



Laboratory for Laser Energetics (LLE)
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FROM LASERS TO THE UNIVERSE: SCALING LAWS in LABORATORY ASTROPHYSICS

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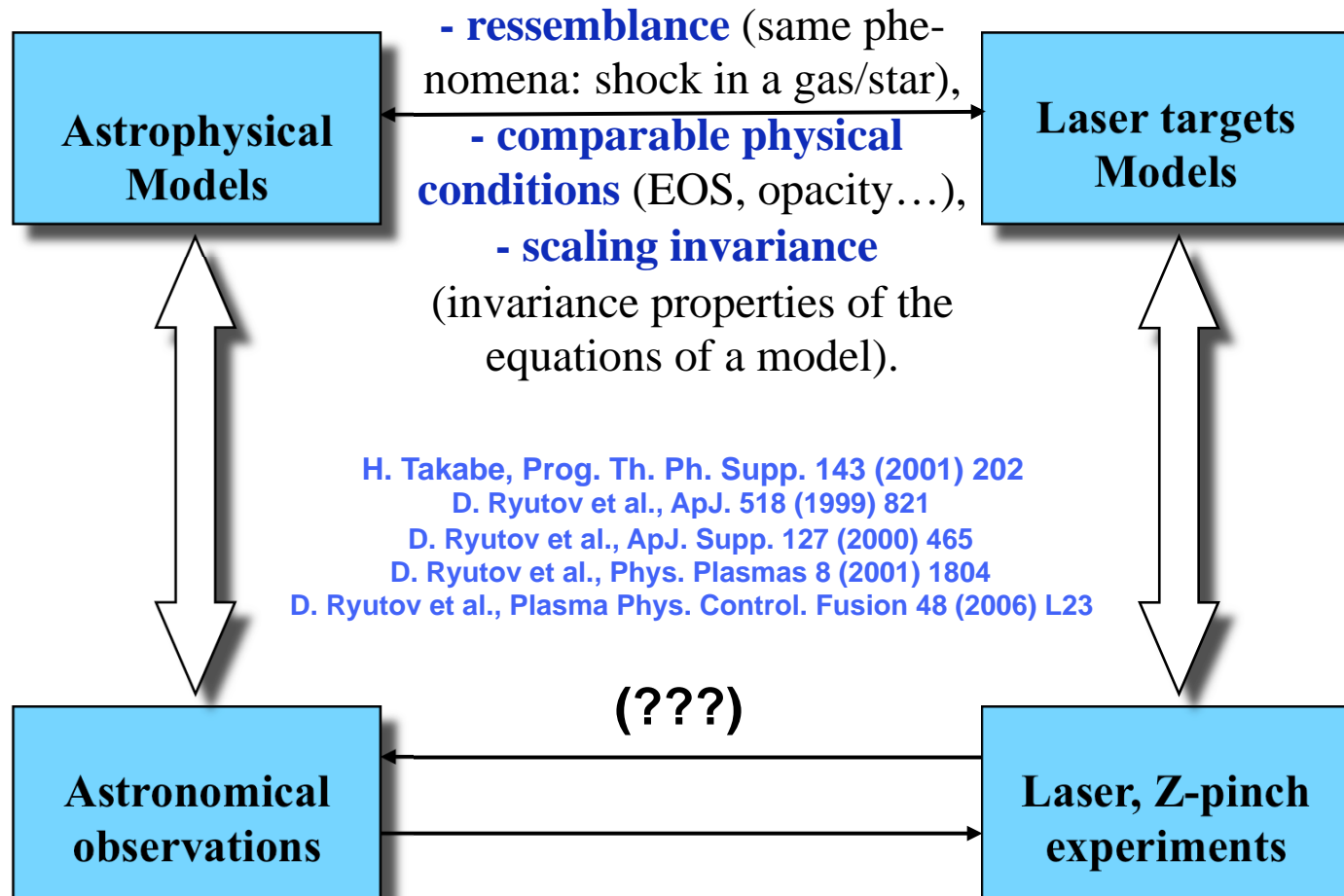


OUTLINE

- 1) - CLASSICAL SCALING LAWS**
- 2) - RIGOUROUS FORMALISM**
- 3) - YOUNG STELLAR OBJECT (YSO) JETS**
- 4) - RADIATIVE SHOCKS**
- 5) - CONCLUSION**



LASER EXP. vs. ASTRON. OBS.

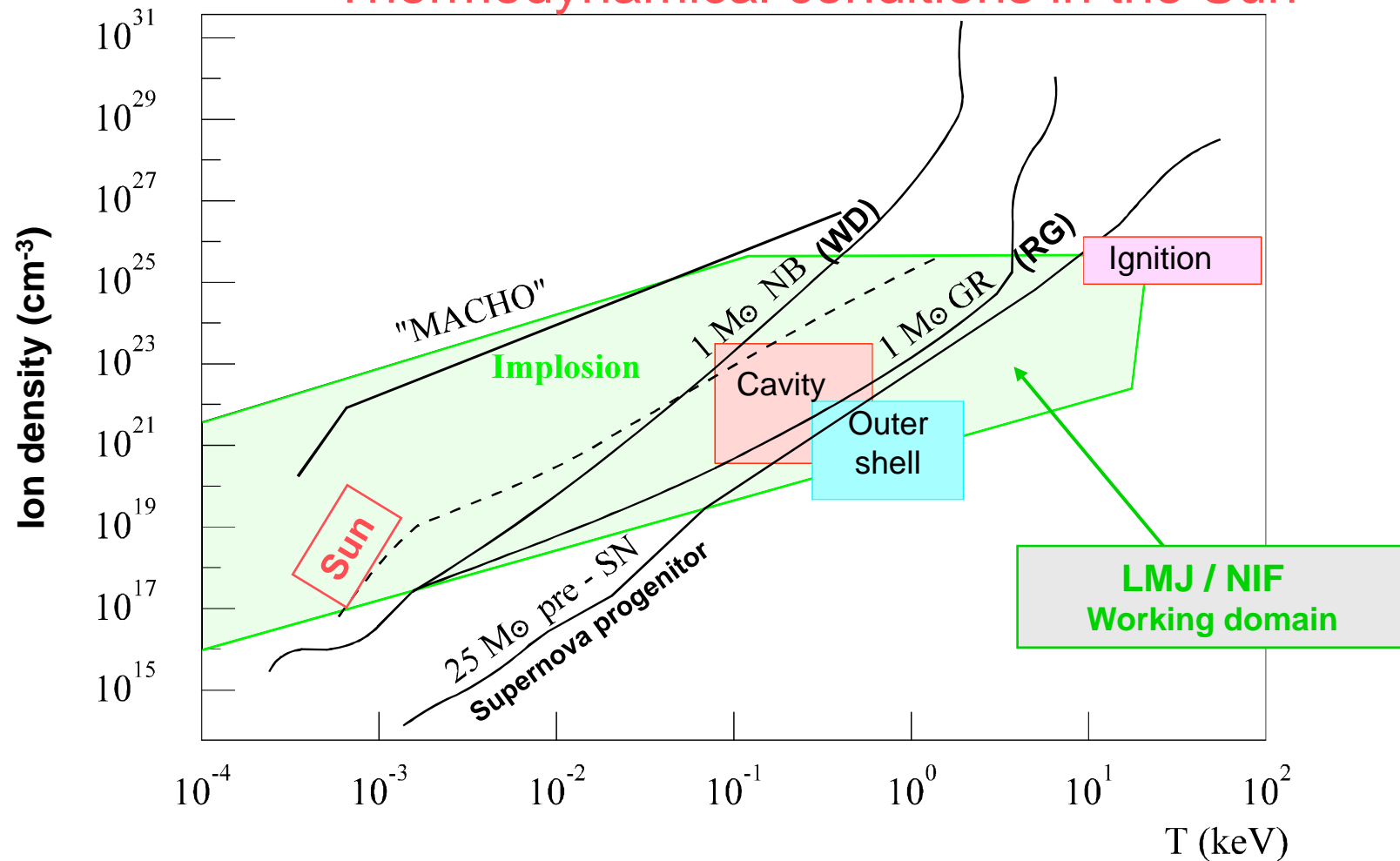


**CONNECTION BETWEEN LASER EXPERIMENTS
AND ASTRONOMICAL OBSERVATIONS**

ASTRONOMICAL OBJECTS and LASER PLASMAS

Fig. from J.-P. Chièze

Comparable physical conditions:
Thermodynamical conditions in the Sun



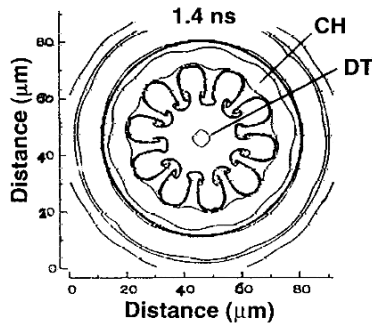


FCI TARGET vs. SUPERNOVA

Dimensionless number : Rayleigh - Taylor instabilities

Typical quantities for laser target (S1) and supernovae (S2)

Imploding laser target (ICF)



Physical quantities	Laser target (S1)	Supernova (S2)
Characteristic length	$l_1 \approx 100 \mu\text{m} \approx 10^{-2} \text{ cm}$	$l_2 \approx 10^{12} \text{ cm}$
Characteristic time	$\tau_1 \approx 10^{-9} \text{ s}$	$\tau_2 \approx 1000 \text{ s}$
Characteristic velocity	$V_1 \approx 10^7 \text{ cm/s}$	$V_2 \approx c/10 \approx 10^9 \text{ cm/s}$
Characteristic acceleration	$g_1 \approx 10^{16} \text{ cm/s}^2$	$g_2 \approx 10^6 \text{ cm/s}^2$

The acceleration of supernovae is very weak !!!

