direct-drive implosions

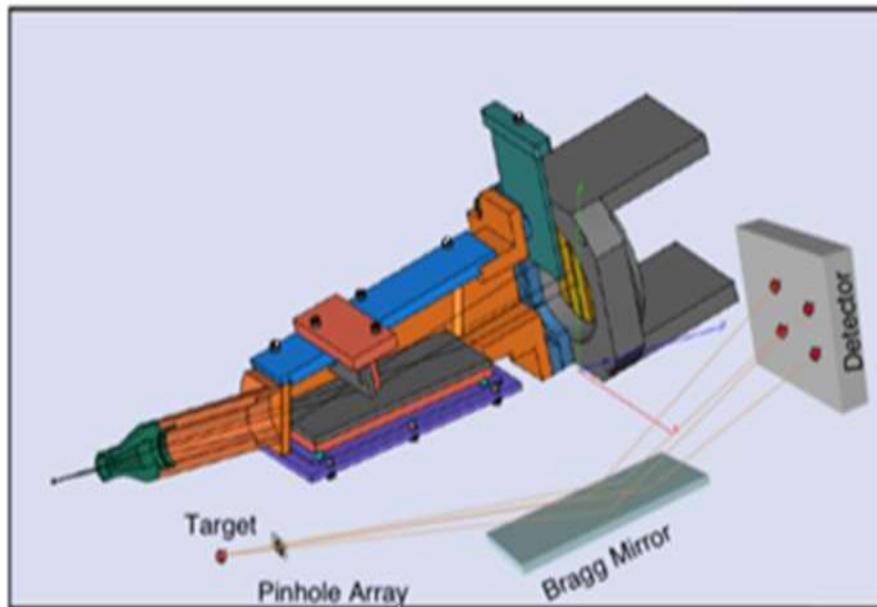
- The amount of Ar has to be very small:
 - Not to change the hydrodynamics
 - To keep the optical depth of the He β and Ly β (n=3-1 transitions) small
- Laser:
 - 60 beams, several pulse shapes
 - Smoothing: 2D-SSD/DPP-SG4/DPR
- Three identical DDMMI instruments:
 - DDMMI \equiv Direct-Drive Multi-Monochromatic x-ray Imager
 - Fielded along 3 quasi-orthogonal lines of sight (TIM3/TIM4/TIM5)
 - Record a collection of, gated, spectrally-resolved x-ray images of the implosion core



Spectrally-resolved core imaging with DDMMI

DDMMI \equiv Direct-Drive Multi-Monochromatic x-ray Imager

- A pinhole-array coupled to a multi-layer Bragg mirror produces many quasi-monochromatic core images, each one characteristic of a slightly different photon energy range^{1,2}



Pinhole is snout-mounted and placed as close as possible to target to maximize signal and spatial resolution, for a given pinhole aperture.

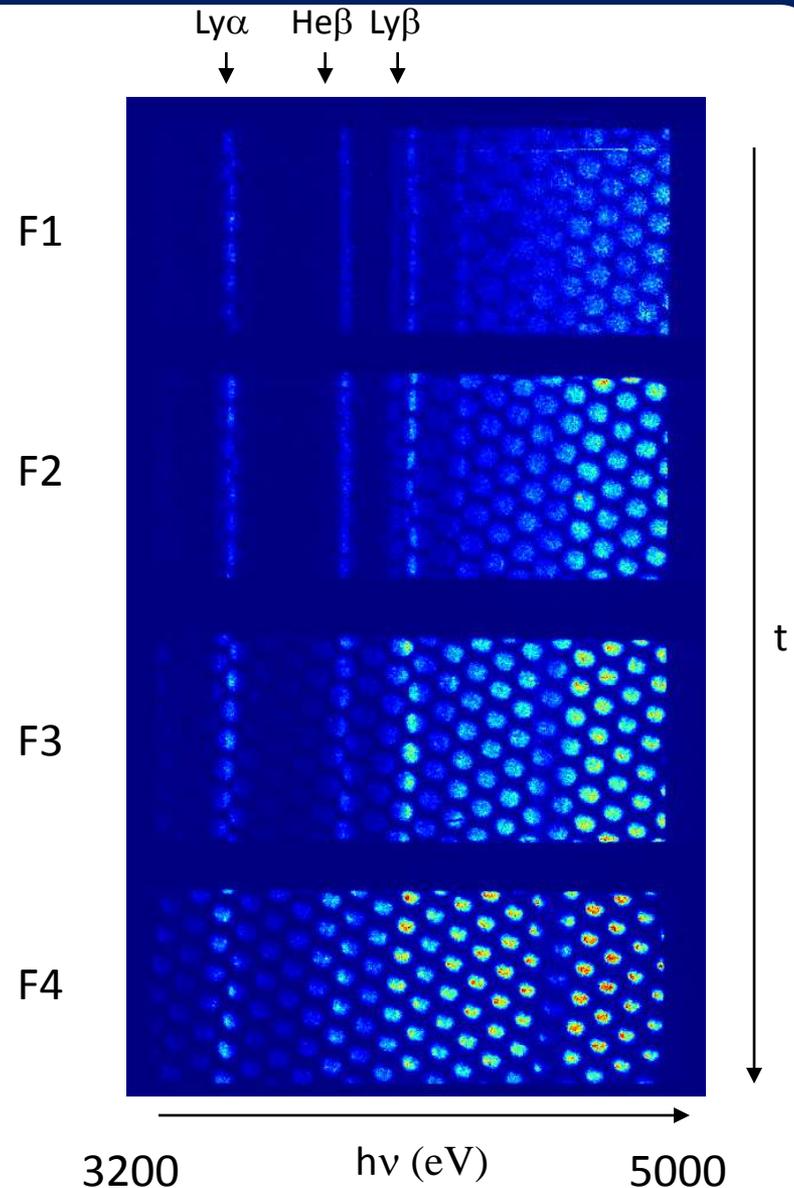
- pinhole array-target distance = 31.5mm
- target-mirror distance = 188mm
- Pinhole diameter = 10 μ m
- detector = gated X-ray framing cameras
- images recorded with CCD or film.
- Magnification, $M = 8.5X$.

¹R. Tommasini, J. Koch, N. Izumi, L. Welsler, R. Mancini, J. Delettrez, S. Regan and V. Smalyuk, Rev. Sci. Instrum. 77, 10E303 (2006);

²T. Nagayama, R. Mancini, R. Florido, R. Tommasini, J. Koch, J. Delettrez, S. Regan, V. Smalyuk, L. Welsler, and I. Golovkin, Rev. Sci. Instrum. 79, 10E921 (2008);

DDMMI data: spectrally resolved images

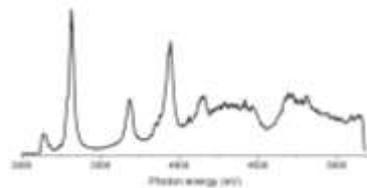
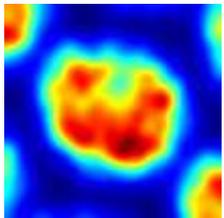
- Collection of gated, spectrally-resolved images
- Time increases from F1 to F4
- Photon energy axis increases from left to right
- Resolution:
 - Spatial: $\Delta x = 10 \mu\text{m}$
 - Spectral: $E/\Delta E = 150$
 - Frame separation = 100 ps



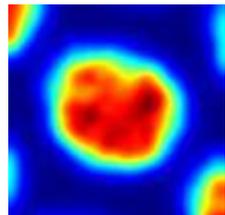
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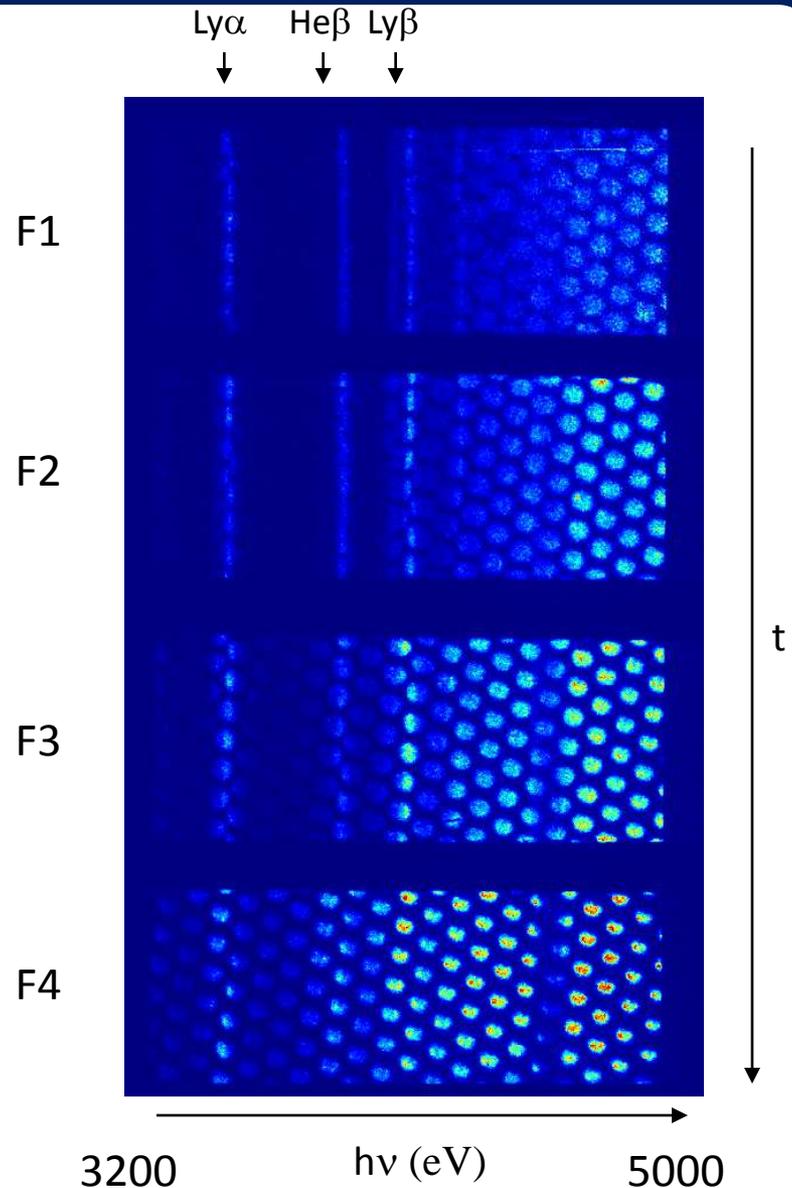
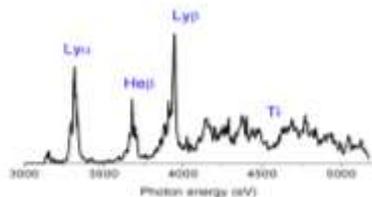
Narrow-band (He β) Space-integrated



Broad-band

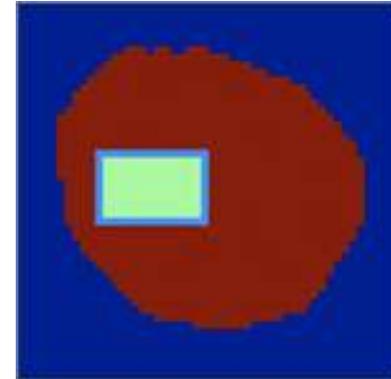
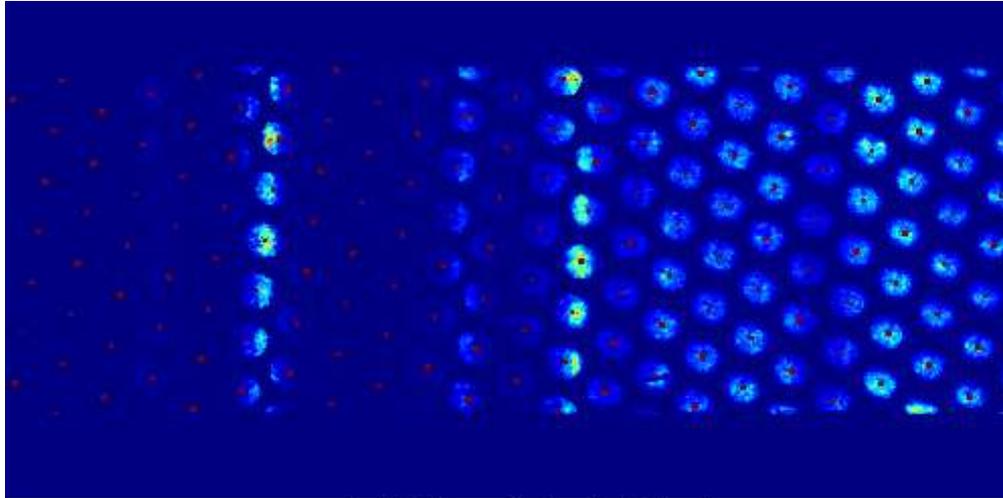


Space-resolved

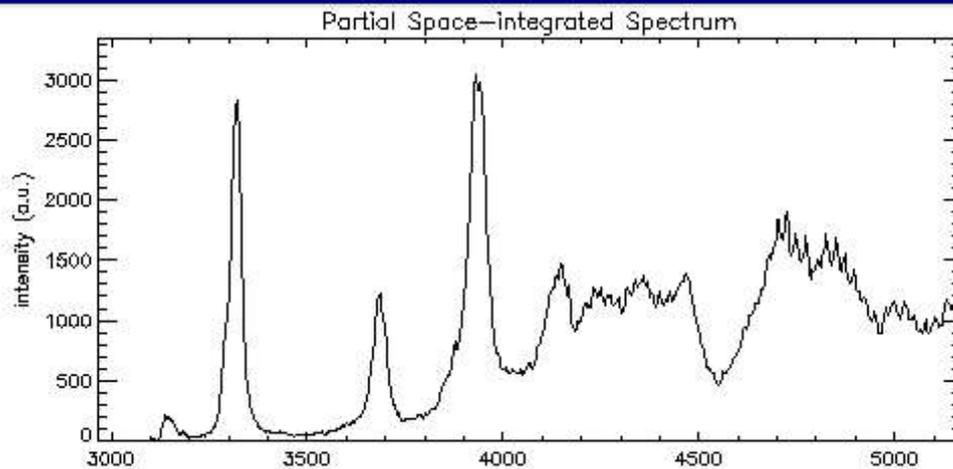


Data processing: space-resolved spectrum (SRS)

- What if we pick up the contributions only from a selected region of the core image?