Characteristics of the Rayleigh-Taylor Instability (RTI) :

$$\text{Instability growth rate: } \alpha_{\text{IRT}, i} \approx \sqrt{g_i / l_i}$$

We should compare $\alpha_{\text{IRT}, i}$ to the proper time τ_i of the system S_i

Physical quantities	S1 (target)	S2 (supernova)
Instability rate α_{IRT}	$\alpha_{\text{IRT},1} \approx 10^9 \text{ s}^{-1}$	$\alpha_{\text{IRT},2} \approx 10^{-3} \text{ s}^{-1}$
Dimensionless numb. N_{IRT}	$N_{\text{IRT},1} \approx 1$	$N_{\text{IRT},2} \approx 1$

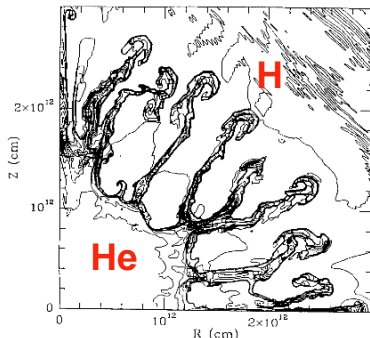
THE DIMENSIONLESS NUMBER N_{IRT} IS GIVEN BY THE PRODUCT $N_{\text{IRT}} = \alpha_{\text{IRT}} \cdot \tau$ FOR EACH SYSTEM

$$N_{\text{IRT}}(\text{target}) = N_{\text{IRT}}(\text{supernova}) !!!$$

and the common value is about 1

The physics of both objects is similar

Exploding star : supernova



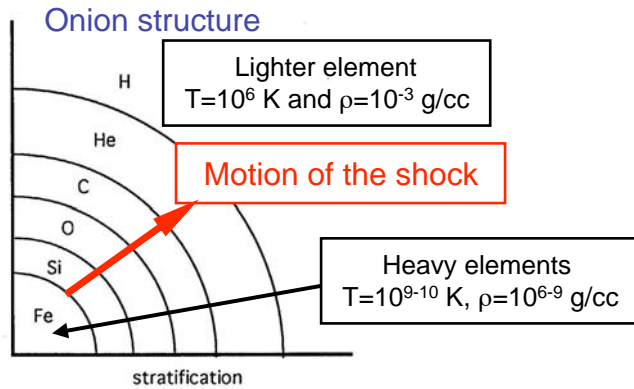
Among the most violent phenomena in the universe !!!



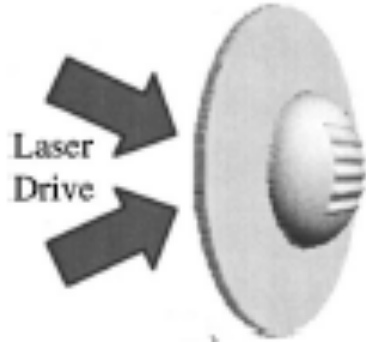
SUPERNOVA SN87A: SIMULATION vs EXPERIMENT

Scaling laws : Rayleigh - Taylor instabilities

EXPERIMENTS from DRAKE's GROUP :



Robey et al., Phys. Plasmas 8 (2001) 2448



Length: $100 \mu\text{m} \leftrightarrow 10^{11} \text{cm}$

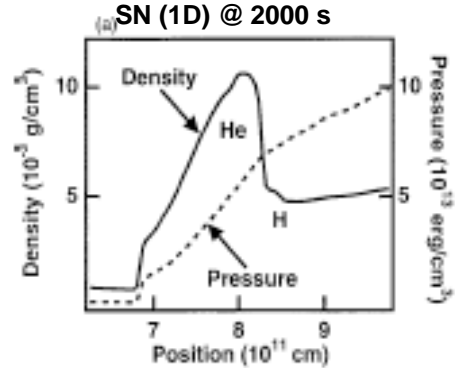
and

Time: $20 \text{ns} \leftrightarrow 2000 \text{s}$

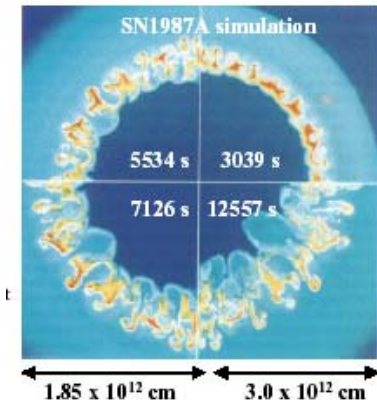
Therefore:

Velocity: $100 \text{km/s} \leftrightarrow 10\,000 \text{km/s}$

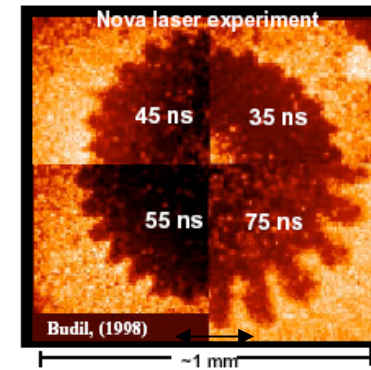
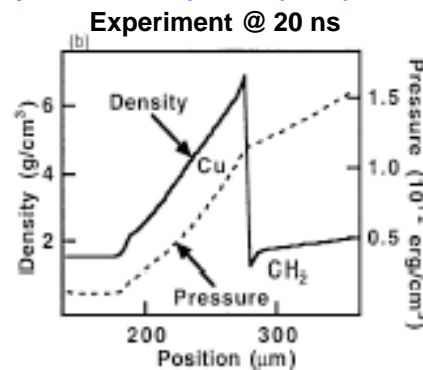
Ryutov et al., Phys. Plasmas 8 (2001) 1804



Muller et al., Astron. Astrophys. 251 (1991) 505



Ryutov et al., ApJ 518 (1999) 821



10 000 km/s is relevant for SN remnants
100 km/s is relevant for laser targets

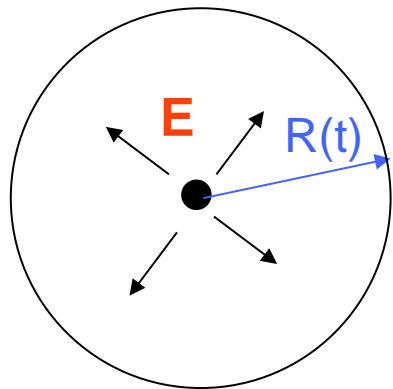
J. Kane et al., Phys. Plasmas 6 (1999) 2065



STRONG EXPLOSION, DIMENSIONLESS NUMBER and SELF-SIMILAR SOLUTION

Strong point explosion with energy E in an ambient medium of uniform density ρ_0

Fireball



Time position of the shock, $R(t)$???

Use of Dimensional analysis

Unit of mass: M
Unit of length: L
Unit of time: T

$[E] = M.L^2.T^{-2}$
 $[\rho_0] = M.L^{-3}$
 $[R] = L$

density ρ_0

Ratio $E/\rho_0 \sim L^5.T^{-2}$

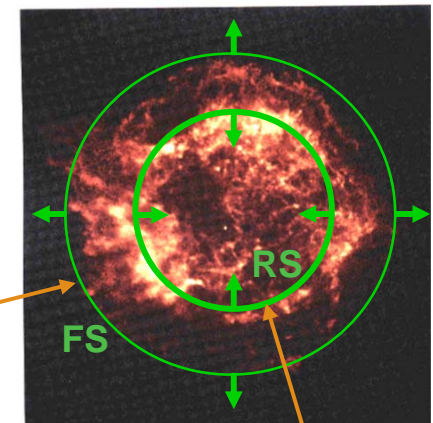
→ M disappears

Product $(E/\rho_0).t^2 \sim L^5$

→ M and T disappear

Time t is inserted !!! Nice !!!