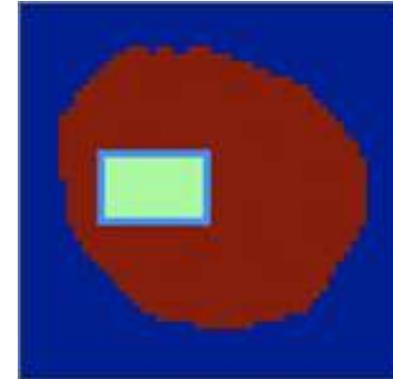
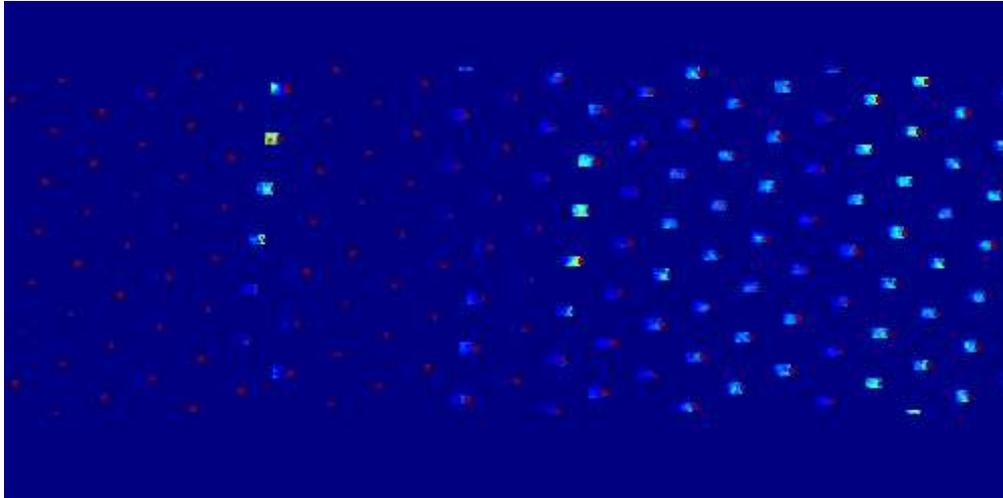


Mask of selected region

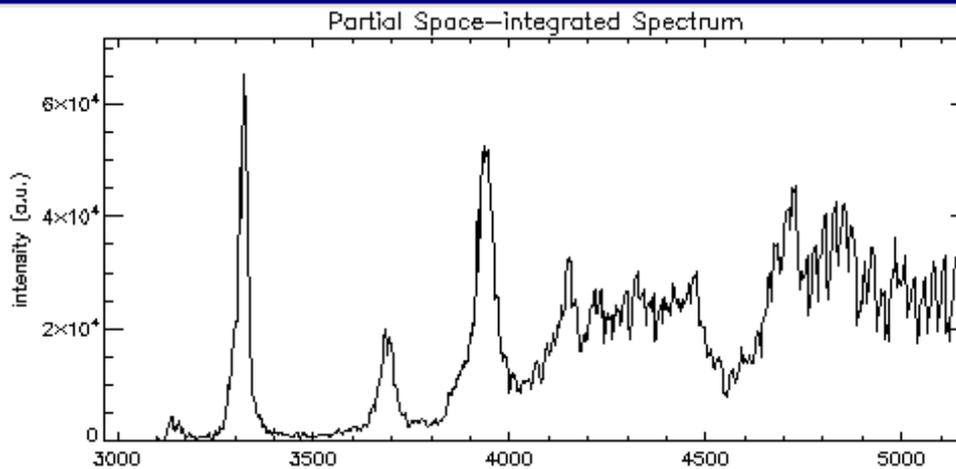


Data processing: space-resolved spectrum (SRS)

- What if we pick up the contributions only from a selected region of the core image?
- The result is a space-resolved spectrum integrated along a chord in the core