Cassiopee A (1680)
Type Ia SN



Forward shock

Reverse shock

CONCLUSION : $(E/\rho_0).t^2 / [R(t)]^5 \sim \xi$: Dimensionless Number

and $R(t) \sim (E/\rho_0)^{1/5} .t^{2/5}$ Sedov - Taylor law

$R(t) \sim t^\alpha$: SELF-SIMILAR EVOLUTION



SEDOV - TAYLOR SOLUTION

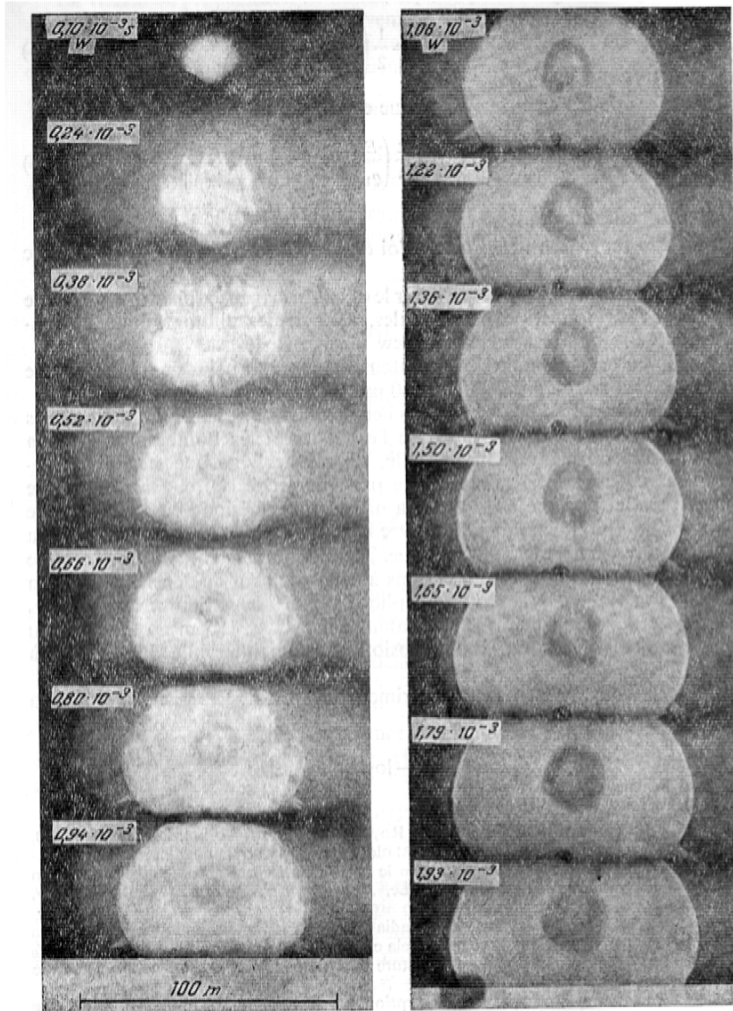


Fig. 67. Photographies d'une boule de feu prise dans l'intervalle de $t=0,1 \cdot 10^{-3}$ à $t=1,93 \cdot 10^{-3}$ s lors de l'explosion de la bombe atomique à New Mexico

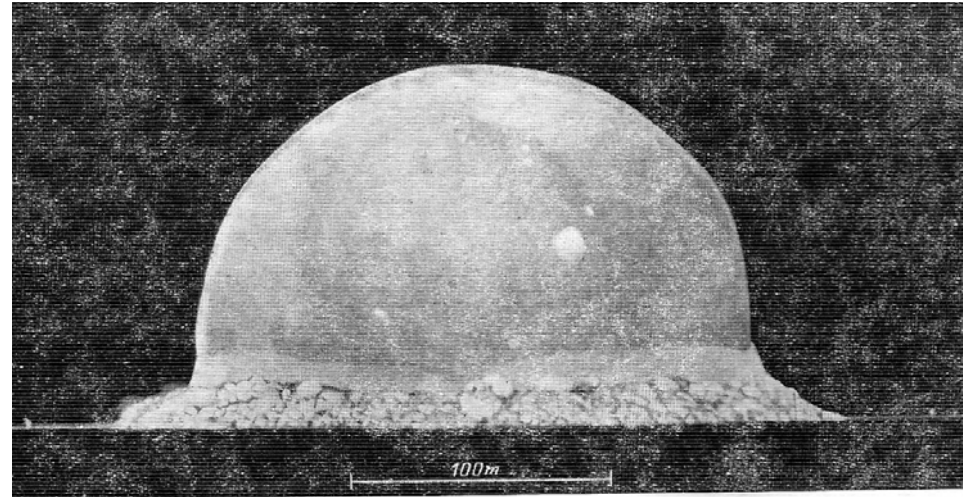
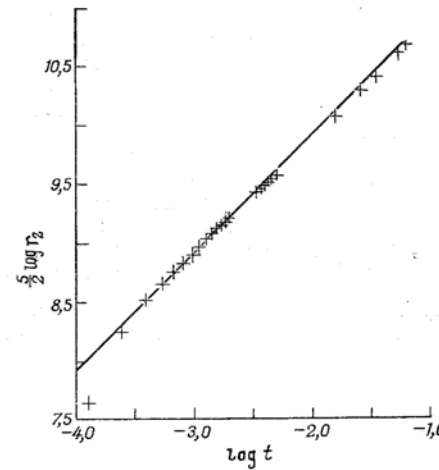


Fig. 68. Boule de feu à l'instant $t=15 \cdot 10^{-3}$ s

Measurements Vs. Theory



$$R(t) \sim t^{2/5}$$

Self-Similar Solution (SSS)

- Fireball:
 $R \sim 100 \text{ m} \sim 10^4 \text{ cm}$
- Supernova remnant:
 $R \sim 1 \text{ pc} \sim 3 \cdot 10^{18} \text{ cm}$

SAME BEHAVIOUR



INVARIANCE - SCALING LAWS

Model equation: Non-linear heat equation

$$\frac{\partial T}{\partial t} = D \cdot \frac{\partial^2 T^n}{\partial x^2}$$

T: temperature (D: diffusion coefficient = cst.)

Solution: $T = S(x,t)$ where S is a known function

INVARIANCE under the transformation: λ_x , λ_t and λ_T : Scaling parameters

D. Ryutov et al., ApJ 518 (1999) 821

Independent variables: x and t

$$x = \lambda_x \cdot \bar{x}, \quad t = \lambda_t \cdot \bar{t}$$

Dependent variable: T(x,t)

$$T = \lambda_T \cdot \bar{T}$$

$$\frac{\lambda_T}{\lambda_t} \cdot \frac{\partial \bar{T}}{\partial \bar{t}} = \frac{(\lambda_T)^n}{(\lambda_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$$

$$\frac{\partial \bar{T}}{\partial \bar{t}} = \frac{\lambda_T \cdot (\lambda_T)^{n-1}}{(\lambda_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$$

$\frac{\partial \bar{T}}{\partial \bar{t}} = D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$	$\frac{\lambda_T \cdot (\lambda_T)^{n-1}}{(\lambda_x)^2} = 1$
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The equation is **invariant** under the transformation

Solution: $\bar{T} = \bar{S}(\bar{x}, \bar{t})$ but $\bar{S} = S$

λ_x and λ_t are arbitrary !

$$\lambda_T = [(\lambda_x)^2 / (\lambda_t)]^{1/(n-1)}$$

The solution is **invariant**

The solutions are **the same** at **both scales**

Two free parameters (!!!) to make the 2 systems homothetic



LIE GROUP VIEW POINT

The equation $\frac{\partial T}{\partial t} = D \cdot \frac{\partial^2 T^n}{\partial x^2}$ is invariant under the transformation:

$x = \lambda_x \cdot \bar{x}$, $t = \lambda_t \cdot \bar{t}$, $T = \lambda_T \cdot \bar{T}$ provided the relation $\lambda_T = [(\lambda_x)^2 / (\lambda_t)]^{1/(n-1)}$ holds.

$$\frac{T \cdot t^{1/(n-1)}}{(x^2)^{1/(n-1)}} = \frac{\bar{T} \cdot \bar{t}^{1/(n-1)}}{(\bar{x}^2)^{1/(n-1)}} = I = \text{INVARIANT of the transformation}$$

It is not a dimensionless number !

Relation between the quantities of the 2 systems

Combine x and t: **S.S.S** are obtained

$$\frac{\lambda_t \cdot (\lambda_T)^{n-1}}{(\lambda_x)^2} = 1$$

λ_x , λ_t and λ_T : Scaling parameters

$$x = a^{\delta_1} \bar{x} ; t = a^{\delta_2} \bar{t} \text{ and } T = a^{\delta_3} \bar{T} \quad (a: \text{group parameter})$$

$$\frac{a^{\delta_2} \cdot (a^{\delta_3})^{n-1}}{(a^{\delta_1})^2} = 1 \Leftrightarrow \delta_2 + (n-1)\delta_3 - 2\delta_1 = 0$$

Two free parameters !

The constraint is a linear equation between the δ_i 's

SYSTEMATIC AND RIGOUROUS APPROACH BASED ON LIE GROUP SYMMETRIES

Dimensionless numbers, invariants, S.S.S's, EDP's become EDO's, analytical solutions ...



BROKEN SYMMETRY

Add a linear term (still very simple equation !)

$$\frac{\partial T}{\partial t} = D \cdot \frac{\partial^2 T^n}{\partial x^2} + T$$

$$\frac{\lambda_T}{\lambda_t} \cdot \frac{\partial \bar{T}}{\partial \bar{t}} = \frac{(\lambda_T)^n}{(\lambda_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2} + \lambda_T \cdot \bar{T}$$

$$\frac{\partial \bar{T}}{\partial \bar{t}} = \frac{\lambda_t \cdot (\lambda_T)^{n-1}}{(\lambda_x)^2} \cdot D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2} + \lambda_T \cdot \bar{T}$$

Independent variables: x and t

$$x = \lambda_x \cdot \bar{x} \quad , \quad t = \lambda_t \cdot \bar{t}$$

Dependent variable: T

$$T = \lambda_T \cdot \bar{T}$$

$\lambda_t = 1$: **no scaling for time**
One symmetry is lost

$$\frac{\lambda_t \cdot (\lambda_T)^{n-1}}{(\lambda_x)^2} = 1$$

becomes

$$\lambda_T = (\lambda_x)^{2/(n-1)}$$

$$\frac{\partial \bar{T}}{\partial \bar{t}} = D \cdot \frac{\partial^2 \bar{T}^n}{\partial \bar{x}^2}$$

The equation is **invariant** under the transformation

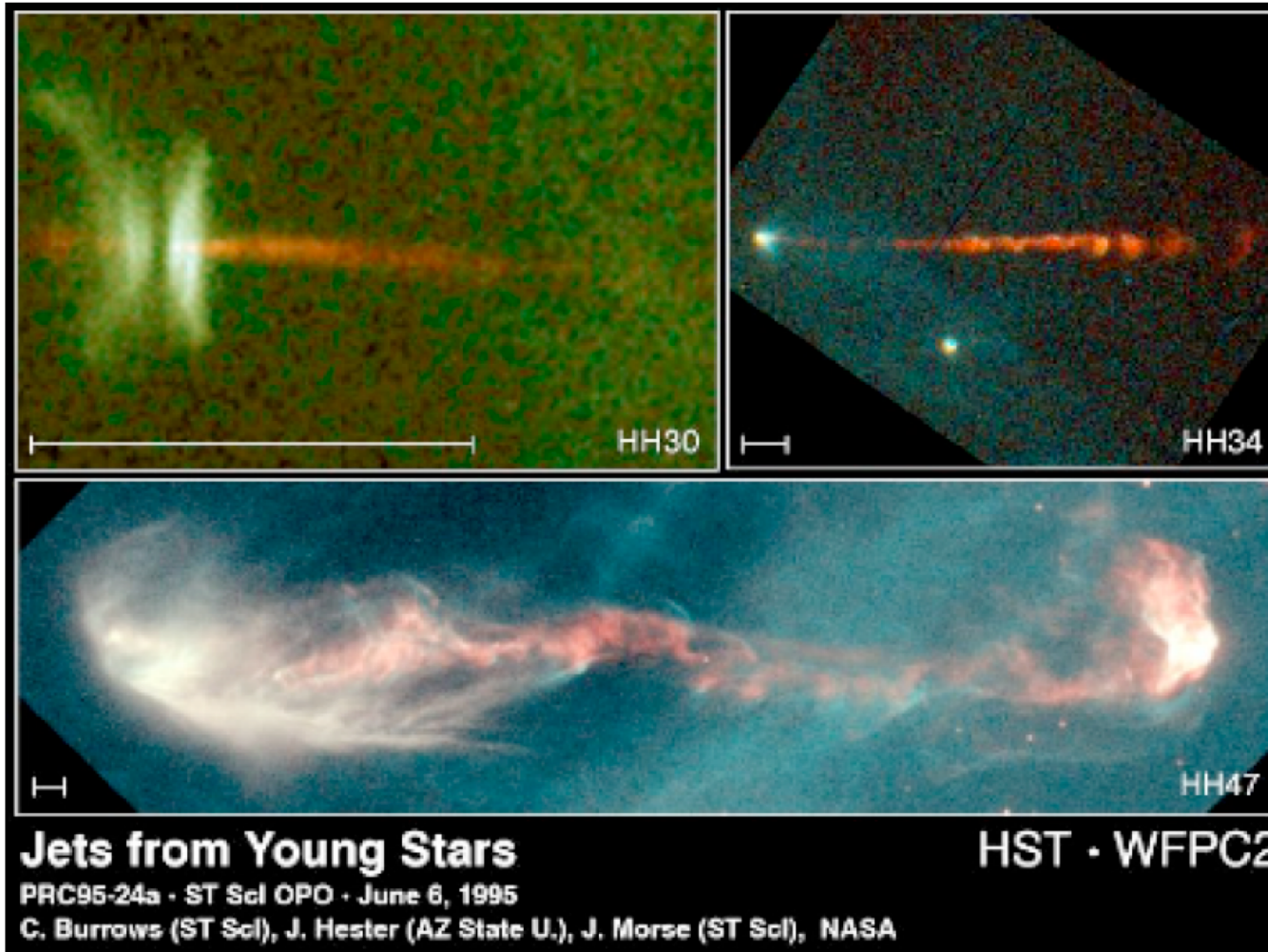
$$\text{Solution: } \bar{T} = \bar{S}(\bar{x}, \bar{t}) \quad \text{but} \quad \bar{S} = S !$$

The solution is **invariant** but with **a single time** ($t = \bar{t}$) !

Too much terms or too much equations : **no symmetry at all**

CEA YOUNG STELLAR OBJECTS JETS

Herbig - Haro Objects



Unit : 1 000 au
(1 au = $1.5 \cdot 10^{13}$ cm
et 1 pc = $2 \cdot 10^5$ au)

Length from
1 000 au
to
0.1 pc

Differences
in the structure



INVARIANCE OF RADIATION HYDRODYNAMICS ?

Optically thin radiation hydrodynamics

- $\frac{\partial \rho}{\partial t} + \vec{\nabla}_N \cdot [\rho \vec{v}] = 0$ (N=0: plane, N=1: cylindrical, N=2: spherical geometry)
- $\left[\frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \vec{v} = -\frac{1}{\rho} \vec{\nabla} P$
- $\left[\frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] P - \gamma \frac{P}{\rho} \left[\frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \rho = -(\gamma - 1) \Lambda(\rho, P)$

$\Lambda(\rho, P)$ = cooling function

$$\Lambda(\rho, P) = \Lambda_0 \rho^\varepsilon P^\zeta$$

$$\Lambda(\rho, P) \rightarrow \Lambda(\rho, T) \quad P = \varepsilon_0 [Z] \rho^\mu T^\nu$$

$\Lambda_0 = \text{constant}$
 Power law form
 Exponents ε and ζ

Invariance ?

$$\begin{aligned}
 x &= a^{\delta_1} \tilde{x}; & t &= a^{\delta_2} \tilde{t}; & \rho &= a^{\delta_3} \tilde{\rho}; & v &= a^{\delta_4} \tilde{v}; \\
 P &= a^{\delta_5} \tilde{P}; & T &= a^{\delta_6} \tilde{T}; & M &= a^{\delta_7} \tilde{M}; & \gamma &= a^{\delta_8} \tilde{\gamma}; & \varepsilon_0 &= a^{\delta_9} \tilde{\varepsilon}_0; & \Lambda &= a^{\delta_{10}} \tilde{\Lambda}
 \end{aligned}$$

« upper tilde » instead of an « upper bar » (\tilde{x} !!!)

Solve a linear system of equations for the δ_i 's

Yes !



SCALING LAWS

$$x = \lambda_x \cdot \bar{x} \rightarrow q = \lambda_q \cdot \bar{q} \rightarrow q = \lambda_q \cdot \tilde{q} \quad \text{and} \quad \lambda_i \equiv a^{\delta_i} \quad i = r, t, v, \dots = 1, 2, 3, \dots$$

a: Group parameter

Ratios	General laws	A single cooling ϵ_1 and ζ_1	Bremsstrahlung
x/\bar{x}	a^{δ_1}	$a^{(3/2-\zeta_1)\delta_5 - (\epsilon_1+1/2)\delta_3}$	$a^{\delta_5-2\delta_3} \quad B/A^2$
t/\bar{t}	$a^{\delta_1+(\delta_3-\delta_5)/2}$	$a^{(1-\zeta_1)\delta_5 - \epsilon_1\delta_3}$	$a^{(\delta_5-3\delta_3)/2} \quad (B/A^3)^{1/2}$
$\rho/\bar{\rho}$	a^{δ_3}	a^{δ_3}	$a^{\delta_3} \equiv A$
v/\bar{v}	$a^{(\delta_5-\delta_3)/2}$	$a^{(\delta_5-\delta_3)/2}$	$a^{(\delta_5-\delta_3)/2} \quad (B/A)^{1/2}$
P/\bar{P}	a^{δ_5}	a^{δ_5}	$a^{\delta_5} \equiv B$
T/\bar{T}	$a^{(\delta_5-\delta_3-\mu\delta_1)/\nu}$	$a^{\delta_5-\delta_3}$	$a^{(\delta_5-\delta_3)} \quad B/A$
M/\bar{M}	$a^{\delta_3+N\delta_1}$	$a^{[1-N(\epsilon_1+1/2)]\delta_3+N(3/2-\zeta_1)\delta_5}$	$a^{[1-2N]\delta_3+N\delta_5} \quad A^{(1-2N)} \cdot B^N$ N: dimensionality
s/\bar{s}	$a^{\delta_5-\gamma\delta_3}$	$a^{\delta_5-\gamma\delta_3}$	$a^{\delta_5-\gamma\delta_3} \quad B/A^\gamma$ γ : polytropic constant
$\Lambda_{0,1}/\bar{\Lambda}_{0,1}$	$a^{(3/2-\zeta_1)\delta_5 - (\epsilon_1+1/2)\delta_3 - (\theta_1+1)\delta_1}$	1	1
$\Lambda_{0,2}/\bar{\Lambda}_{0,2}$	$a^{(3/2-\zeta_2)\delta_5 - (\epsilon_2+1/2)\delta_3 - (\theta_2+1)\delta_1}$	0	0