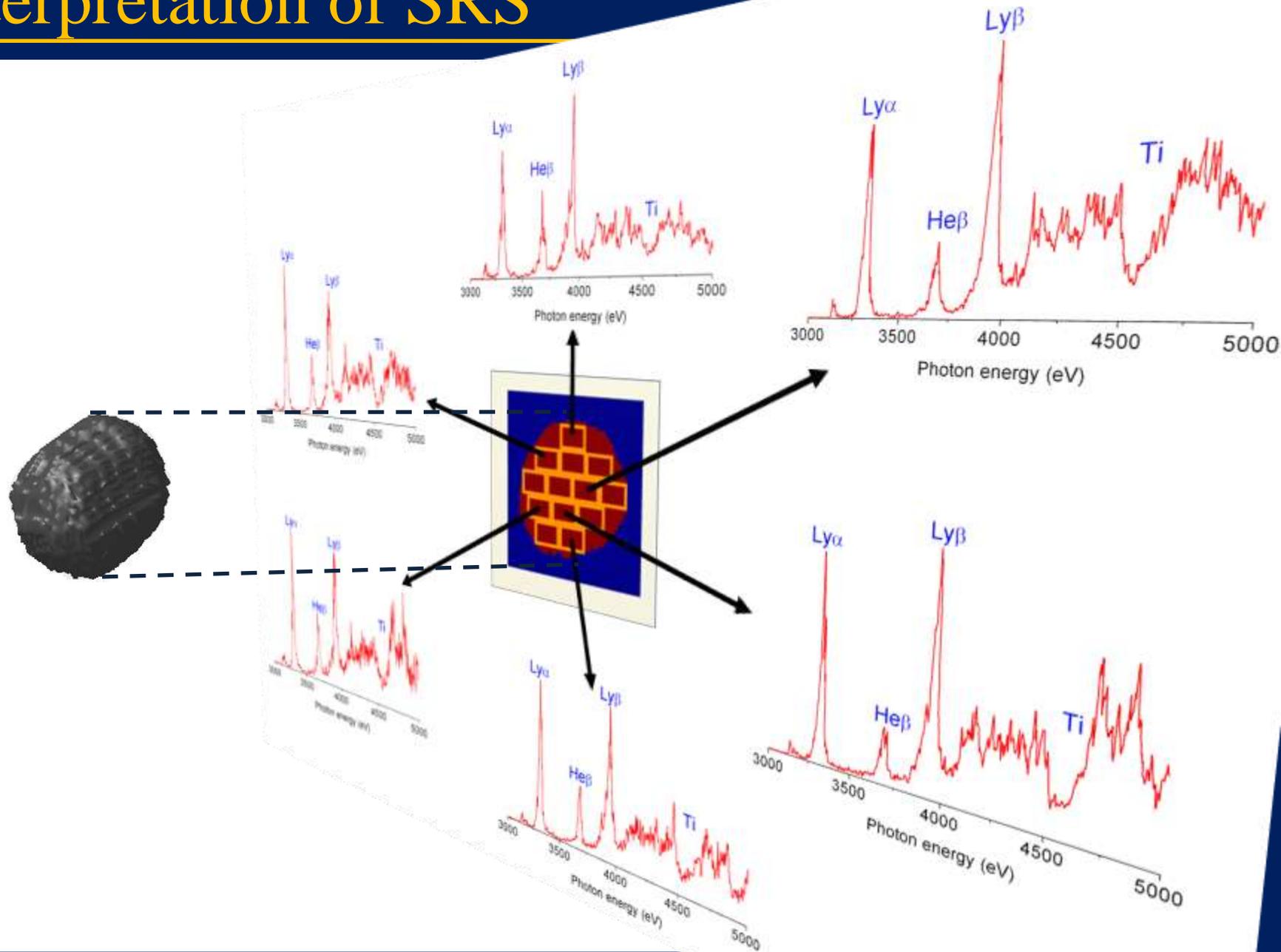
Mask of selected region



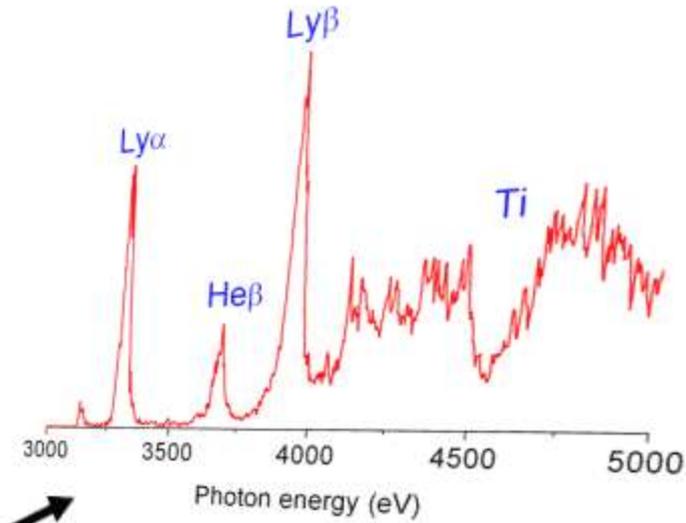
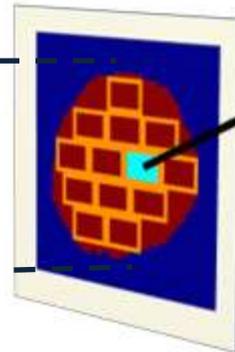
Limitations:

- Signal-to-noise ratio
- Spatial resolution

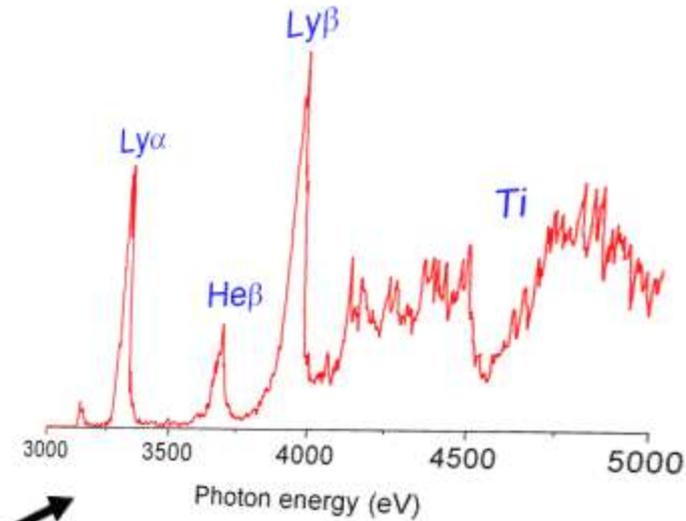
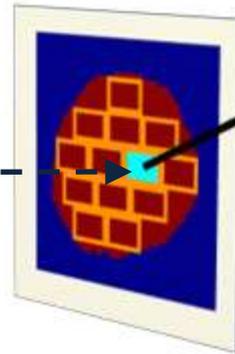
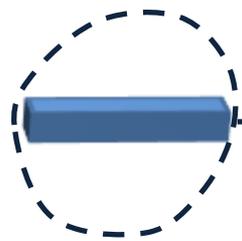
Interpretation of SRS



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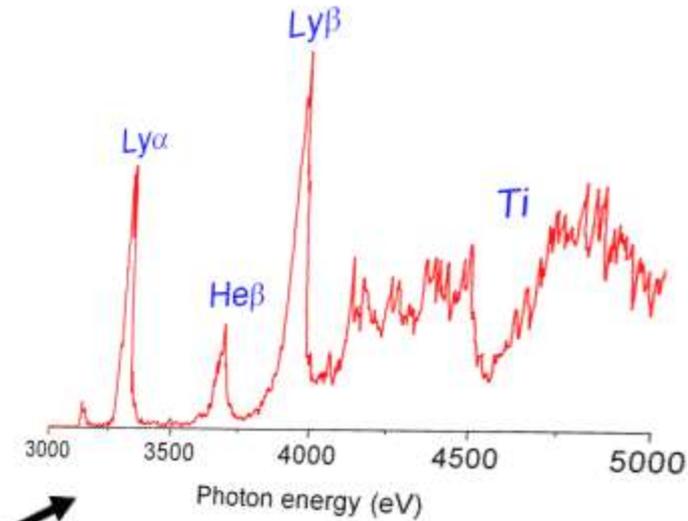
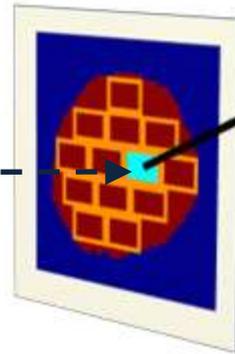
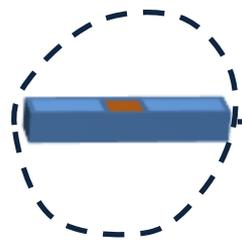


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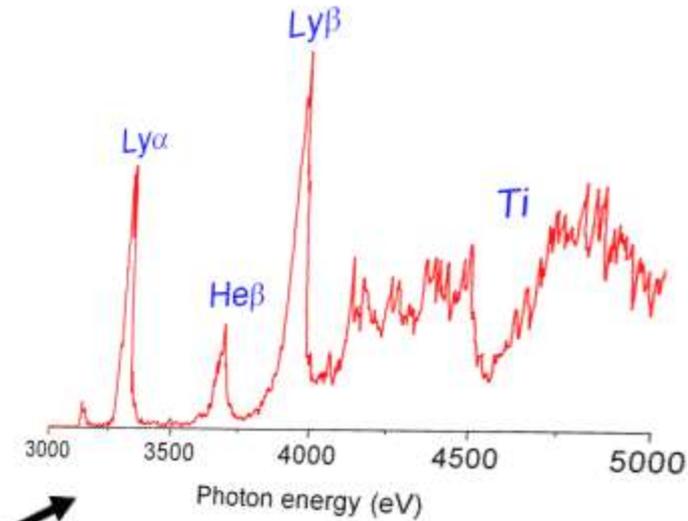
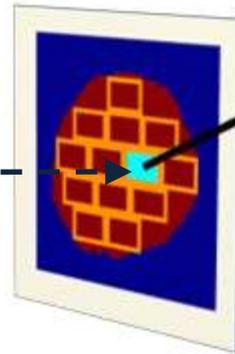
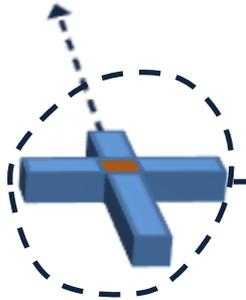
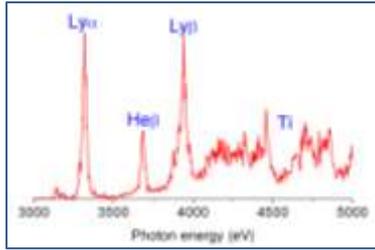
- Each space-resolved spectrum has temperature and density information integrated along chord parallel to LOS and perpendicular to the image plane