δ_1, δ_3 et δ_5

Three free parameters

δ_3 et δ_5

Two free parameters

δ_3 et δ_5

($\epsilon_1 = 3/2$; $\zeta_1 = 1/2$)

E. Falize et al., Inertial Fusion Sc. Appl. (IFSA07), Kobe, Japan (2007)

E. Falize et al., Journal Physics: Conf. Series 112 (2008) 042015

E. Falize et al., Astrophys. Sp. Sc., to appear (2009)



ASTROPHYSICS and EXPERIMENTS



NASA and B. Reipurth (CASA, Universi

HH 111

Velocity (about 100 km/s) and temperature (about 10 000 K) are kept invariants

↔ δ_3 et δ_5 are calculated:

$$A \equiv \rho_{\text{astro}} / \rho_{\text{lab}}, \quad B \equiv P_{\text{astro}} / P_{\text{lab}},$$

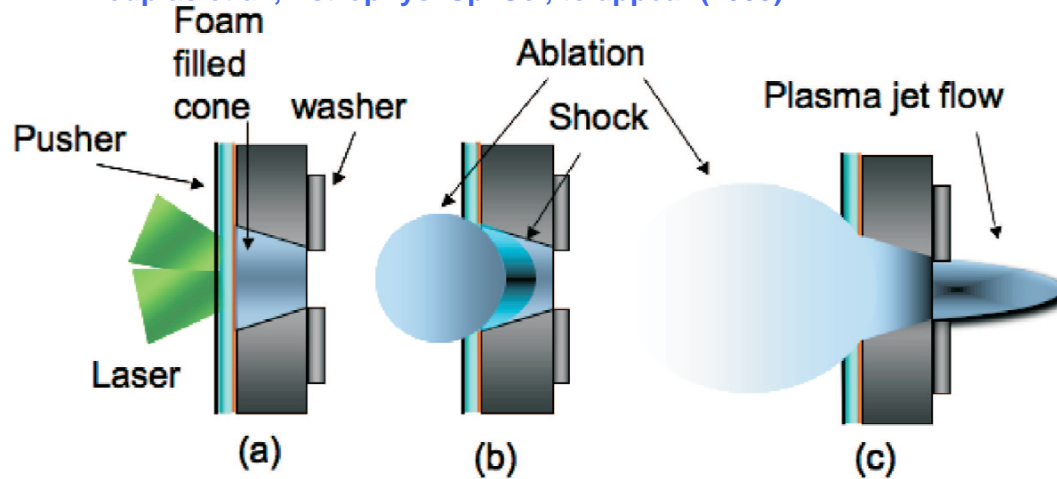
$$A \approx 3B \approx 2 \cdot 10^{-19}$$

Wrong, indeed !!!
Use length.

Physical quantities	Cold protostellar jet (HH111)	Experimental values	Scaling factor
Length (cm)	$3 \cdot 10^{17}$	0.1	$3 \cdot 10^{18}$
Time (s)	$3 \cdot 10^{10}$	10^{-8}	$3 \cdot 10^{18}$
Velocity (km/s)	100	100	1
Density (g/cm^3)	$2 \cdot 10^{-22}$	10^{-3}	$2 \cdot 10^{-19}$
Density (part/cm^3)	100	10^{17}	10^{-15}
Temperature (K)	10 000	10 000	1

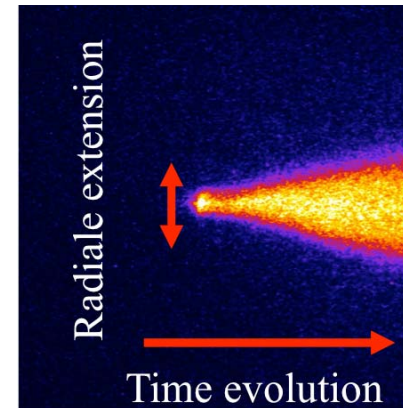
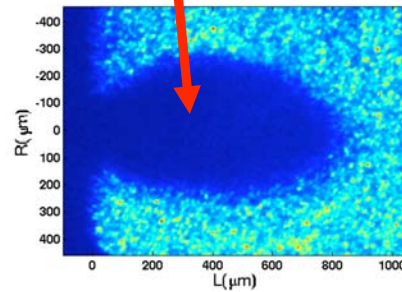
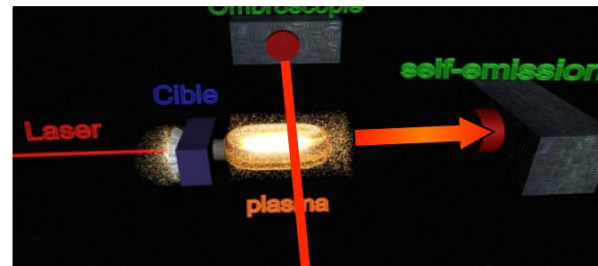
LASER TARGETS

B. Loupias et al., Phys. Rev. Lett. 99 (2007) 265001
 B. Loupias et al., Astrophys. Sp. Sc., to appear (2009)



- Différente **densité** : de 20mg/cc à 200mg/cc
- Mousse **dopée** : Br, Cl
- Avec et sans **cible solide**
- Différent **angle de cône** : 38° et 22°
- Différente **intensité laser** : $5 \cdot 10^{14} \text{W/cm}^2$, $7 \cdot 10^{13} \text{W/cm}^2$ ou $3 \cdot 10^{13} \text{W/cm}^2$
- Différent **profil laser**: Gaussien (RPP) ou supergaussien (PZP)
- Avec ou sans « **washer** »

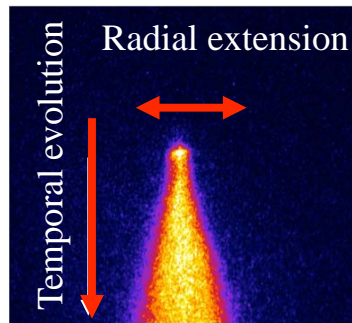
LULI 2000
laser facility



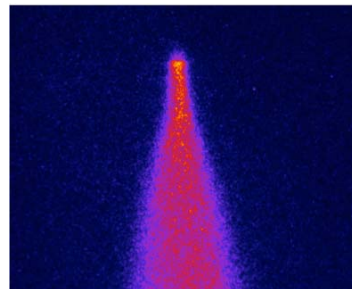
B. LOUPIAS, PhD Thesis, Paris, October 21, 2008

COMPARISON THEORY / JET EXPERIMENTS

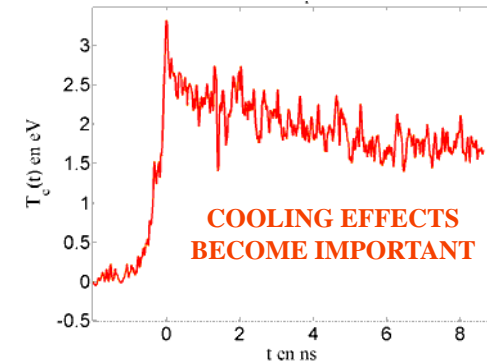
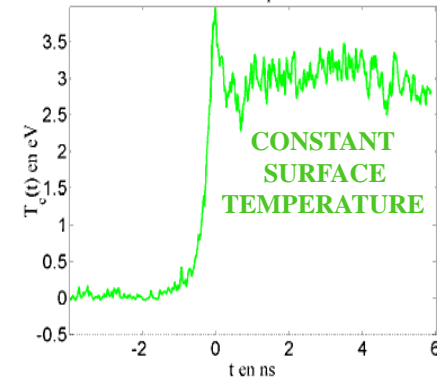
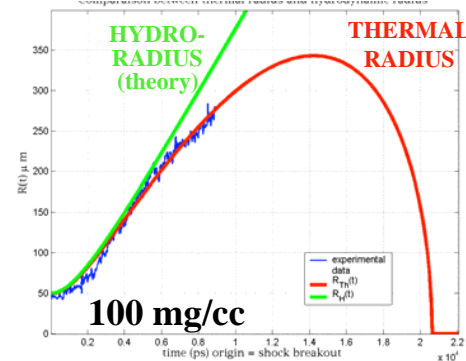
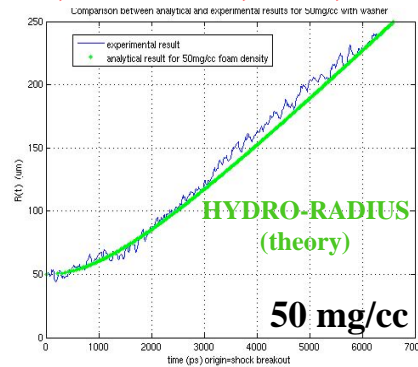
E. FALIZE, PhD Thesis, Paris, October 23, 2008