Interpretation of SRS



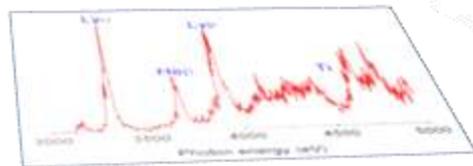
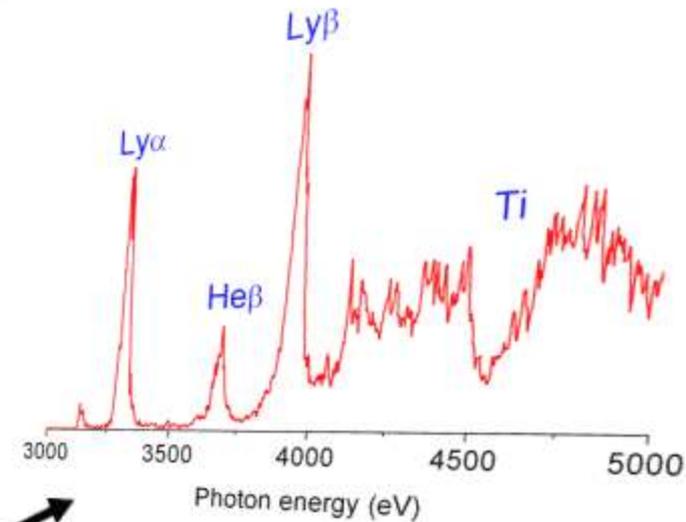
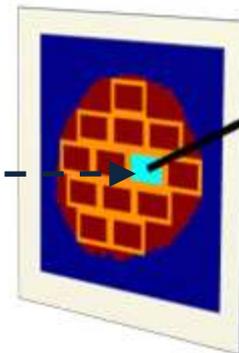
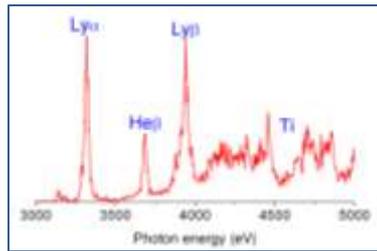
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Interpretation of SRS



- Each space-resolved spectrum has temperature and density information integrated along chord parallel to LOS and perpendicular to the image plane
- Each spatial region is located at the intersection of three chords
- Spatial regions are constrained by their contributions to spatially-resolved spectra recorded along three LOS

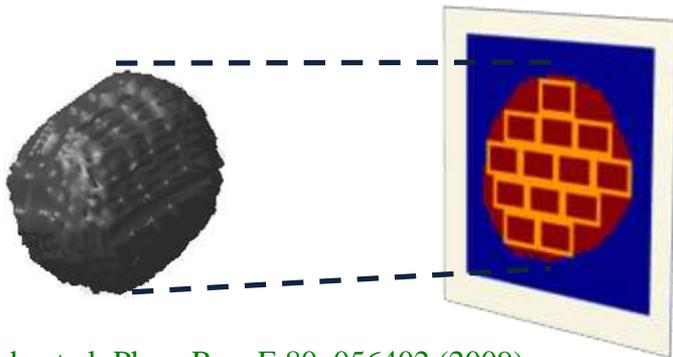
3 LOS, but multiple λ



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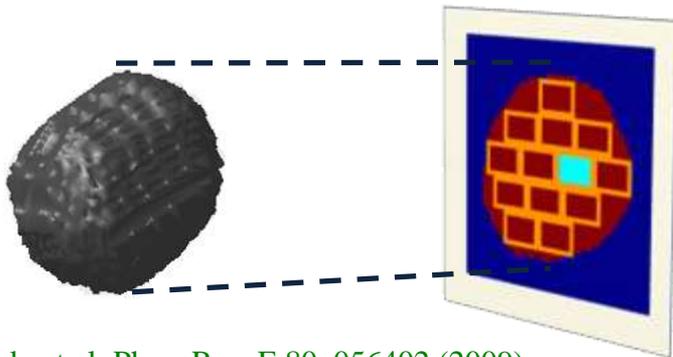
Modeling

- Physics model: T_e and $N_e \rightarrow$ SRS
 1. Detailed collisional-radiative atomic kinetics model
 2. Numerical integration of the radiation transport equation
- Search and reconstruction + model: SRS $\rightarrow T_e$ and N_e
 1. Pareto genetic algorithm (PGA)
 - Fast and robust search algorithm
 - Initialized by random number generator \rightarrow unbiased
 2. Fine-tuning step
 - Least-squares minimization method
 - Refine the PGA results to the very best



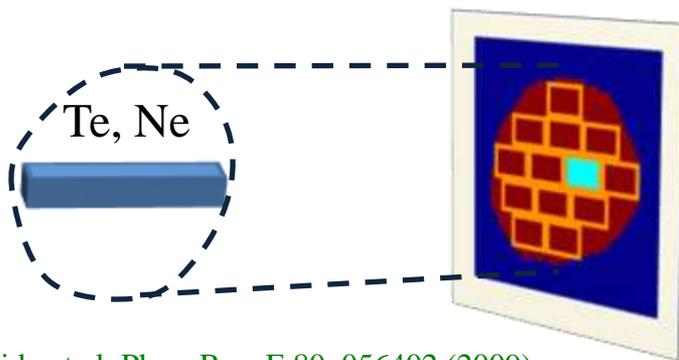
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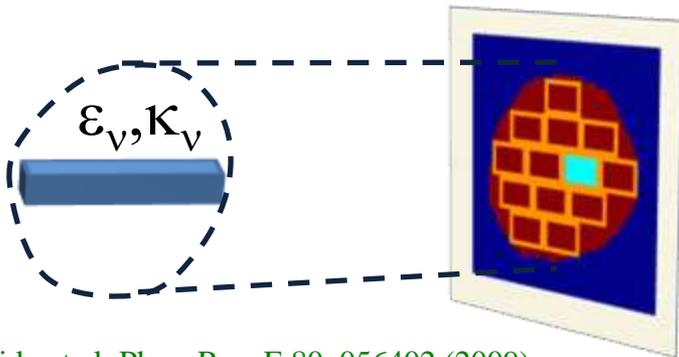
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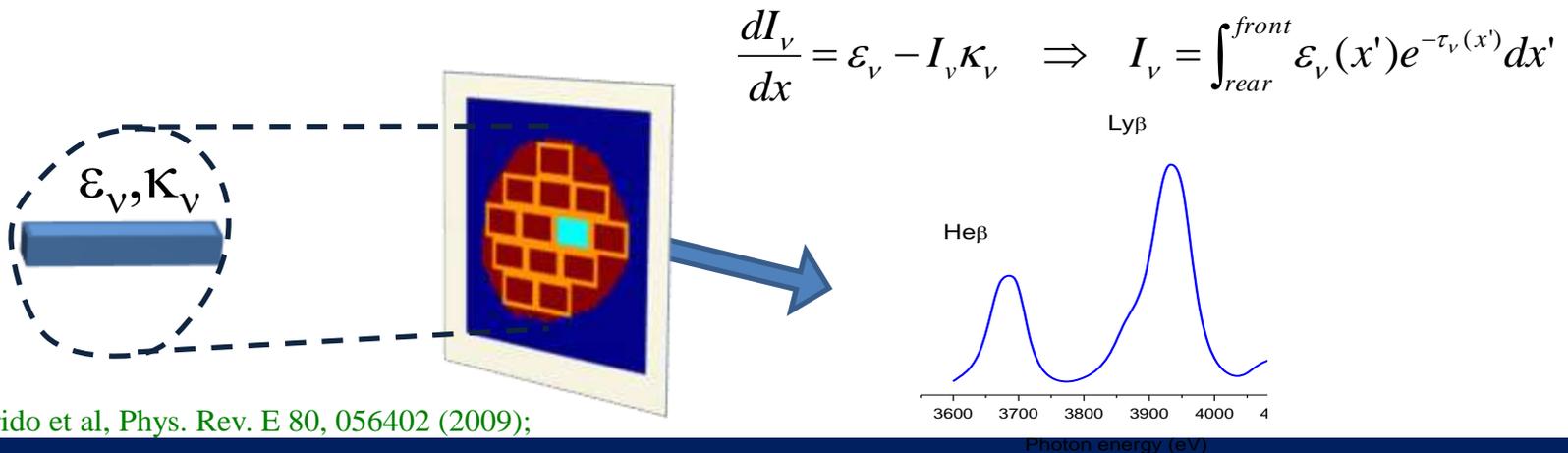
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$$\frac{dI_\nu}{dx} = \epsilon_\nu - I_\nu \kappa_\nu \quad \Rightarrow \quad I_\nu = \int_{rear}^{front} \epsilon_\nu(x') e^{-\tau_\nu(x')} dx'$$