Into vacuum



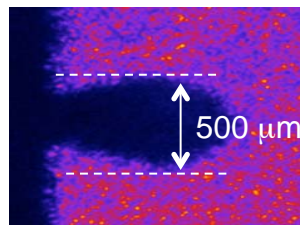
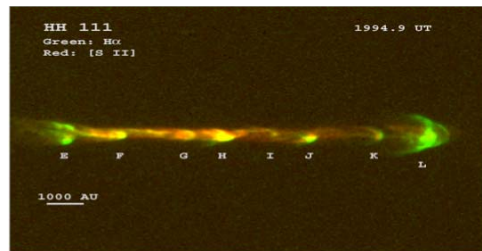
Into vacuum



	Re	$Pe = \frac{F_{conv}}{F_{cond}}$	$\chi = t_{cool}/t_{dyn}$	Mach	$\xi = \frac{\lambda_{mfp}}{L_{hydro}}$
YSO jet	10^7	10^6	0.1 - 10	10 - 30	10^{-7}
Exp. 5 ns	10^6	10^3	100	2	10^{-7}
Exp. 25 ns	10^5	10^2	10	20	10^{-7}

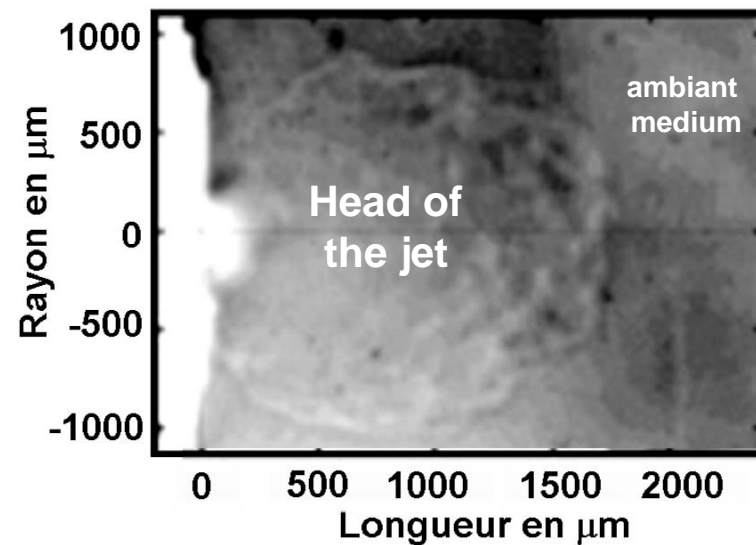
INFLUENCE of an AMBIANT MEDIUM

C.D. Gregory et al., PPCF 50(2008)124039



Into vacuum

Into argon gaz (ambient medium), $t = 30$ ns



Rayleigh – Taylor instability (RTI):

$$\omega = \sqrt{At.g.k}$$

$$At = \frac{\rho_2 - \rho_1}{\rho_2 + \rho_1} : \text{Atwood, } \rho_2: \text{heavy, } \rho_1: \text{light, } g: \text{deceleration, } k: \text{wave number}$$

$$\rho_2 = 1 \text{ mg/cc, } \rho_1 = 0.04 \text{ mg/cc, } \eta = \rho_{\text{jet}} / \rho_{\text{ambient}} = 25 (= 0.1 - 10), At = 1$$

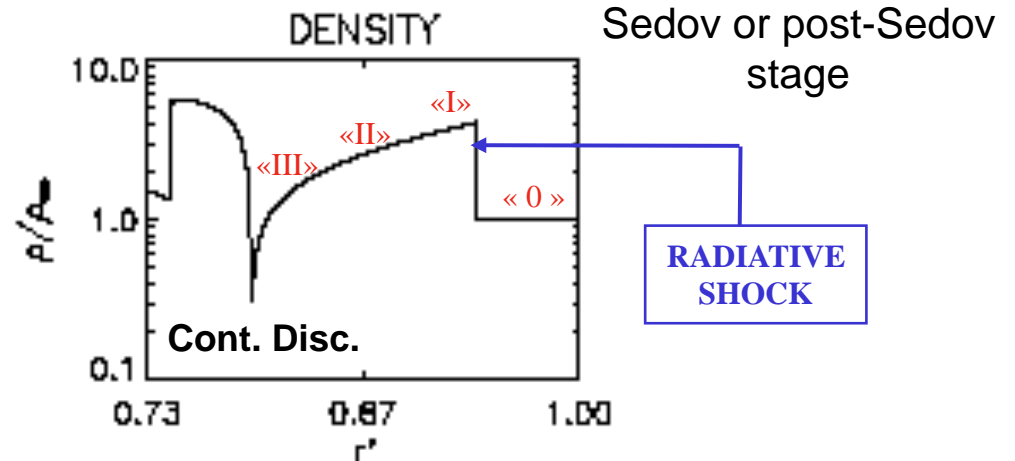
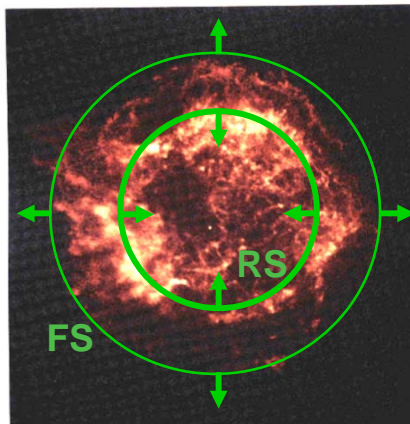
$$g = 60 \text{ (km/s)} / 30 \text{ (ns)} = 2 \text{ } \mu\text{m} / (\text{ns})^2, \lambda = 100 \text{ } \mu\text{m}$$

$$\tau_{RTI} = 1/\omega \approx 3 \text{ ns}$$

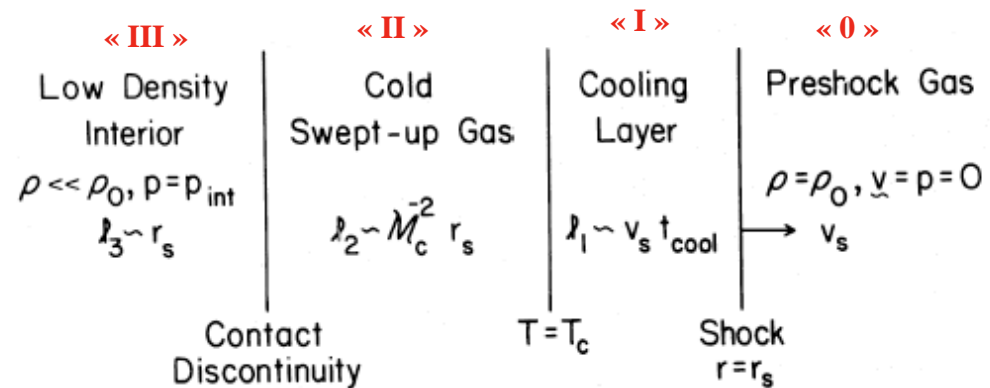
RTI may play a role in the structure of the BOW SHOCK

HIGHER RESOLUTION REQUIRED IN OBSERVATIONS + Compressible effects ...