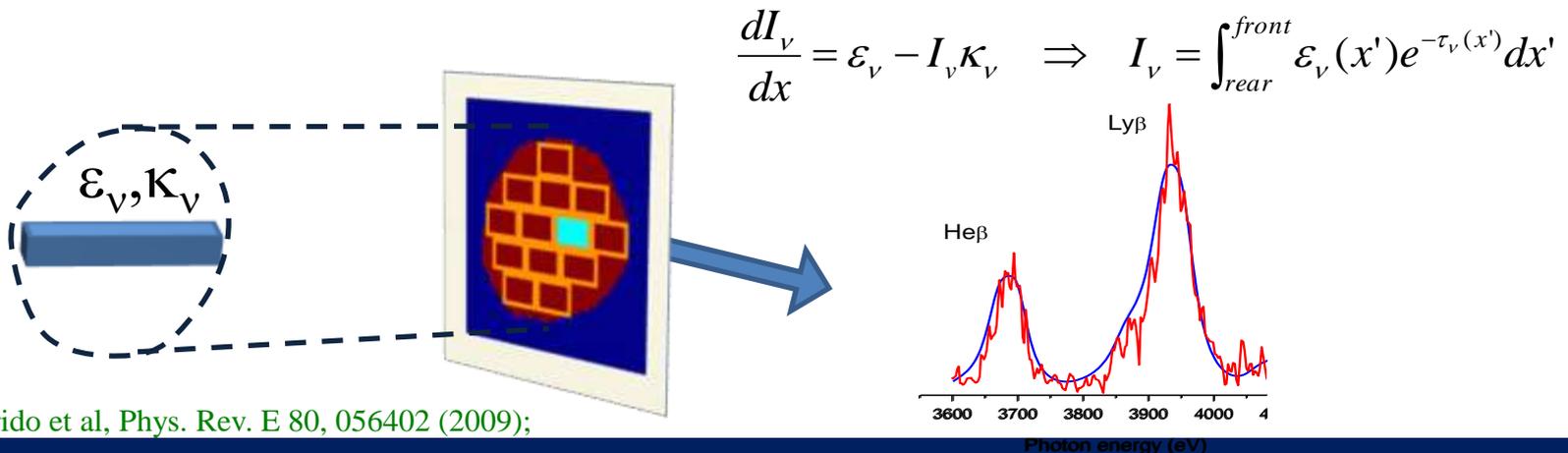
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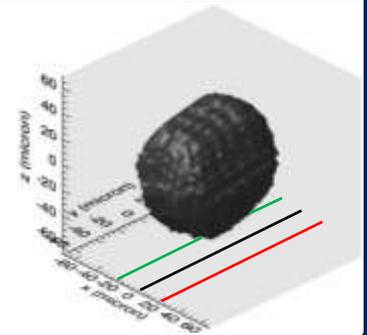
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* R. Florido et al, Phys. Rev. E 80, 056402 (2009);

Results: OMEGA shot 49956 frame 3

- A total of 141 SRS were used to extract T_e and N_e spatial structure
- T_e tends to be larger in central region N_e in the periphery
- 3D asymmetries in the spatial structures are observed

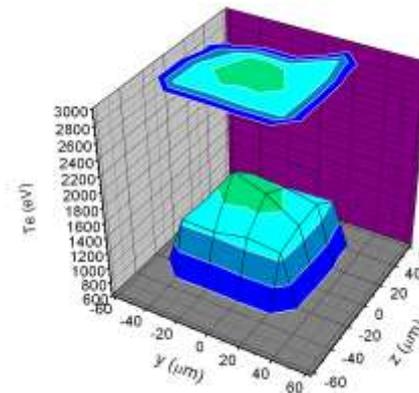
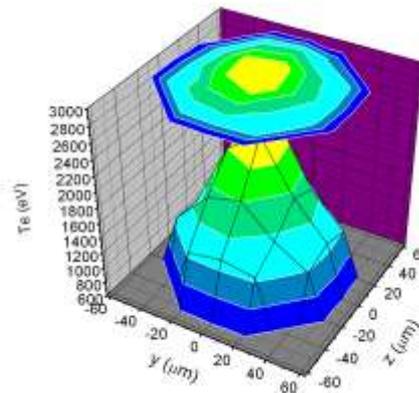
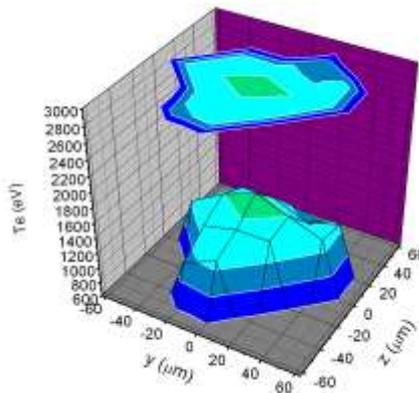


$x = -21 \mu\text{m}$

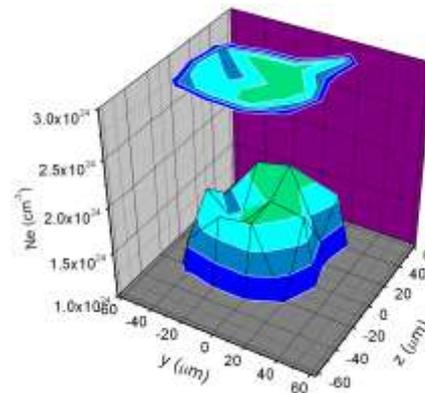
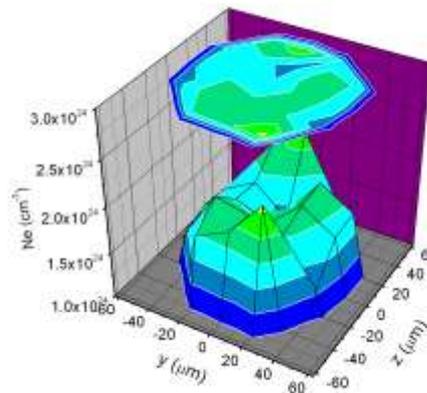
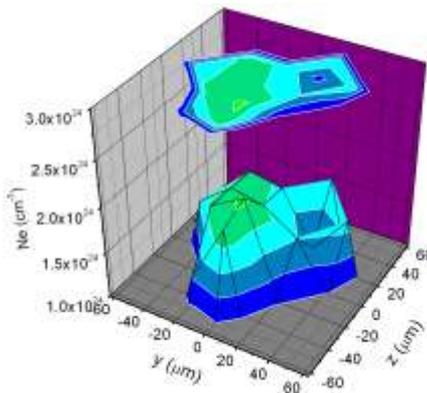
$x = 0 \mu\text{m}$

$x = 21 \mu\text{m}$

T_e (eV)

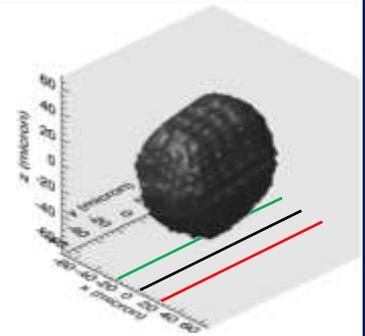


N_e (cm^{-3})



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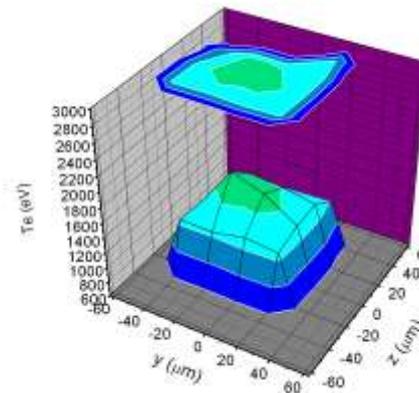
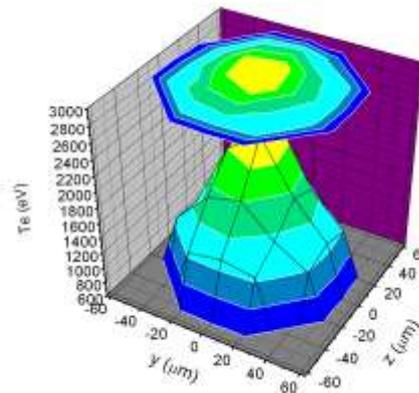
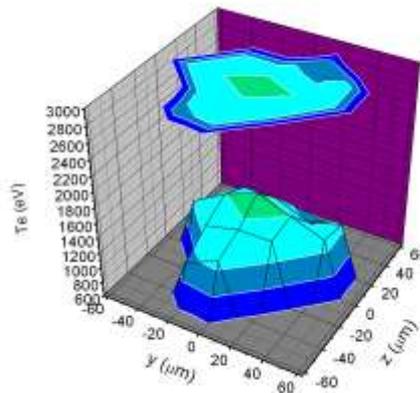


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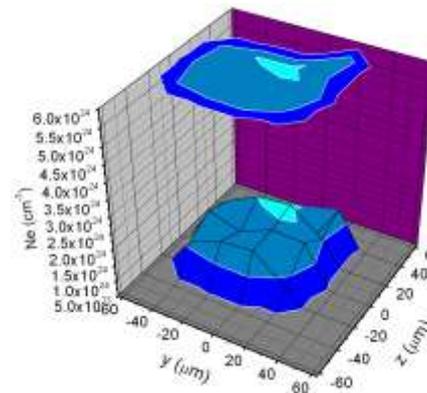
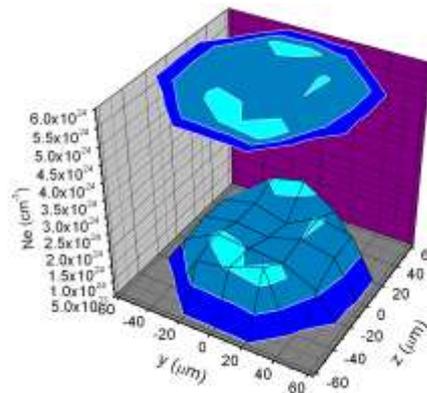
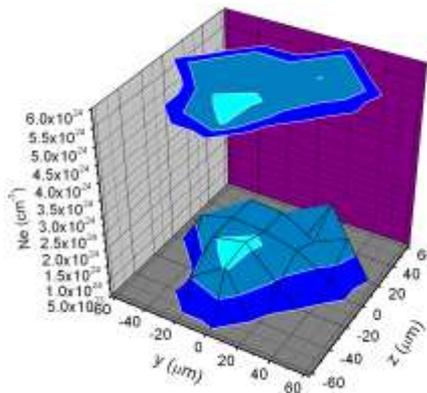
$x = 0 \mu\text{m}$

$x = 21 \mu\text{m}$

T_e (eV)

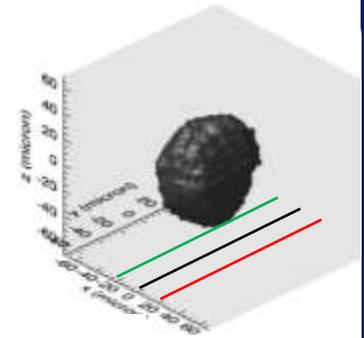


N_e (cm^{-3})



Results: OMEGA shot 49956 frame 4

- A total of 85 SRS were used to extract T_e and N_e spatial structure
- Frame 4 is close to stagnation and the volume is smaller
- Ne has increased while T_e has decreased

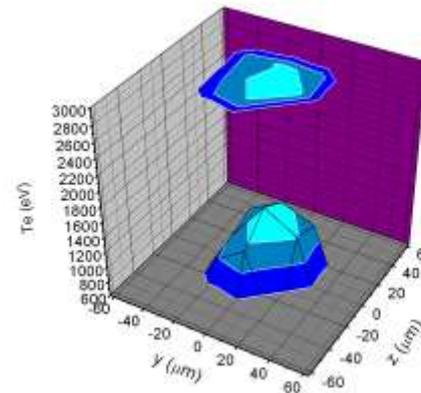
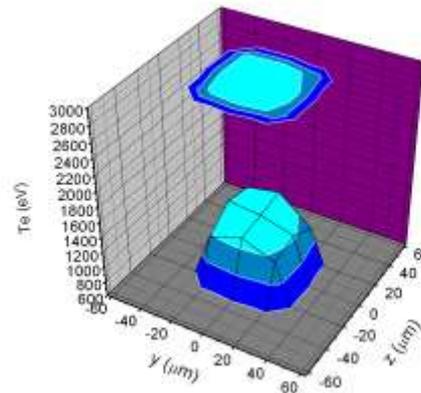
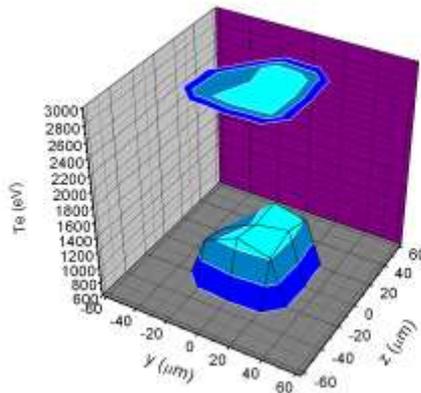