RADIATIVE SHOCK in SNR 's



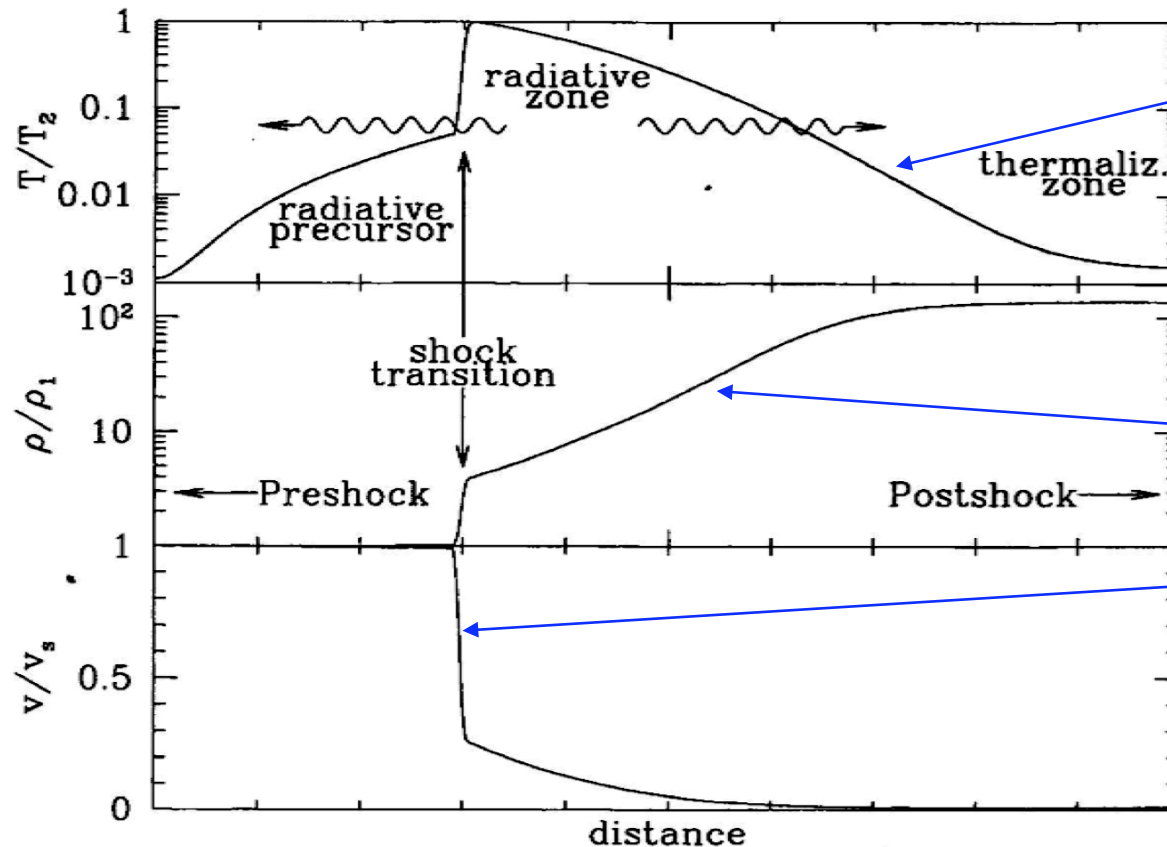
Dwarkadas and Chevalier, ApJ 497 (1998) 497



E. Bertschinger, ApJ 304(1986)154

RADIATIVE SHOCK in SNR 's

Motion of the Forward Radiative Shock



T decreases due to the cooling (radiative flux ahead the sock)

therefore

ρ increases (first the compression is 4 and becomes much larger)

The velocity is normalized to the shock velocity

Radiative precursor: the energy goes through the discontinuity and heats the medium ahead of the shock.

B.T. Draine & C.F. McKee, Annual Rev. Astron. Astrophys. 31, 373 (1993)

Also in supernovae: $\rho_{\text{downstr.}} / \rho_{\text{upst.}} = 7$ ($\gamma = 4/3$)



OPTICALLY THICK RADIATION HYDRODYNAMICS

- $\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot [\rho \vec{v}] = 0$
- $\left[\frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right] \vec{v} = -\frac{1}{\rho} \vec{\nabla} (P_{th} + P_{rad}),$ $P_{th} = \varepsilon_0 [Z] \rho^\mu T^\nu,$ $P_{rad} = a_R T^4 / 3$
 $\mu = \nu = 1, \text{ Ideal Gas}$
- $\frac{d}{dt} \left(\frac{P_{th}}{\gamma - 1} + E_{rad} \right) - \gamma \frac{P_{th} / (\gamma - 1) + P_{th} + E_{rad} + P_{rad}}{\rho} \frac{d\rho}{dt} = -\vec{\nabla} \cdot \vec{F}_{rad} - Q(\rho, T)$
 $\frac{d}{dt} = \left[\frac{\partial}{\partial t} + (\vec{v} \cdot \vec{\nabla}) \right]$
 $E_{rad} = a_R T^4$
 $\vec{F}_{rad} = -\kappa_{rad} \vec{\nabla} T, \quad \kappa_{rad} = \kappa_0 \rho^m T^n$ $m = -2, n = 7/2, \text{ Kramers opacity}$
 $Q(\rho, T) = \text{heating source/cooling}$ $\text{Stellar structure, stellar evolution}$

Invariance ?



SCALING INVARIANCE YES !!!

$$P_{\text{rad}}/P_{\text{th}} \ll 1 \text{ and } E_{\text{rad}}/E_{\text{th}} \ll 1$$

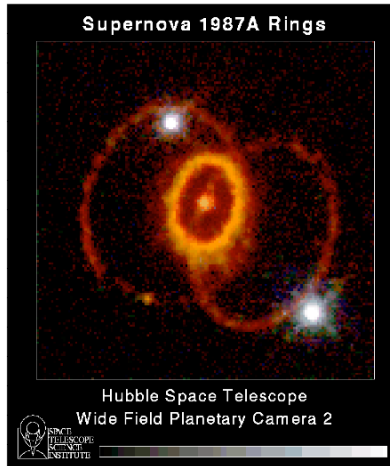
$\mu = \nu = 1$, Ideal Gas and $m = -2$, $n = 7/2$, Kramers opacity

quotients	Invariance absolue
x/\tilde{x}	$a^{[m+1/2-(n+1)\mu/\nu]\delta_3 + [(n+1)/\nu - 3/2]\delta_5}$
t/\tilde{t}	$a^{[m+1-(n+1)\mu/\nu]\delta_3 + [(n+1)/\nu - 2]\delta_5}$
$\rho/\tilde{\rho}$	a^{δ_3}
v/\tilde{v}	$a^{(\delta_5 - \delta_3)/2}$
P/\tilde{P}	a^{δ_5}
T/\tilde{T}	$a^{(\delta_5 - \mu\delta_3)/\nu}$
$\epsilon_0/\tilde{\epsilon}_0$	1
$F_{\text{rad}}/\tilde{F}_{\text{rad}}$	$a^{3\delta_5/2 - \delta_3/2}$
$\kappa_{\text{rad}}/\tilde{\kappa}_{\text{rad}}$	$a^{n\delta_5/\nu + [m - n\mu/\nu]\delta_3}$
$\kappa_0/\tilde{\kappa}_0$	1

Two free parameters again $\mathbf{A} \equiv \rho_{\text{astro}}/\rho_{\text{lab}}$, $\mathbf{B} \equiv P_{\text{astro}}/P_{\text{lab}}$,

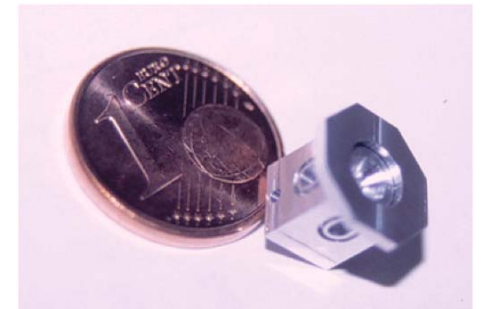
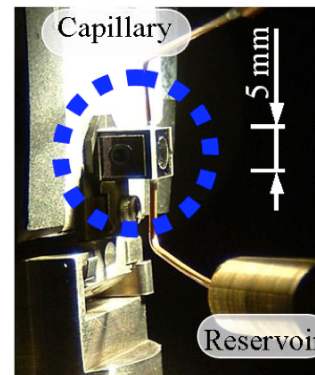
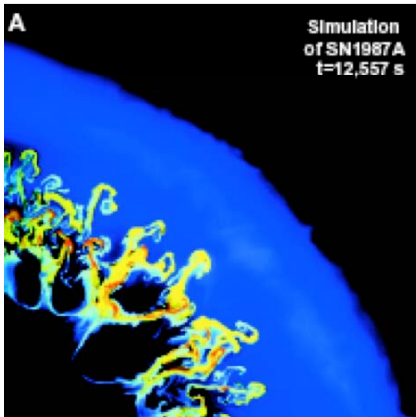
SCALING FACTORS

$$A \equiv \rho_{\text{astro}}/\rho_{\text{lab}}, \quad B \equiv P_{\text{astro}}/P_{\text{lab}}, \quad A \approx 10^8; \quad B \approx 3 \cdot 10^{-14}$$