x = -21 μm

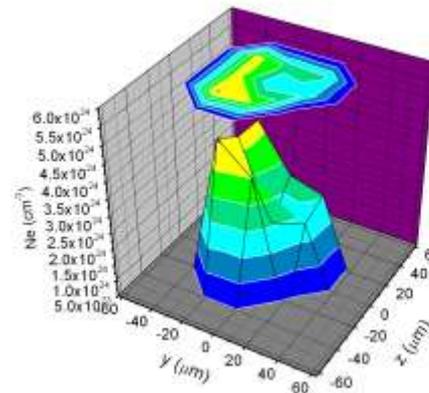
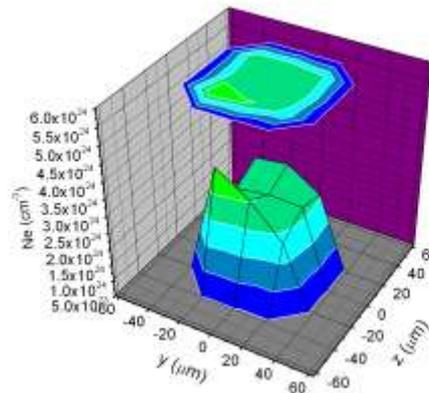
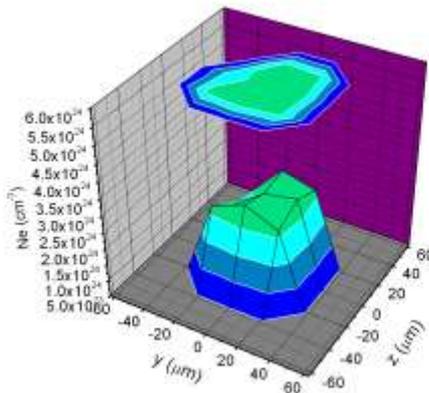
x = 0 μm

x = 21 μm

Te (eV)



Ne (cm^{-3})



Results: OMEGA shot 49956 (Pe evolution)

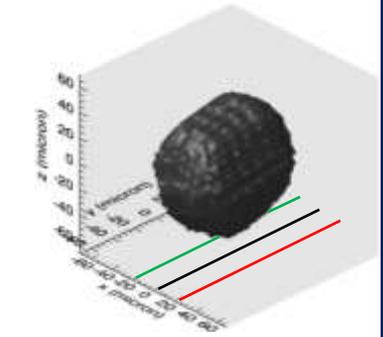
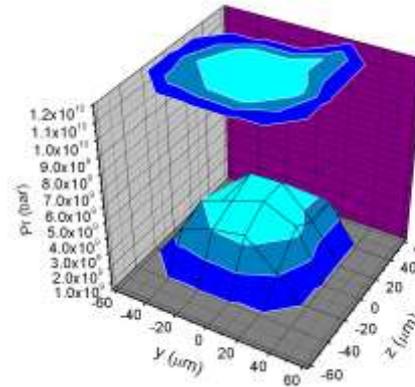
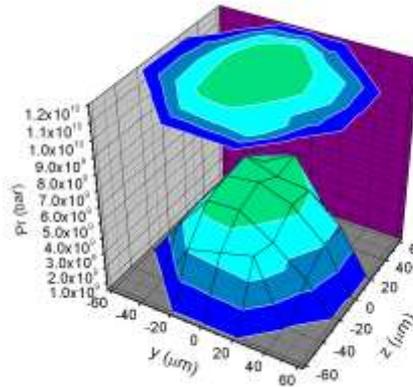
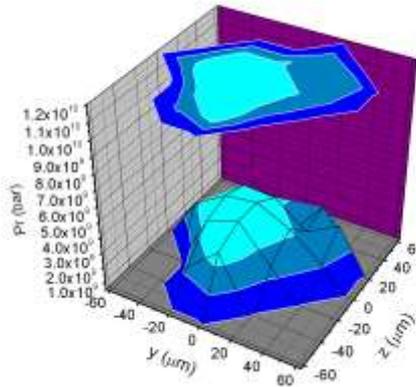
- Pressure distribution is computed based on the Te and Ne distributions
- Frame 3 shows larger gradient in the pressure distribution than Frame 4
- As imploded, the core becomes more isobaric

x = -21 μm

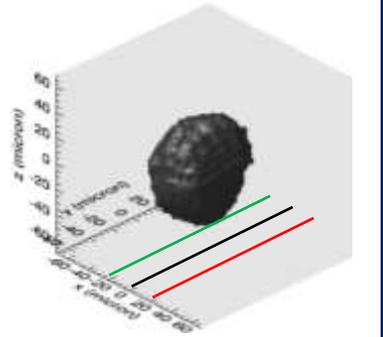
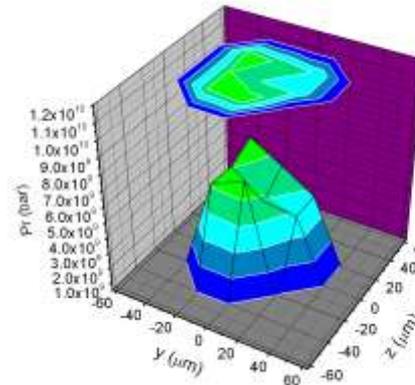
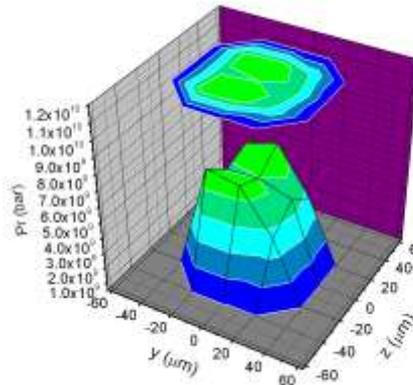
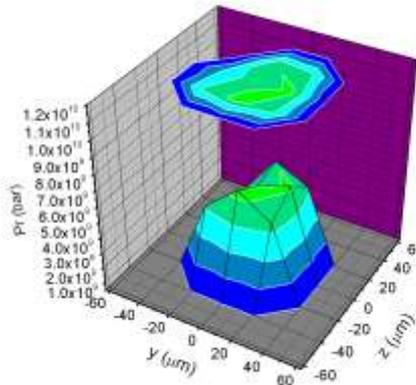
x = 0 μm

x = 21 μm

Frame 3



Frame 4



Conclusions

- T_e and N_e spatial distributions have been extracted from the analysis of space-resolved spectra (SRS) obtained from spectrally-resolved images recorded with three-identical DDMMI instruments fielded along quasi-orthogonal directions
- Analysis method:
 - Two step search and reconstruction: PGA followed up by fine-tuning
 - Method was tested with the synthetic test case
 - This method can be interpreted as polychromatic tomography; number of LOS is limited but there are multiple wavelengths associated with each LOS
- Work in progress:
 - Extract mixing distribution
 - Error estimation
 - Further synthetic data test cases
 - Comparison with 2D/3D hydrodynamics simulation

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