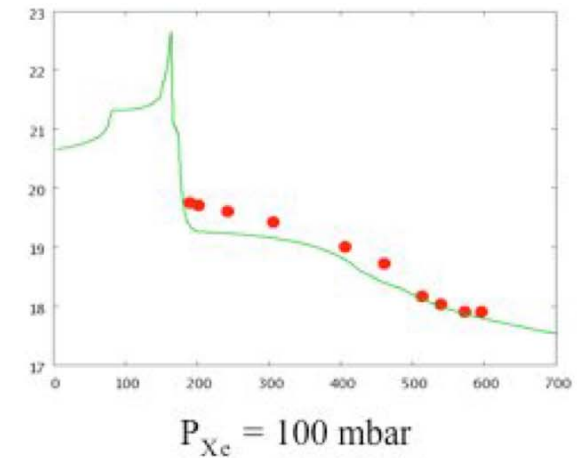
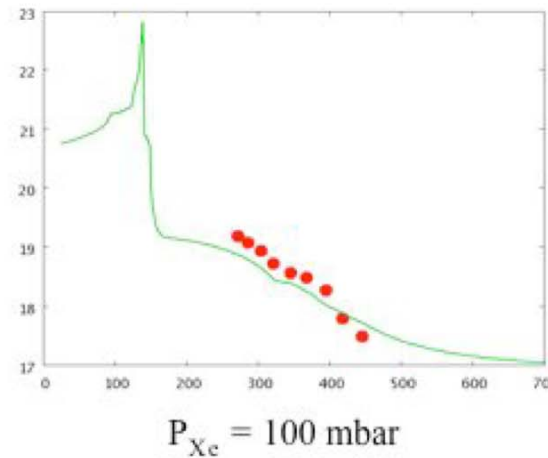
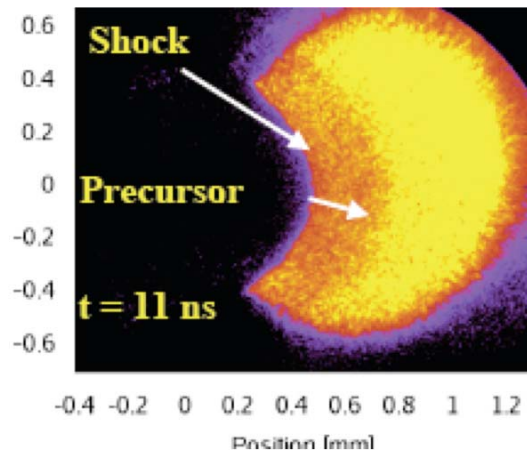
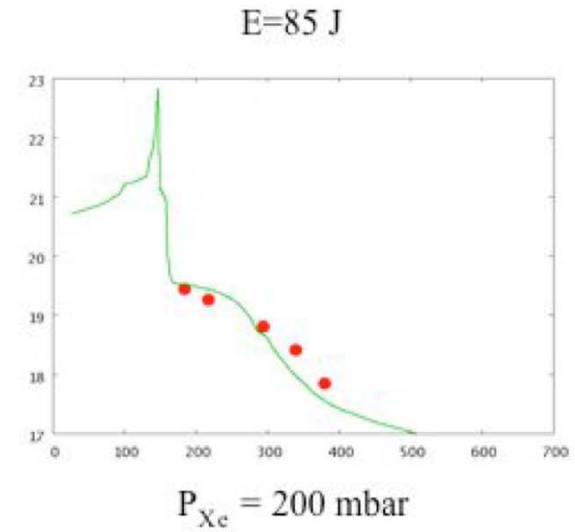
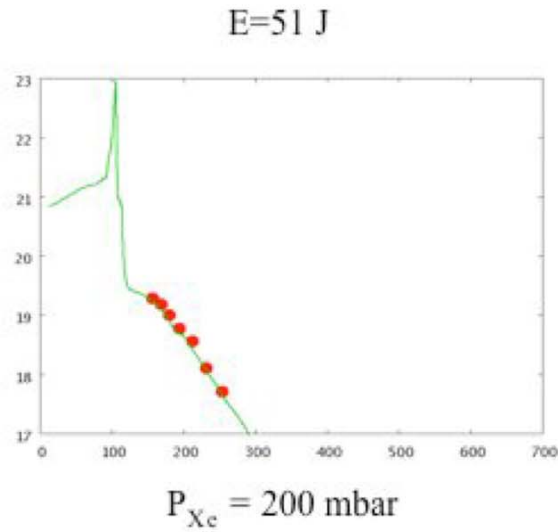
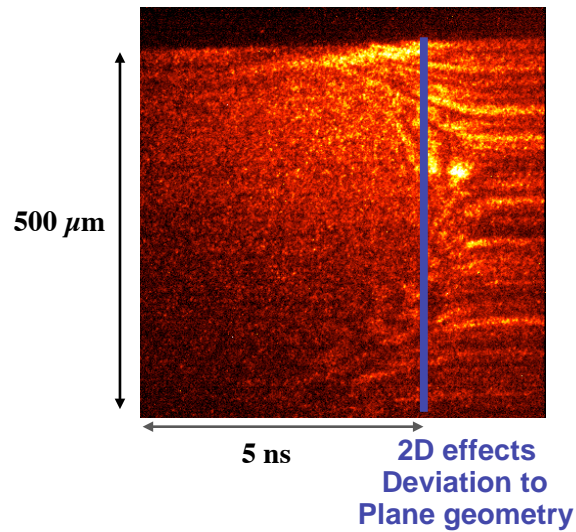
Muller et al. *Astron. Astrophys.* (1991)

Physical quantities	Supernova	Experiments	Scaling factors
Length (cm)	10^{12}	0.01 (100 microns)	10^{14}
Time (s)	3600	10^{-8}	$3.6 \cdot 10^{11}$
Velocity (km/s)	$c/2$!!!	100	10^3
Density (g/cm ³)	10^{-2}	10^{-5}	10^3
Temperature (K)	10^{10}	10 000	10^6





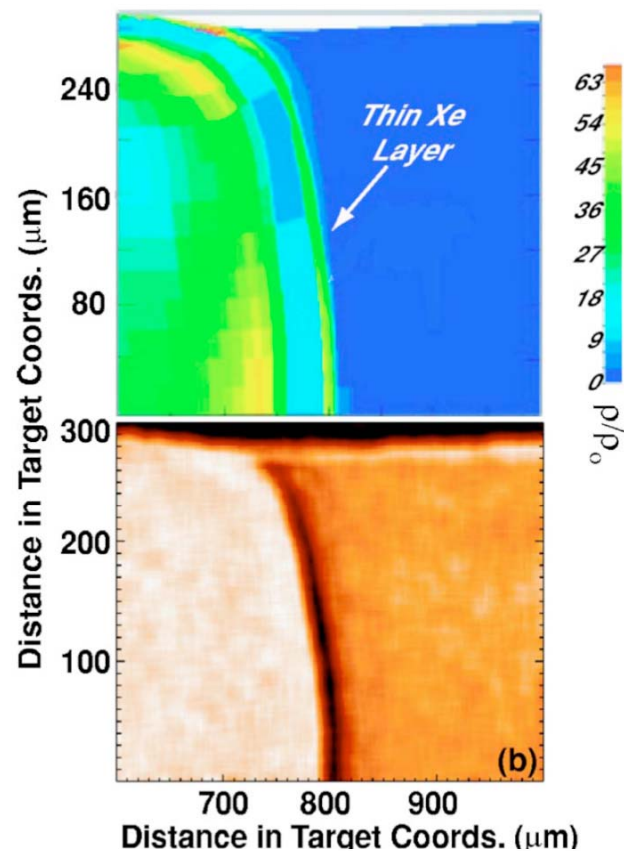
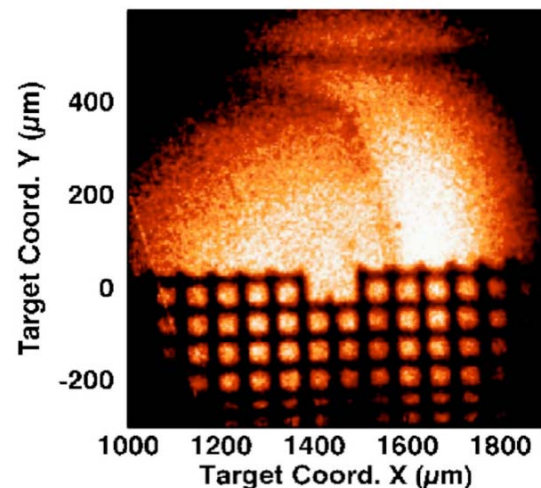
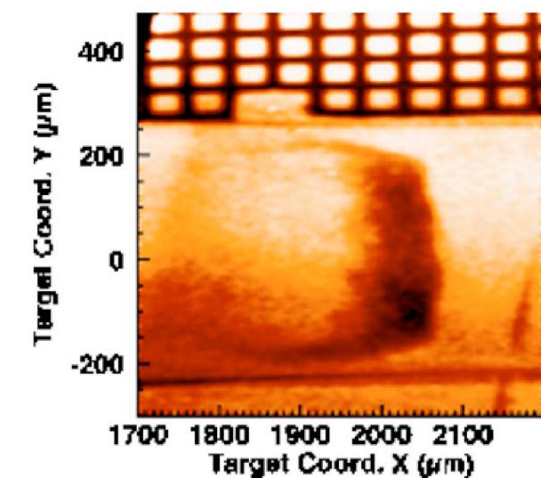
LULI EXPERIMENTS VS. NUMERICAL SIMULATION



Bouquet et al., PRL (2004), Koenig et al., APIP-AIP, CP926 (2007) 110, Michaut et al., ApSS, to appear (2009)

OMEGA EXPERIMENTS

Amy Reighard (Cooper), Paul Drake, Laurent Boireau, Paul students ...



High
compression
rate in
the shocked
material

FIG. 5. (Color online) (a) Density profile at 7 ns, from a 2D simulation of the experiment, using the FCI code. The shock is moving to the right. The color bar calibrates the density as a ratio to the initial gas density. (b) Simulated radiograph, using density data from (a). Poisson noise and a point-spread function from data are included.

Reighard et al., PoP 13 (2006) 032901



CONCLUSION

- 1) – For the first time, rigorous derivation of scaling laws have been made and the connection between experiments and astrophysical objects is 1 to 1
- 2) – Coherence and redundancy of the models
- 3) – Laboratory astrophysics is a relevant approach